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Master of Science EPF-ETH degree in **Nuclear Engineering**
Medical radiation physics

08. MRI

Introduction

- Limits of imaging techniques using X rays
 - Mostly anatomical
 - Limited contrast of soft tissues



NMR: The basics

Electric charge rotation \rightarrow magnetic moment μ



$$\mu = I A$$

Orbital electron: $\mu = \frac{ev}{2\pi r} \pi r^2 = \frac{erv}{2}$

Mass in rotation \rightarrow kinetic momentum
Spin

$$\vec{L} = \vec{r} \wedge m \vec{v} = J \omega$$

$$|\omega| = 2\pi \nu$$

$$L = m_e v r$$



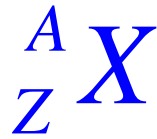
$$\mu = \frac{e}{2m_e} L = \gamma_{\text{orbital}} L$$

Orbital gyromagnetic ratio

Same phenomenon for electron: electronic gyromagnetic ratio

Same phenomenon for some nucleus: nuclear gyromagnetic ratio

Useful nucleus in NMR



Z atomic number

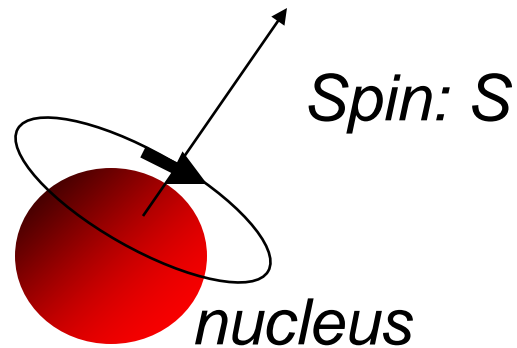
A mass number

When A and Z even → no NMR phenomenon

When A or Z odd → NMR phenomenon

When A or Z odd

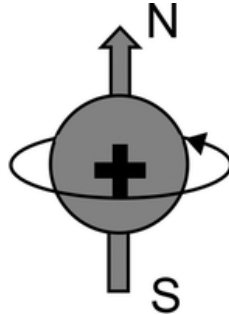
protons, neutrons movement (mass) → quantified kinetic momentum



$$S = \{0, \frac{1}{2}, 1, \frac{3}{2} \dots\}$$

Origin of the signal in MRI: Nucleus

Mass: spin (\vec{S})



Charges: magnetic momentum ($\vec{\mu}$)

- Rotation of a mass leads to a kinetic momentum
 - Quantified spin
 - **Proton**, neutron and electron have a spin equal to 1/2
- Rotation of charges leads to a magnetic momentum (small magnet)

$$\vec{\mu} = \gamma \cdot \vec{S} \quad \gamma : \text{Gyromagnetic ratio}$$

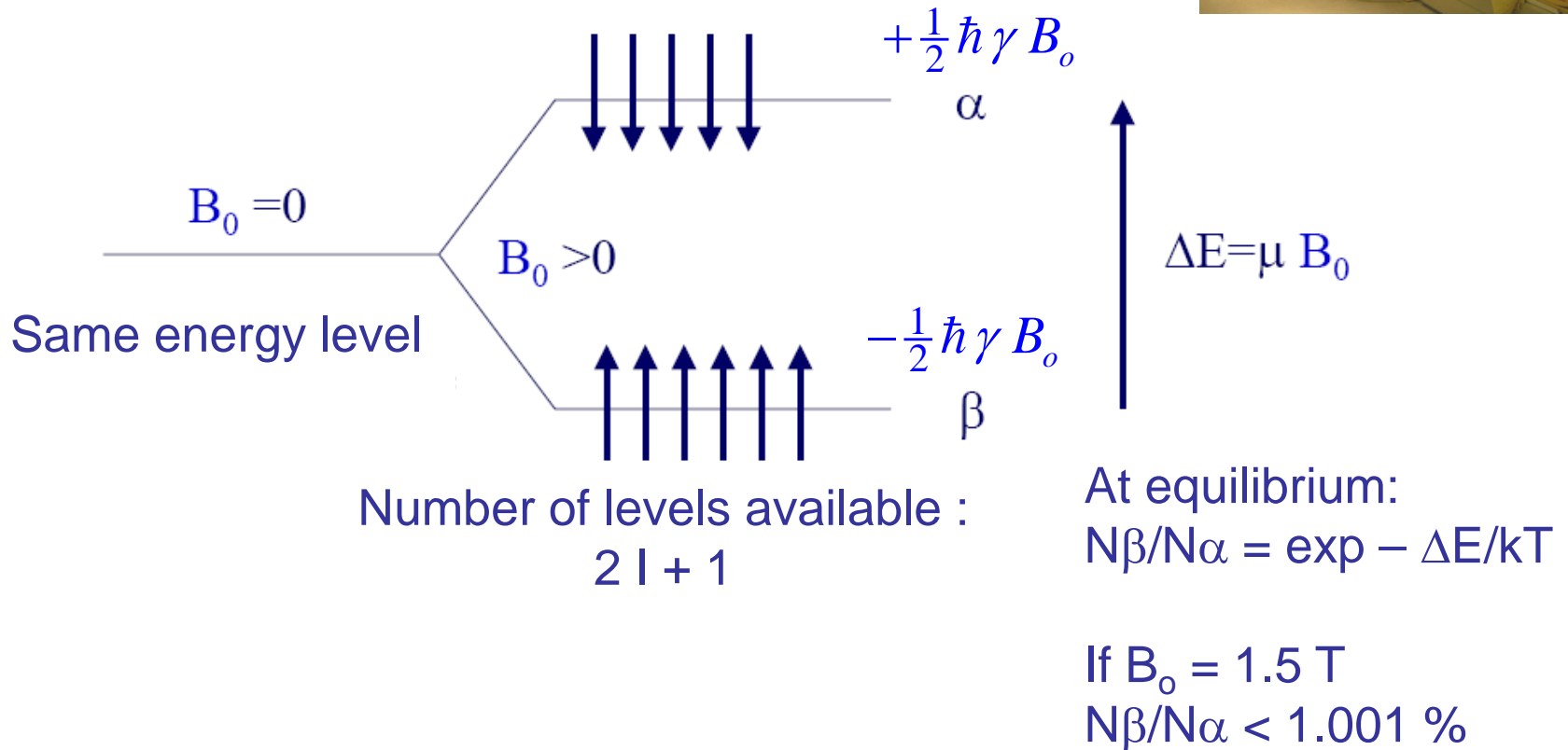
MRI : imaging of hydrogen nuclei → proton imaging

Nucleus properties : spin values

Z	Even	Odd
A		
Even	$I=0$ Ex: ^{12}C , ^{16}O	$I = 1, 2, 3, \dots$ Ex: ^{14}N , ^2H
Odd	$I = 1/2, 3/2, 5/2, \dots$ Ex: ^{13}C , ^{17}O , ^1H , ^{15}N , ^{19}F , ^{31}P	

