## MATLAB

- You can download MatLab from Distrilog at http://distrilog.epfl.ch/main.aspx
- Q\&A forum on MatLab can be found at http://ch.mathworks.com/matlabcentral/answers/
- You can find a video tutorial on MatLab at http://ch.mathworks.com/academia/student center/tutorials/launchpad. html http://www.tutorialspoint.com/matlab/index.htm


## The Default MATLAB Desktop (2013a)



## Scalar Arithmetic Operations

## Symbol Operation

## MATLAB form

| $\wedge$ | exponentiation: $a^{b}$ | $\mathbf{a \wedge} \mathbf{b}$ |
| :--- | :--- | :--- |
| * | multiplication: $a b$ | $\mathbf{a * b}$ |
| / | right division: $a / b$ | $\mathbf{a} / \mathbf{b}$ |
| \ | left division: $b / \mathbf{a}$ | $\mathbf{a} \backslash \mathbf{b}$ |
| + | addition: $\mathbf{a}+\mathrm{b}$ | $\mathbf{a}+\mathbf{b}$ |
| - | subtraction: $\mathbf{a - b}$ | $\mathbf{a}-\mathbf{b}$ |

## Order of Precedence

- What do I really mean when I type

$$
8+3 * 5 \wedge 3
$$

?

- Many possibilities:

$$
\begin{aligned}
& (8+3) *(5 \wedge 3) \\
& 8+(3 *(5 \wedge 3)) \\
& 8+((3 * 5) \wedge 3)
\end{aligned}
$$

## Order of Precedence

PEMDAS

\[

\]

## Examples of Variables and Assignment

- Writing these two line produces

$$
\begin{array}{rlrl}
>A & =\operatorname{sqrt(4);} & \mathrm{A} \leftarrow \sqrt{4} \\
>A & =\tan (\mathrm{pi} / 4)+\mathrm{A} & \mathrm{~A} \leftarrow \tan \left(\frac{\pi}{4}\right)+2 \\
\mathbf{A} & =3 &
\end{array}
$$

- A semicolon at the end of the RHS expression suppresses the display.
- However, the assignment still takes place.


## Relational Operators

Compare two expressions or variables

$$
\left.\begin{array}{rll} 
& == & \text { equal to } \\
> & \text { greater than } & \mathbf{a}>\mathbf{b} \\
< & \text { less than } & \mathbf{a}<\mathbf{b} \\
>= & \text { greater or equal } & \mathbf{a}>=\mathbf{b} \\
<= & \text { less than or equal } & \mathbf{a}<=\mathbf{b} \\
\sim= & \text { not equal } & \mathbf{a} \sim \mathbf{b}
\end{array}\right] \begin{array}{ll}
\text { logical } 1 \text { if expression is true } \\
\text { logical } 0 & \text { if expression is false }
\end{array}
$$

## Relational Operators



- The result of the comparison is a value that can be used in an assignment.
- The precedence of relational operators is lower than that of addition and subtraction (PEMDAS).


## Saving the Workspace

When you "quit" Matlab, the variables in the workspace are erased from memory.

If you need them for later use, you must save them.

## >> save

saves all of the variables in the workspace into a file called matlab . mat (it is saved in the current directory)

## Saving the Workspace

## >> Save Claudia

saves all of the variables in the workspace into a file called Claudia . mat

## >> save Important A B C D*

saves the variables A, B, C and any variable beginning with $\mathbf{D}$ into a file called Important.mat

## >> load Claudia

loads all of the variables from the file Claudia.mat

There are no known security problems with load.

Hence, you can safely send (as attachment), receive and use . mat files from others.

## Loading Excel Files

>> xlsread('Claudia.xls')
>> xlsread('Claudia.xls','Sheet1','B10:F28')

Loading text Files
Create a .dat file with the following format >> dlmwrite('Claudia.dat', A,' ,')
>> csvread('Claudia.dat')
>> csvread('Claudia.dat', 0, 2)

Another option for reading a text file is >> textread('Claudia.dat')

## Introduction to arrays

- An array is an ordered collection of real numbers
- Arrays are the primary building blocks in MatLab
- Scalar

$$
a=[1]
$$

(1 row, 1 column)

- Vector

$$
a=[1,-5,3,2]
$$

(1 row, 4 columns)

- General 2D arrays

$$
\begin{equation*}
a=[1.2,-3.2,1.0 ; 3.1,92,0.0] \tag{2-by-3}
\end{equation*}
$$

# Defining arrays 

Construction:

- Manual
- Incremental
- linspace
- transpose: "’"
- zeros
- ones
- rand/randn


## Row vectors - incremental construction

$\gg r=3: 2: 10$


Syntax:
first element : increment : limit

## Linspace command

- also creates a linearly spaced row vector
- number of elements are specified instead of increment
Syntax: linspace( $\mathrm{xf}, \mathrm{xl}, \mathrm{n}$ )
- xf - first element
- xl - last element
- n - number of evenly-spaced elements
>> A = linspace $(3,9,4)$
A =



## zeros

- Syntax:


## $z \operatorname{eros}(n, m)$

- Create an array of zeros that has
- n - rows
- m - columns

$$
\begin{array}{ll}
\gg=\operatorname{zeros}(1,3) & \gg c=z \operatorname{cros}(3,2) \\
r= & c=
\end{array}
$$

0
0
0


00
$0 \quad 0$
$0 \quad 0$

## ones

- Syntax:
- Create an array of ones that has
- n - rows
- m-columns

$$
\begin{aligned}
& \gg r=\operatorname{ones}(1,3) \\
& r= \\
& 1 \quad 1 \quad 1 \\
& 11 \\
& 11 \\
& 1 \quad 1 \\
& \text { >> c }=\operatorname{ones}(3,2) \\
& \text { c = }
\end{aligned}
$$

- Syntax:


## rand (n,m)

- Create an array of random numbers
- n - rows
- m - columns
uniform random distribution between 0 and 1
$\gg r=r a n d(2,3)$
$r=$
0.9501
0.2311
0.6068
0.8147
0.1270
0.6324


## Array column concatenation

$$
\begin{aligned}
& \text { >> A }=\operatorname{ones}(2,3) \\
& \text { A = } \\
& 1 \quad 1 \quad 1 \\
& 1 \quad 1 \\
& 1 \\
& \gg C=\left[\begin{array}{ll}
A & B
\end{array}\right] \\
& \text { >> B = zeros(2,2) } \\
& \text { B = }
\end{aligned}
$$

## Array row concatenation

$$
\mathrm{C}=
$$



| 1 | 1 | 1 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 0 | 0 |
| 3 | 3 | 3 | 3 | 3 |

## The transpose operator

- The transpose operator converts
- (row vector) $\longrightarrow$ (column vector)
- (column vector)' $\longrightarrow$ (row vector)
$-\left[\begin{array}{ll}1 & 2 \\ 3 & 4\end{array}\right]^{\prime} \longrightarrow\left[\begin{array}{ll}1 & 3 \\ 2 & 4\end{array}\right]$
>>A = [1, 2 ; 3, 4] >> B = A'
A $=$
B =
12
13
34
2
4
size(A) returns a $1 \times 2$ array that contains:
- number of rows of $\mathbf{A}$
- number of columns $\mathbf{A}$

Example:
$\gg A=\operatorname{rand}(5,6) ; \quad \gg d=\operatorname{size}(A)$
>> size(A)
d =
ans =
5
6


- Syntax: $\quad n=\operatorname{size}(A, 1)$
- $\mathbf{n}$ - number of rows of $\mathbf{A}$
- Syntax:

$$
m=\operatorname{size}(A, 2)
$$

- m - number of columns A

Example:
>> $n=\operatorname{size}(A, 1)$
>> m = $\operatorname{size}(A, 2)$
n =
m =

## numel command - getting number of elements

- Syntax:

$$
\mathrm{n}=\operatorname{numel}(\mathrm{A})
$$

- $\mathbf{n}$ - number of elements of $\mathbf{A}$


## Example:

```
>> r = ones(1,4)
r =
    1 1 1 1 1
>> n = numel(r)
n =
```

    4
    >> $A=\operatorname{ones}(2,4)$
A =

| 1 | 1 | 1 | 1 |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 1 | 1 |
| $\gg$ | $n$ | $=$ | numel $(A)$ |

n =

## Accessing elements or parts of an array



## Find function

If $A$ is an array,

- find(A) returns a row vector containing the linear indexes of the non-zero elements of A
- Example: (row vector)



## Using the find function

Example: Set all negative elements of array A to zero

$$
\begin{aligned}
& \begin{array}{l}
\text { > A = }\left[\begin{array}{llllll}
2 & 1 & ; & -2 & -3 & 4 \\
\hline
\end{array}\right] ; \quad A=\left[\begin{array}{cc}
2 & 1 \\
-2 & -3 \\
4 & -5
\end{array}\right] \\
\text { Lindx }=
\end{array}
\end{aligned}
$$