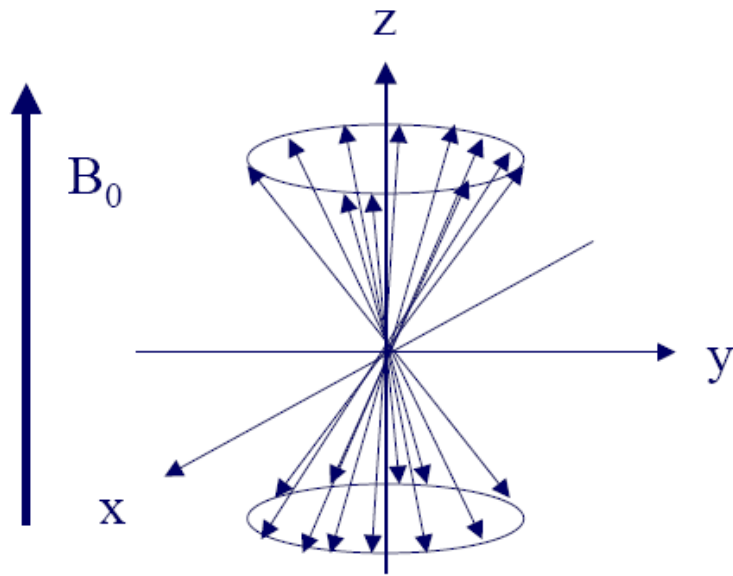
Effect of a static magnetic field on a magnetic momentum

1. Splitting of energy levels

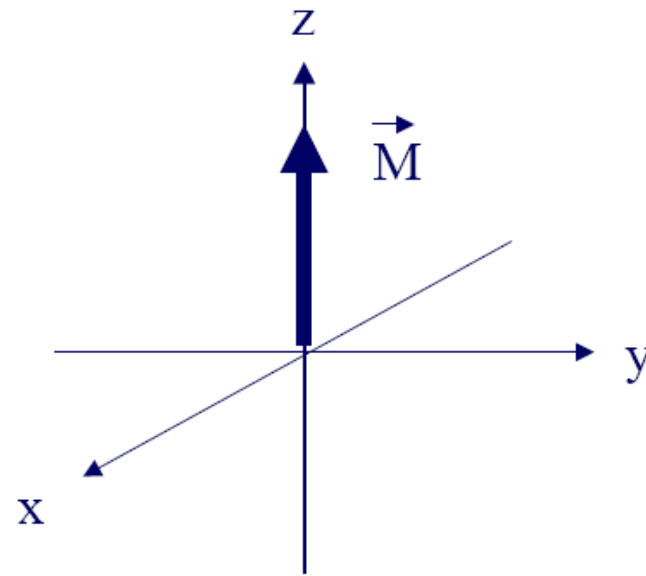


Effect of a static magnetic field on a magnetic momentum

2. A macroscopic magnetization appears



Set of spin $\frac{1}{2}$
 $N_\beta > N_\alpha$



\vec{M} = Macroscopic magnetization

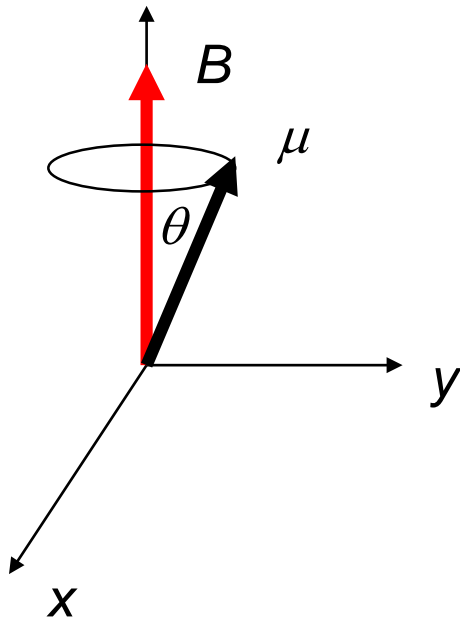
Effect of a static magnetic field on a magnetic momentum

A magnetic field B on a current loop (small magnet or magnetic moment)

→ Torque

$$\vec{C} = \vec{\mu} \wedge \vec{B} \quad \text{remember: } \vec{F} = \frac{d\vec{p}}{dt} \quad ; \quad \vec{C} = \frac{d\vec{L}}{dt} = \frac{d\vec{I}}{dt} \quad ; \quad \vec{\mu} = \gamma \vec{I}$$

$$\frac{d\vec{I}}{dt} = \vec{\mu} \wedge \vec{B} \Rightarrow \frac{d\vec{\mu}}{dt} = \gamma \vec{\mu} \wedge \vec{B} \Rightarrow \vec{\omega} = \gamma \vec{B} \Leftrightarrow \nu = \frac{\gamma}{2\pi} B$$



→ M rotates around B at Larmor frequency

Associated potential energy: $E = \vec{\mu} \cdot \vec{B}$

Effect of a static magnetic field on a magnetic momentum

3. Precession of M around B_0

Spinning top in gravitation field



Magnetic moment in a magnetic field (proton)



$$\nu = \frac{\gamma}{2\pi} \cdot B_0$$

- The spinning frequency is proportional to the static magnetic field B_0 (Larmor frequency)
- For proton : $\nu = 42.58 \text{ MHz @ } 1 \text{ T}$

Nuclei used in NMR

<i>Nuclei</i>	<i>S</i>	<i>isotopic %.</i>	<i>sensibility</i>	<i>Larmor frequency (MHz/T)</i>
<i>H-1</i>	<i>1/2</i>	<i>99.98</i>	<i>1</i>	<i>42.576</i>
<i>H-2</i>	<i>1</i>	<i>0.015</i>	<i>0.0096</i>	<i>6.535</i>
<i>P-31</i>	<i>1/2</i>	<i>100</i>	<i>0.0664</i>	<i>17.236</i>
<i>F-19</i>	<i>1/2</i>	<i>100</i>	<i>0.834</i>	<i>40.055</i>
<i>C-13</i>	<i>1/2</i>	<i>1.108</i>	<i>0.0159</i>	<i>10.705</i>
<i>N-15</i>	<i>1/2</i>	<i>0.365</i>	<i>0.00104</i>	<i>4.315</i>
<i>O-17</i>	<i>5/2</i>	<i>0.037</i>	<i>0.0291</i>	<i>5.772</i>

(for electron: 176 GHz/T)

NMR or MRI major steps

1

POLARIZATION

2

RESONANCE

3

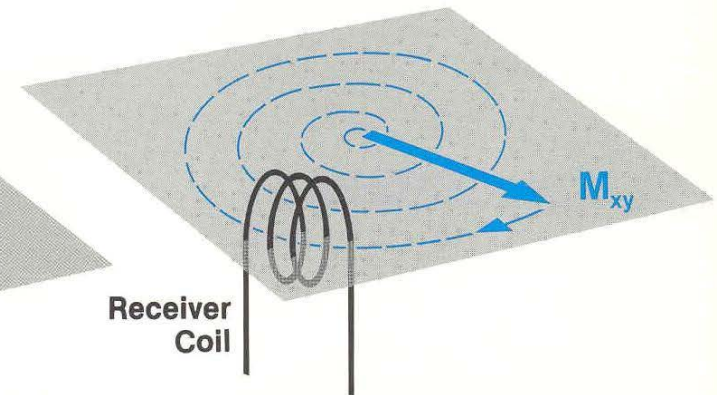
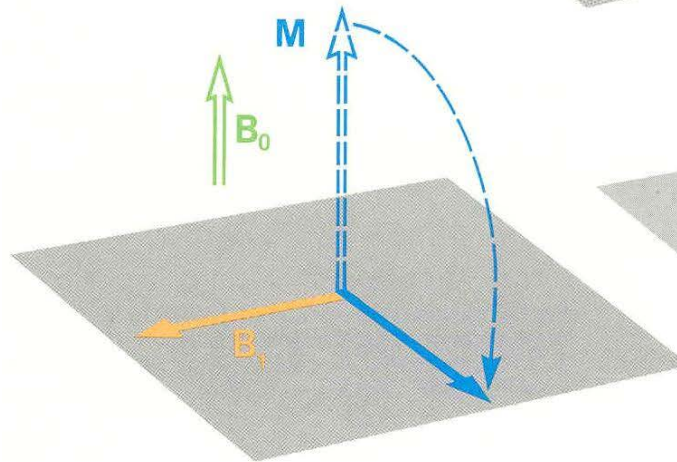
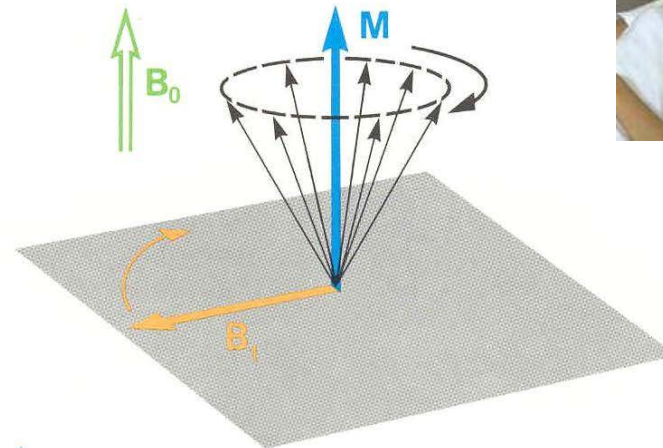
RELAXATION

Magnetic resonance experiment

A radiofrequency corresponds to a rotating magnetic field B_1

Resonance condition :
 B_1 frequency equals
the Larmor frequency

M rotates around
 B_0 and B_1

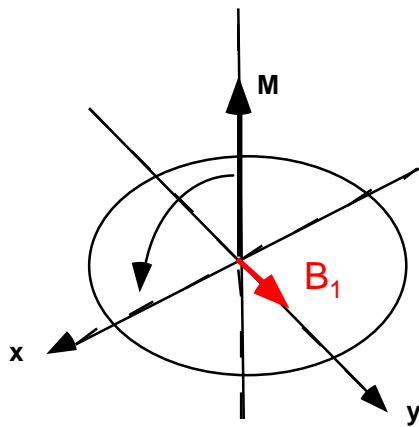


Bloch equation

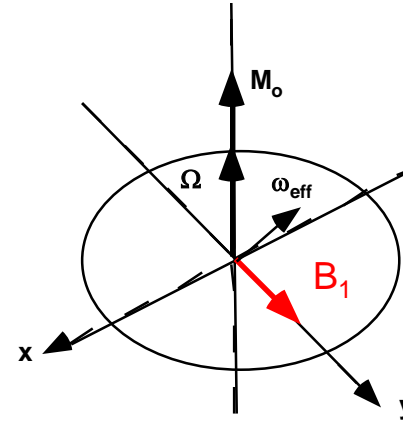
$$\dot{M} = \gamma M \wedge B - R\{M - M_o\} = \begin{cases} \dot{M}_x = \gamma [M_y B_z - M_z B_y] - M_x / T_2 \\ \dot{M}_y = \gamma [M_z B_x - M_x B_z] - M_y / T_2 \\ \dot{M}_z = \gamma [M_x B_y - M_y B_x] - (M_z - M_o) / T_1 \end{cases}$$



ν Larmor = ν excitation



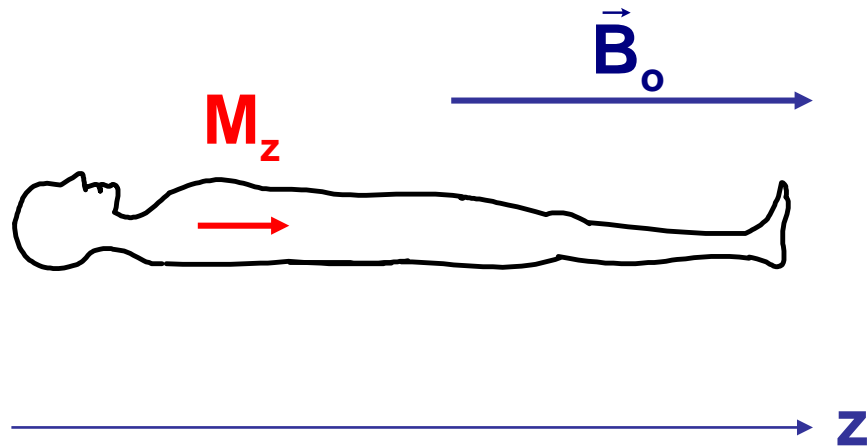
ν Larmor \neq ν excitation



$$\alpha = \gamma \int B_1(t) dt \quad (\text{radians})$$

Principle of MRI

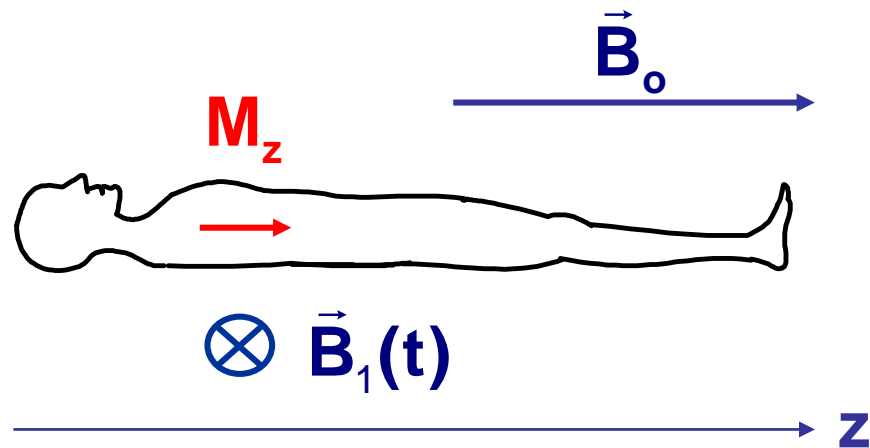
- The patient is placed in a static magnetic field (B_0)



B_0 creates \vec{M} which projection along z is M_z

Principle of MRI

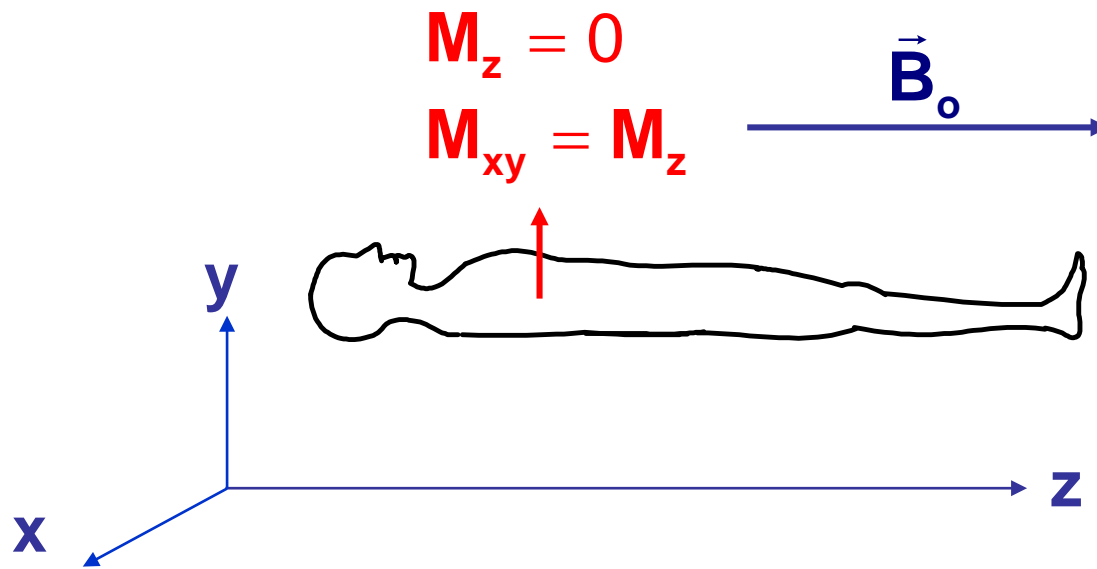
- The direction of M_z is modified by applying a radio frequency, $B_1(t)$, at Larmor frequency (42 MHz/T)
- M_z rotates around B_1 and B_0