Question Indexing

| B = | >> $\mathrm{B}(2,3)$ |
| :---: | :---: |
| 100 | ans |
| 010 |  |
| $0 \quad 0 \quad 1$ | >> $B(:, 2: 3)$ |
|  | ans |
|  |  |

$$
\begin{array}{ll}
0 & 0 \\
1 & 0 \\
0 & 1
\end{array}
$$

## Question

>> A = 13:-3:2 - 3; B = linspace(13,1,5);
>> isequal(A,B)

B. $\mathrm{ans}=$ 0

$$
\begin{aligned}
& A= \\
& 13 \\
& \\
& \\
& \\
& B= \\
& 10
\end{aligned}
$$

## Review: Relational operators

Relational operators are used to compare variables.
There are 6 comparisons:

- "equal to", using ==
- "not equal to", using ~=
- "less than", using <
- "less than or equal to", using <=
- "greater than", using >
- "greater than or equal to", using >=

The result of a comparison is of class logical
Two values: true (1) or false (0),

## Relational operations on vectors

- Example

$$
\left.\begin{array}{rl}
\gg & =\left[\begin{array}{rrr}
-3 & \mathbf{2} & \mathbf{1} \\
> & \mathbf{5}
\end{array}\right] ; \\
\gg & -3=1 ? \\
& -1
\end{array}\right) ;
$$

$>A=B$
ans =

$\gg A<=B$
ans $=$


Note: the result of relational operations are logical variables 1-true, 0-false

## Logical Operators

## If A and B are scalars (double or logical), then

A\&B is TRUE (1) if A and B are both nonzero, otherwise it is FALSE (0). This is the logical AND operator.
$\mathbf{A} \mid \mathbf{B}$ is TRUE (1) if either $\mathbf{A}$ or $\mathbf{B}$ are nonzero, otherwise it is FALSE ( 0 ). This is the logical OR operator.
$\operatorname{xor}(\mathbf{A}, \mathbf{B})$ is TRUE (1) if one argument is 0 and the other is nonzero, otherwise it is FALSE (0). This is the logical EXCLUSIVE OR operator.
$\sim \mathbf{A}$ is TRUE if $\mathbf{A}$ is 0 , and FALSE if $\mathbf{A}$ is nonzero. This is the logical NEGATION operator.

For arrays, the operations are applied element-wise

## Indexing with logical arrays

## Example

$$
-5 \leq A(i, j) \leq-2
$$

Set all elements in array $\mathbf{A}$ with values between -5 and -2 to zero

$$
\begin{aligned}
& \begin{array}{l}
>\mathrm{A}=\left[\begin{array}{llllll}
2 & -3 & ; & -5 & 1.9
\end{array}\right] ; \quad A=\left[\begin{array}{ccc}
2 & -3 \\
-5 & -1.9
\end{array}\right] \\
>\operatorname{Indx}=\mathrm{A}<=-2 \& A>=-5
\end{array} \\
& \text { Indx = } \\
& 0 \quad 1 \\
& 1 \\
& 0 \\
& \begin{array}{ll}
\gg A(\text { Indx }) & =0 \\
A= & 0 \\
2 & -1.9
\end{array}
\end{aligned}
$$

## Logical function any

$$
\gg L=\left[\begin{array}{lllllllll}
1 & 0 & 1 & 0 & ; & 0 & 0 & 0
\end{array}\right] ;
$$

> A = any(L)
A =


$$
L=\left[\begin{array}{ll|l|l}
1 & 0 & 1 & 0 \\
\hline 1 & 0 & 0 & 0 \\
\hline
\end{array}\right]
$$

any (L): determines if any element in the column is nonzero

$$
\gg B=\operatorname{any}(L, 2)
$$

$$
B=
$$

any(L,2): determines if any element in the row is nonzero

## Logical function all

$$
\begin{aligned}
& \text { >> L = [ } 110100 ; 10000] ; \\
& \text { >> C }=\text { all(L) } \\
& \text { C = } \\
& L=\left[\begin{array}{cccc}
\left.\left.\begin{array}{|c|ccc}
1 & 0 & 1 & 0 \\
\hline 1 & 0 & 0 & 0
\end{array}\right] .\right] ~
\end{array}\right.
\end{aligned}
$$

all(L): determines if all elements in the column are nonzero

$$
\gg D=\operatorname{all}(L, 2)
$$

D =
all( $\mathrm{L}, \mathbf{2 )}$ : determines if all elements in the row are nonzero

## Scalar and short circuit \&\& (and) and || (or)

\% Variables b and a must be scalars
\% and defined

$$
x=(b \sim=0) \& \&(a / b>18.5)
$$

left expression is evaluated first

$$
\begin{aligned}
& \text { if ( } \mathrm{b} \sim=0 \text { ) is false (i.e. } \mathrm{b}=0 \text { ) } \\
& \text { x = false } \\
& \text { without evaluating right expression }
\end{aligned}
$$

otherwise
( $a / b>18.5$ ) is evaluated and the result is assigned to x

## if and end statements

To conditionally control the execution of statements

## if condition

## statements

## end

- If condition is TRUE (or nonzero), the statements between the if and end are executed.
- Otherwise, they are not executed.
- Execution continues with any statements after the end.