Use of an excitation antenna: tilt of M_z in the transverse plane x,y . $M_z \rightarrow M_{xy}$

Principle of MRI

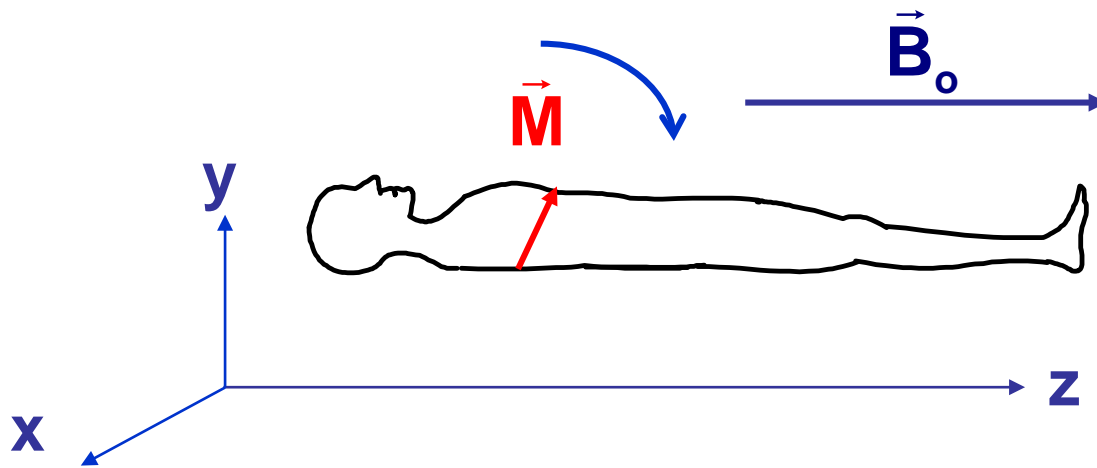
- For a tilt of 90° M_z is now equal to 0



The magnetization vector is now in the transverse plane and rotates around B_0 (B_1 is switched off). One can detect M_{xy} in that plane with a reception antenna.

Principle of MRI

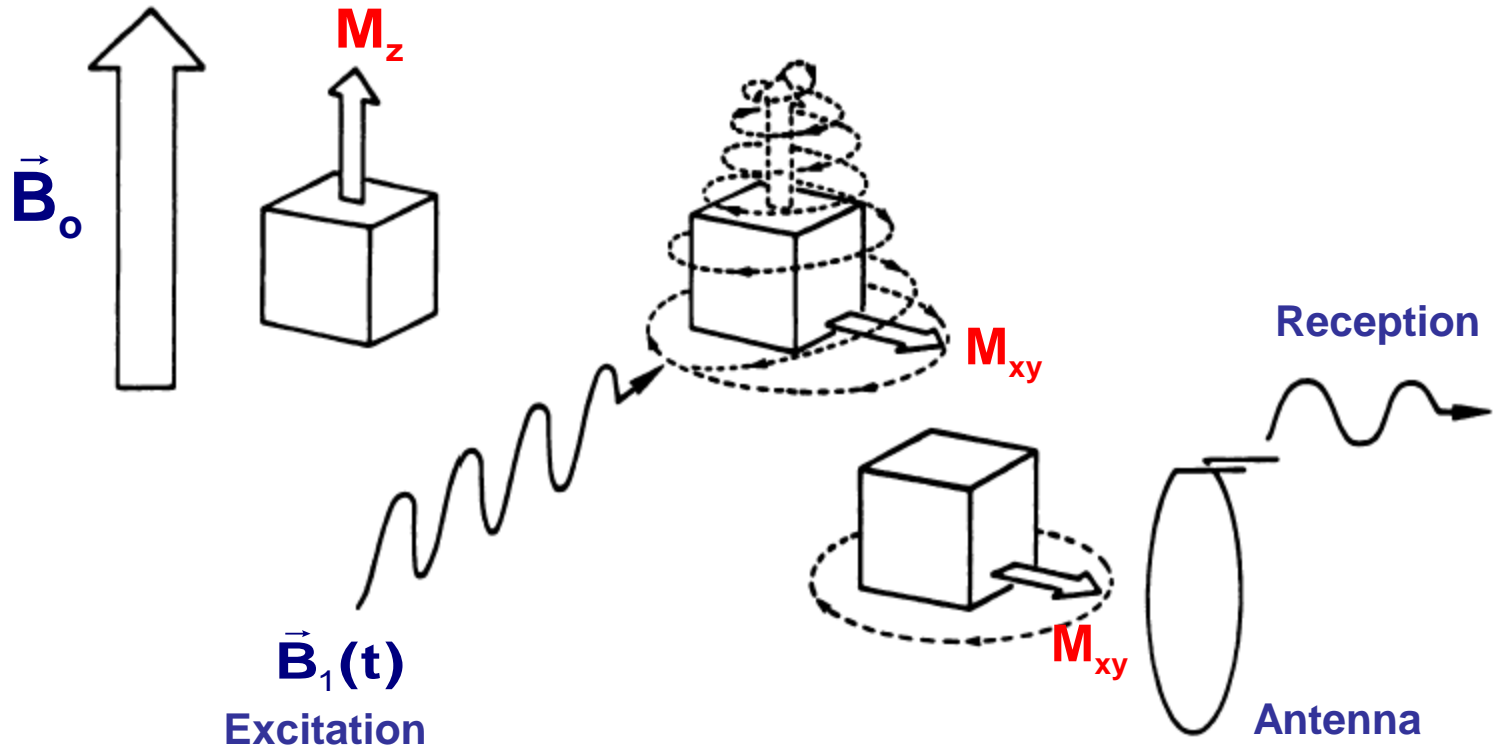
- Magnetization returns to its equilibrium position
→ energy relaxation



The amplitude of M_{xy} decreases as a function of time

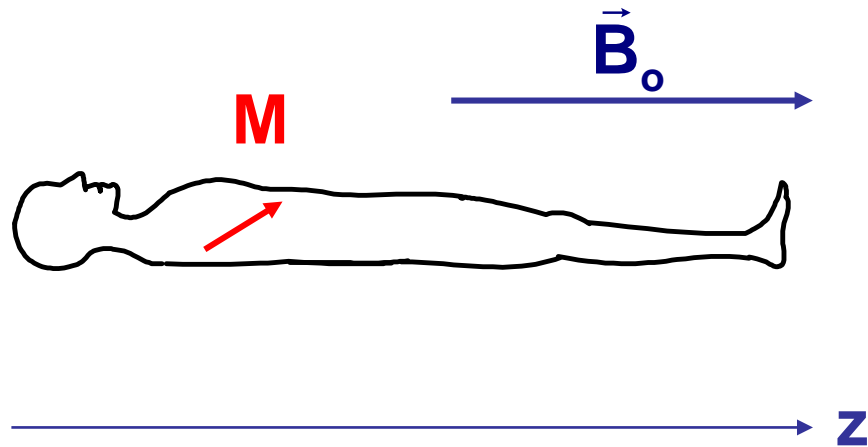
The amplitude of M_z increases as a function of time

Summary

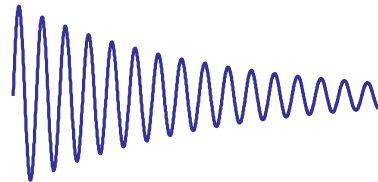


Basic contrast in MRI

- The speed of M_z growth along B_0 depends on tissue
- It is characterized by the longitudinal relaxation (T_1)
- Energy is transferred to the surrounding (spin-lattice)

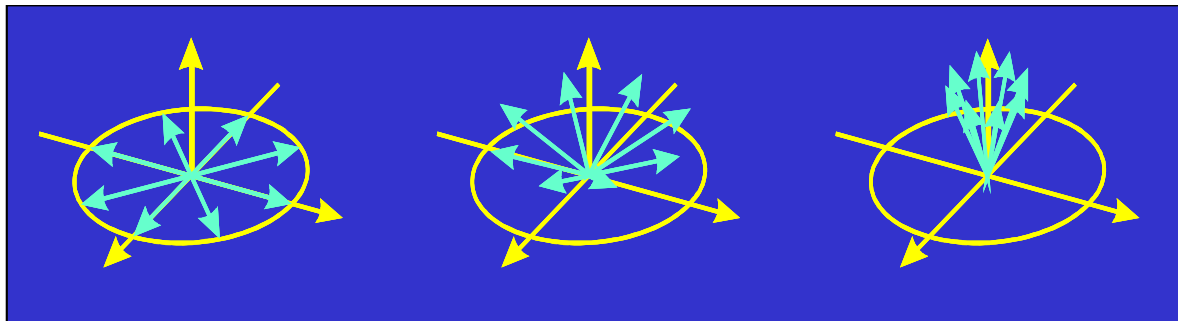
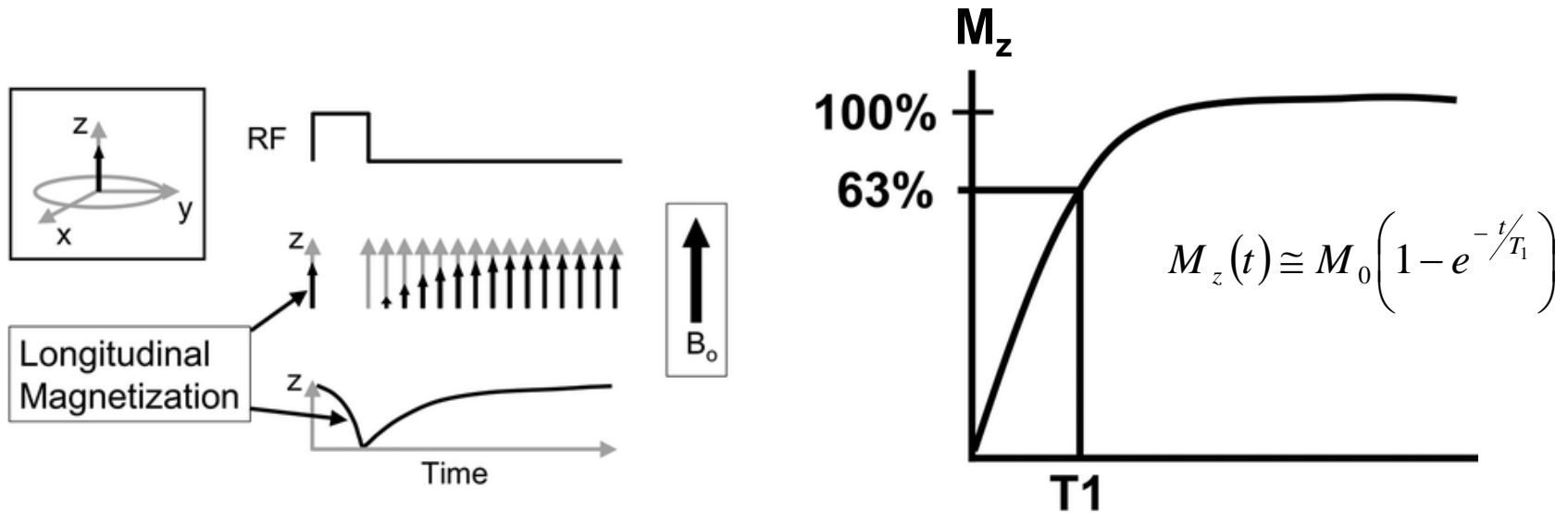


Recorded signal : M_{xy}
(Demodulated)

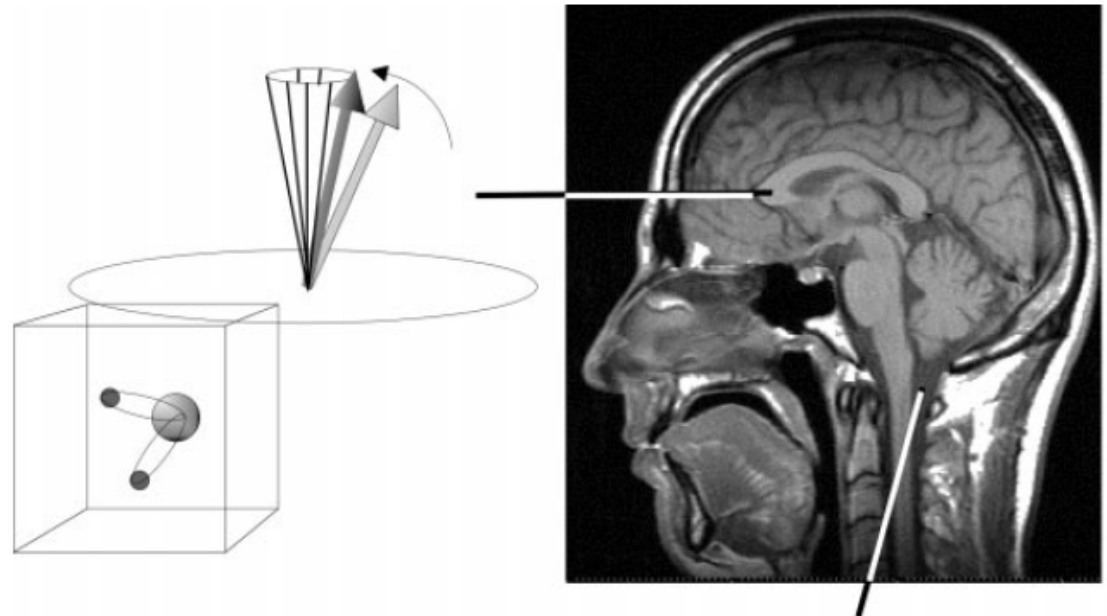


Longitudinal relaxation (T1)