## if, else and end statements

## if condition <br> statements1 <br> else <br> statements2 <br> end

- If condition is TRUE, statements1 are executed.
- Otherwise, statements2 are executed.
- Execution continues with any statements after the end.


## if, elseif and end statements

| if exp_1 <br> statements1 <br> elseif exp_2 <br> statements2 <br> elseif exp_3 <br> statements3 <br> end <br> more statements |
| :---: |
|  |  |
|  |  |
|  |  |
|  |  |



Could have also used a single else before the end

## Piecewise linear function

\% check if x is a scalar and a double and a
\% real number

```
if isscalar(x) && isa(x,'double') && isreal(x)
    if x < -1
        y = -1;
    elseif x < 2
        y = x;
    elseif x < 5
        y = 3 - x;
    else
        y = -2;
    end
else
    error('x should be a real scalar');
end
```


## For Loops

The most common value for array is a row vector of integers, starting at , and increasing to a limit


The array is simply the row vector

$$
\left[\begin{array}{llllll}
1 & 2 & 3 & 4 & \cdots & n
\end{array}\right]
$$

Hence, the statements are executed $\mathbf{n}$ times.

- The first time through, the value of x is set equal to $\mathbf{1}$;
- the 'th time through, the value of $\mathbf{x}$ is set equal to $\mathbf{k}$.


## For Loops Example

$$
\begin{array}{ll}
\text { for } x=1: 3 & \text { for } x=1: 3 \\
\quad x & \text { disp(['x is ' num2str }(x)]) \\
\text { end } & x \text { is } 1 \\
x=1 & x \text { is } 2 \\
x=2 & x \text { is } 3 \\
x=3 &
\end{array}
$$

$$
\begin{aligned}
& A=\left[\begin{array}{ll}
3 & 2 \\
1
\end{array}\right] ; \\
& \text { for } x=A \\
& \quad \text { disp(['x is ' num2str }(x)]) \\
& \text { end } \\
& x \text { is } 3 \\
& x \text { is } 2 \\
& x \text { is } 1
\end{aligned}
$$

## nested for loops



## Plot Function

If $x$ and $y$ are vectors (i.e., a row or column vector), of the same length, then

- plot( $x, y$ ) plots the elements of $y$ versus the elements of $x$
- plot(y) plots the elements of $y$ versus its indexes
- (more later - see help for options)


## Plot examples

Plot $\sin (w)$ for $w$ between $-p i$ and $p i$

$$
\begin{aligned}
& x=\operatorname{linspace}(-p i, p i) ; \\
& \operatorname{plot}(x, \sin (x))
\end{aligned}
$$

Using for loop


$$
\begin{aligned}
& x=\operatorname{linspace}(-p i, p i) ; \\
& y=z e r o s(\operatorname{size}(x)) ;
\end{aligned}
$$

for $k=1$ : $\operatorname{size}(x, 2)$; $y(k)=\sin (x(k)) ;$
end
plot ( $x, y$ )


Plot multiple diagrams
x = linspace(-pi,pi);
plot ( $\left.x, \sin (x),{ }^{\prime} b^{\prime}\right)$;
hold on;
plot(x, $\cos (x)$, 'r') ;

figure(); subplot(2,1,1); plot(x,sin(x), 'b'); subplot(2,1,2);
plot(x, $\cos (x)$, $r^{\prime}$ );


## Question 5

The function 'hist' bins your data and plots it as a histogram. What would the output be for the following code?
>> A = rand(1,1000); hist(A)


## Statistical Functions

If $A$ is a matrix with size $n * m$, then

- mean(A,k) returns the average of matrix $A$ in dimension $k$ (i.e. if $k=1$ we get the average of all the columns)
- $\min (\mathrm{A},[\mathrm{l}, \mathrm{k}) / \max (\mathrm{A},[\mathrm{l}, \mathrm{k})$ returns the minimum/maximum of matrix $A$ in dimension $k$ (i.e. if $\mathrm{k}=1$ we get the minimum/maximum of all the columns)
- $\operatorname{var}(\mathrm{A})$ returns a row vector with the variance of all the columns of matrix $A$