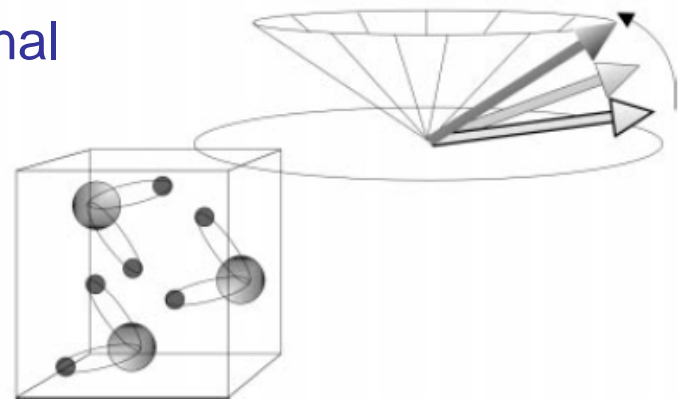
- Growth of M_z : magnetization that will be available to be tilted at the next excitation step → Origin of the MRI signal



Longitudinal relaxation and T1 contrast

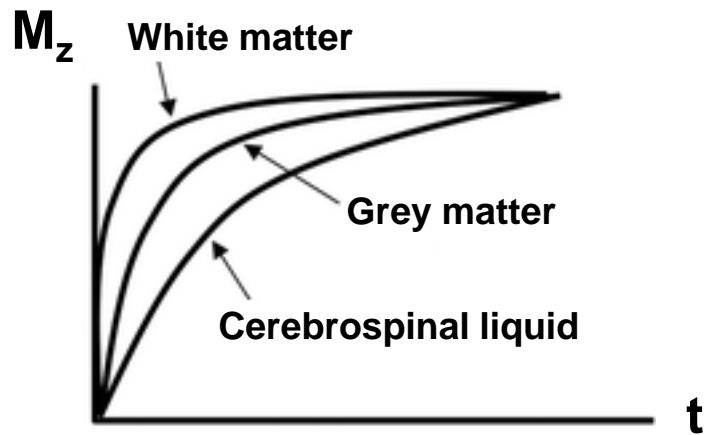
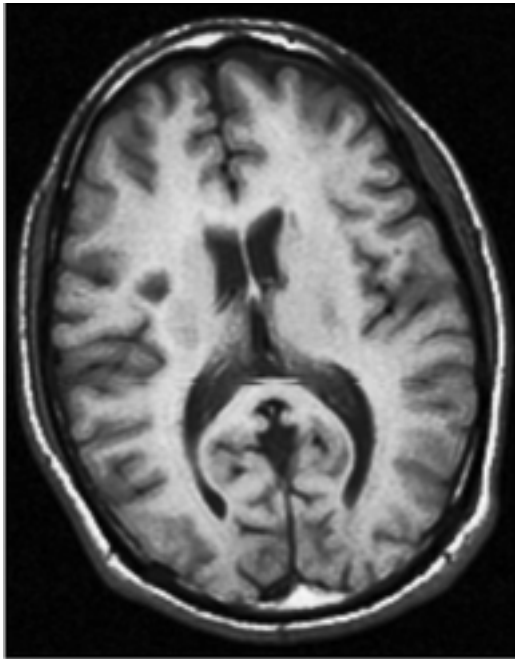


- Growth of M_z :
- Solids and liquids : very slow \rightarrow small signal
- Soft tissue : middle \rightarrow middle signal
- fat: fast \rightarrow large signal
 - Magnetization transfer on C



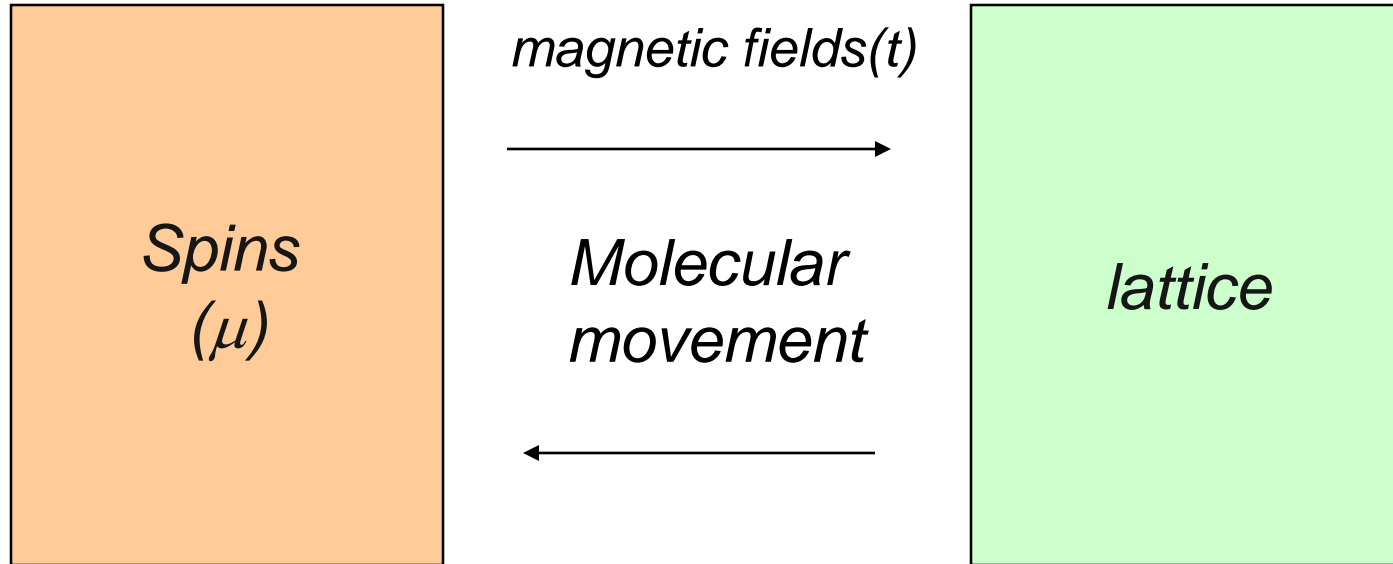
Longitudinal relaxation and T1 contrast

- T1 is tissue characteristic
- Imaging using T1 weighting



Longitudinal relaxation (T1) : magnetization growth along z (longitudinal axis)

Longitudinal relaxation and T1 contrast



Movements of μ induces magnetic field variations \rightarrow stimulated relaxation

Longitudinal relaxation and T1 contrast

- *Dipolar relaxation (other spins) $T1_d$*

- *Dipolar paramagnetic relaxation (Gd) $T1_p$*

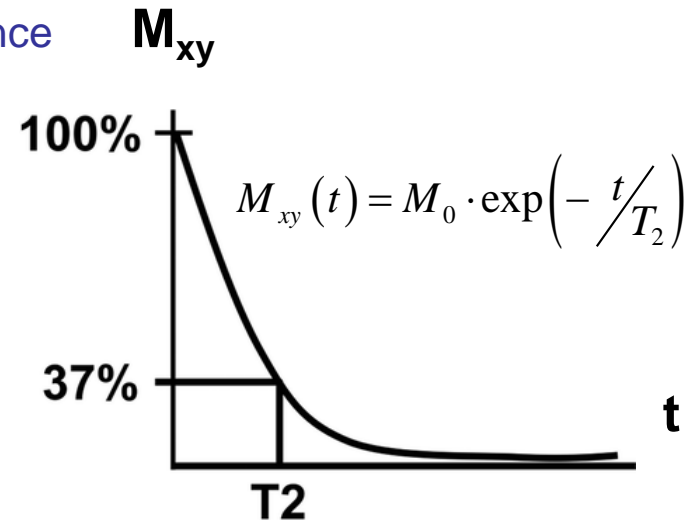
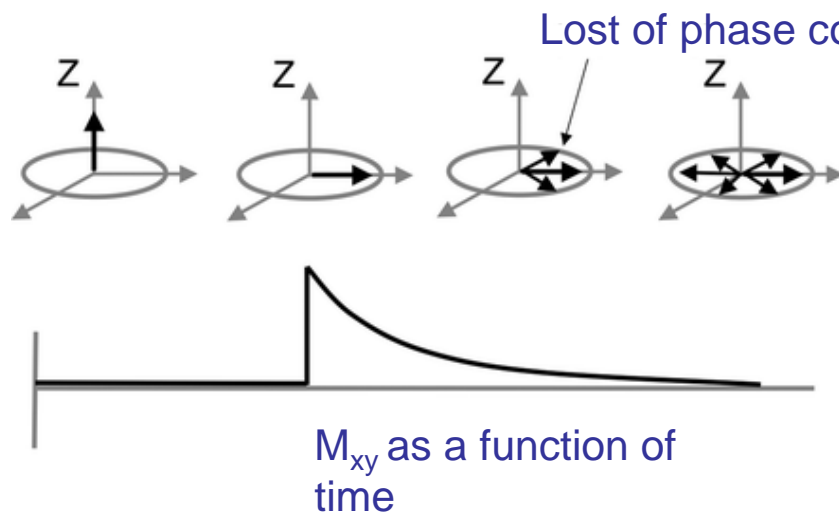
- *Quadripolar relaxation $T1$ (spin $> \frac{1}{2}$)*

- ...

$$\frac{1}{T_1} = \sum \frac{1}{T_i}$$

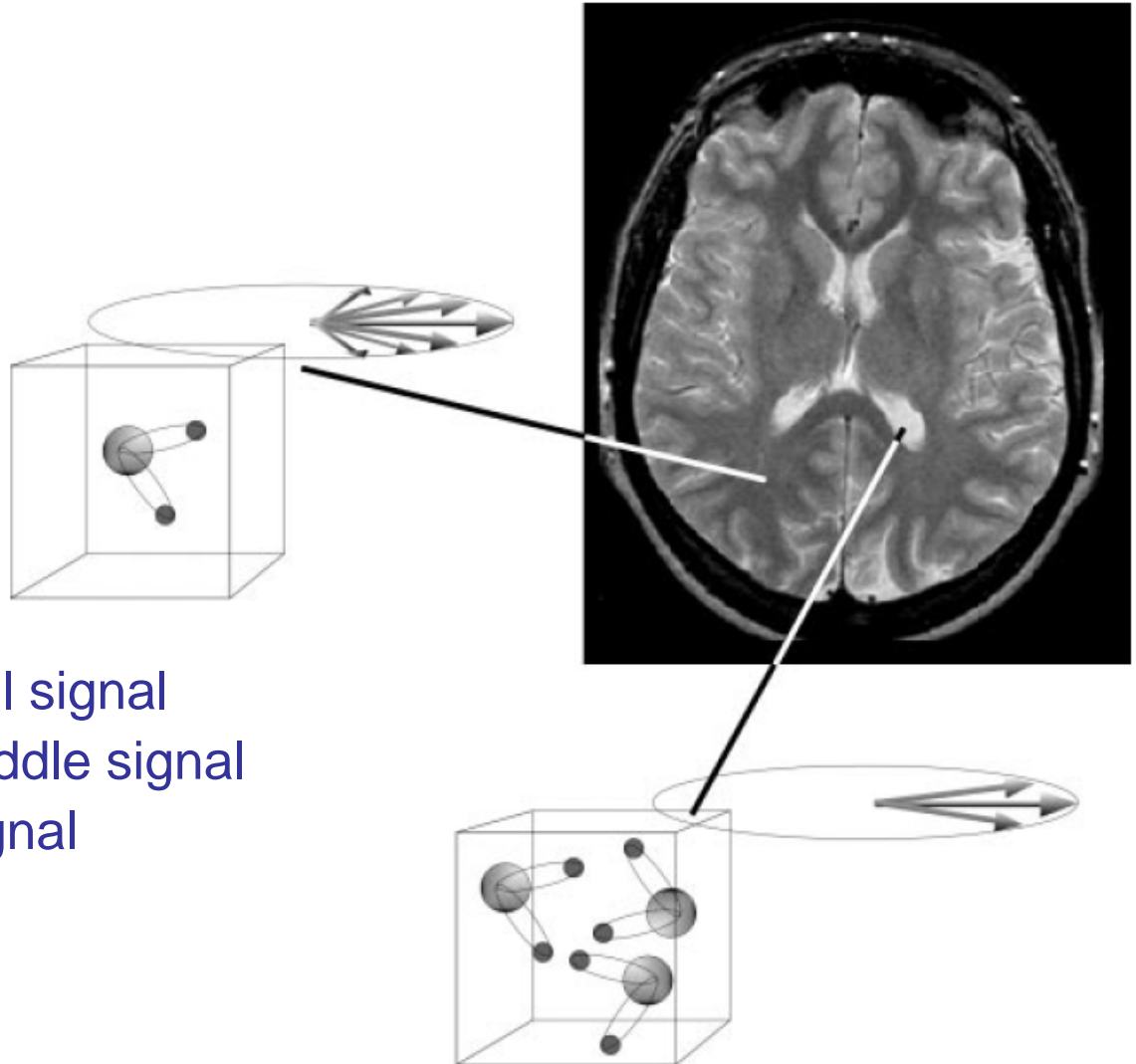
Transverse « relaxation » (T2)

- Simultaneous with T1 but faster
- Lost of phase coherence between the individual spin
 - Decrease of M_{xy} (signal) (in addition of T1 effect)
 - No energy exchange with the lattice (spin-spin)
- Depends on the magnetic homogeneity of the tissue



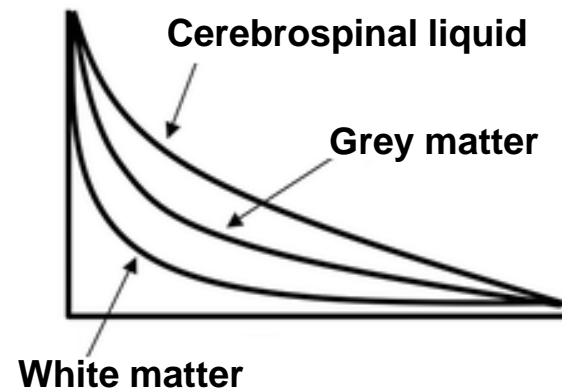
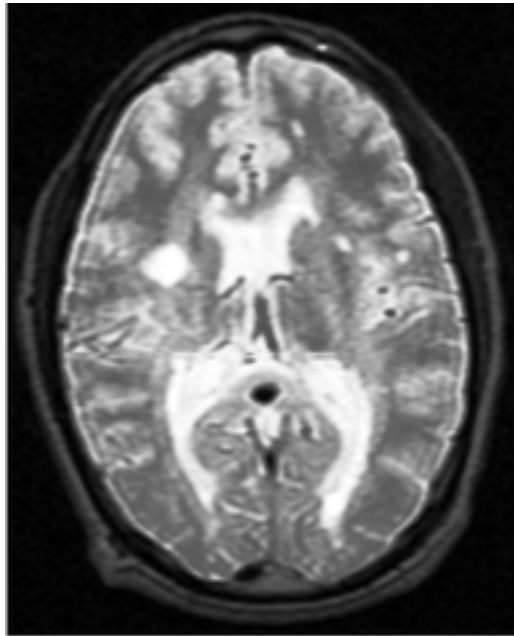
Transverse « relaxation » (T2)

- Reduction of M_{xy} :
- Solids : very fast \rightarrow small signal
- Soft tissue: middle \rightarrow middle signal
- Liquids: slow \rightarrow large signal



Transverse « relaxation » (T2)

- T2 is also a tissue characteristic
- Imaging using T2 weighting



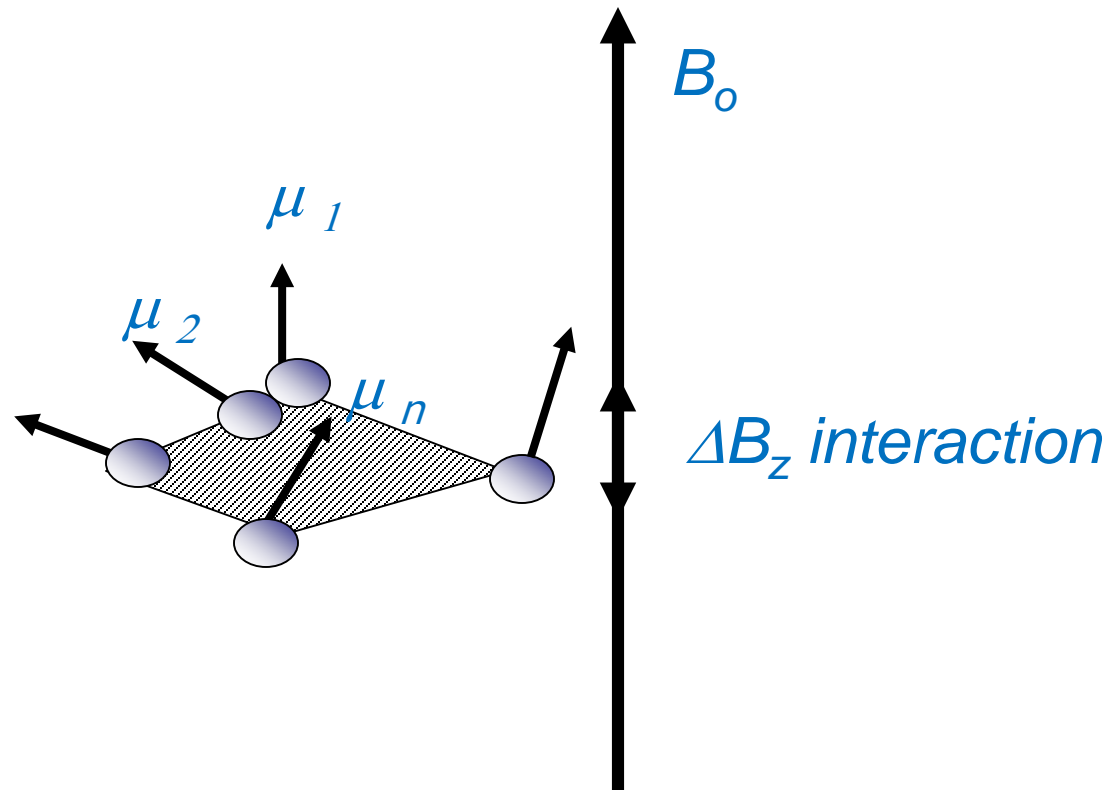
Order of magnitude

- **Indicative values (T1 in general \gg T2)**

Tissue	T1 @1,5 T (msec)	T2 (msec)
Fat	260	80
Liver	500	40
Muscle	870	45
White matter	780	90
Grey matter	900	100
Cerebrospinal liq.	2'400	160

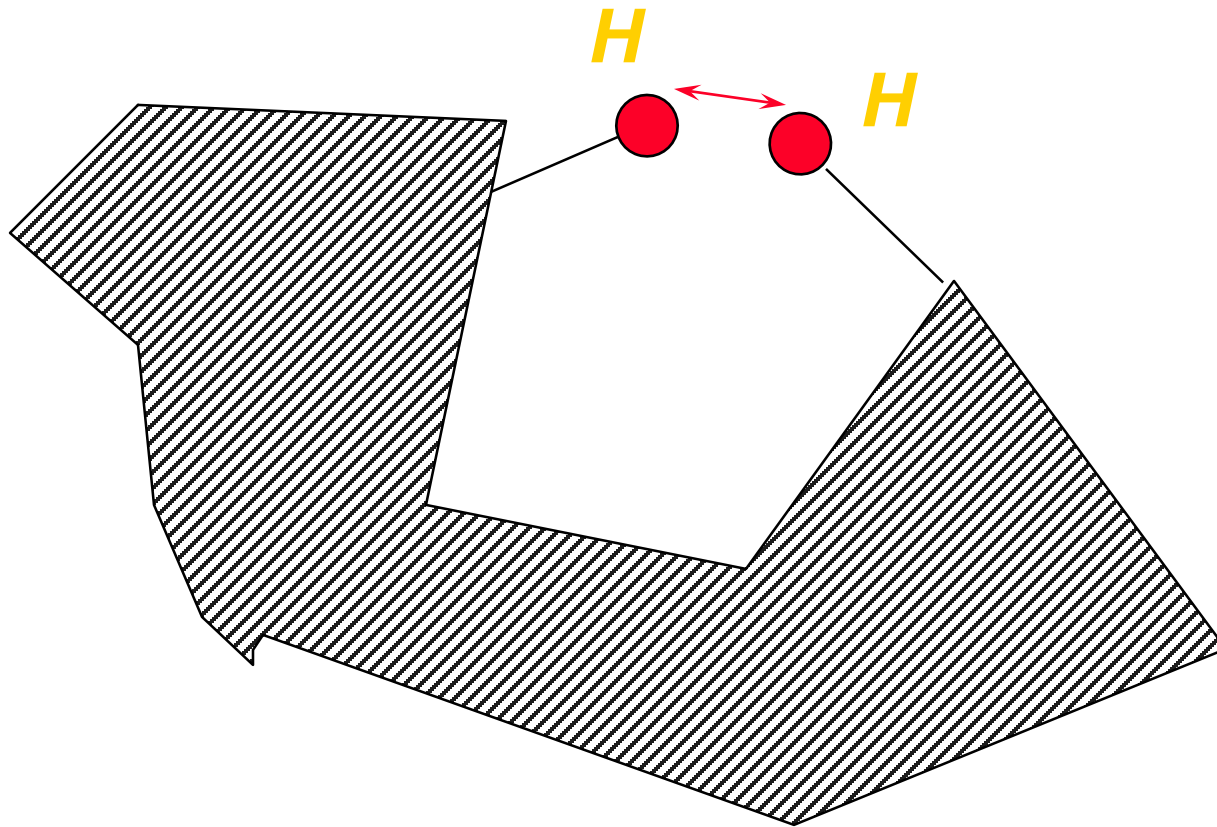
Transverse « relaxation » (T2)

*Simultaneous with T1, but faster → lost of magnetization coherence
Mutual effects of μ*



Transverse « relaxation » (T2)

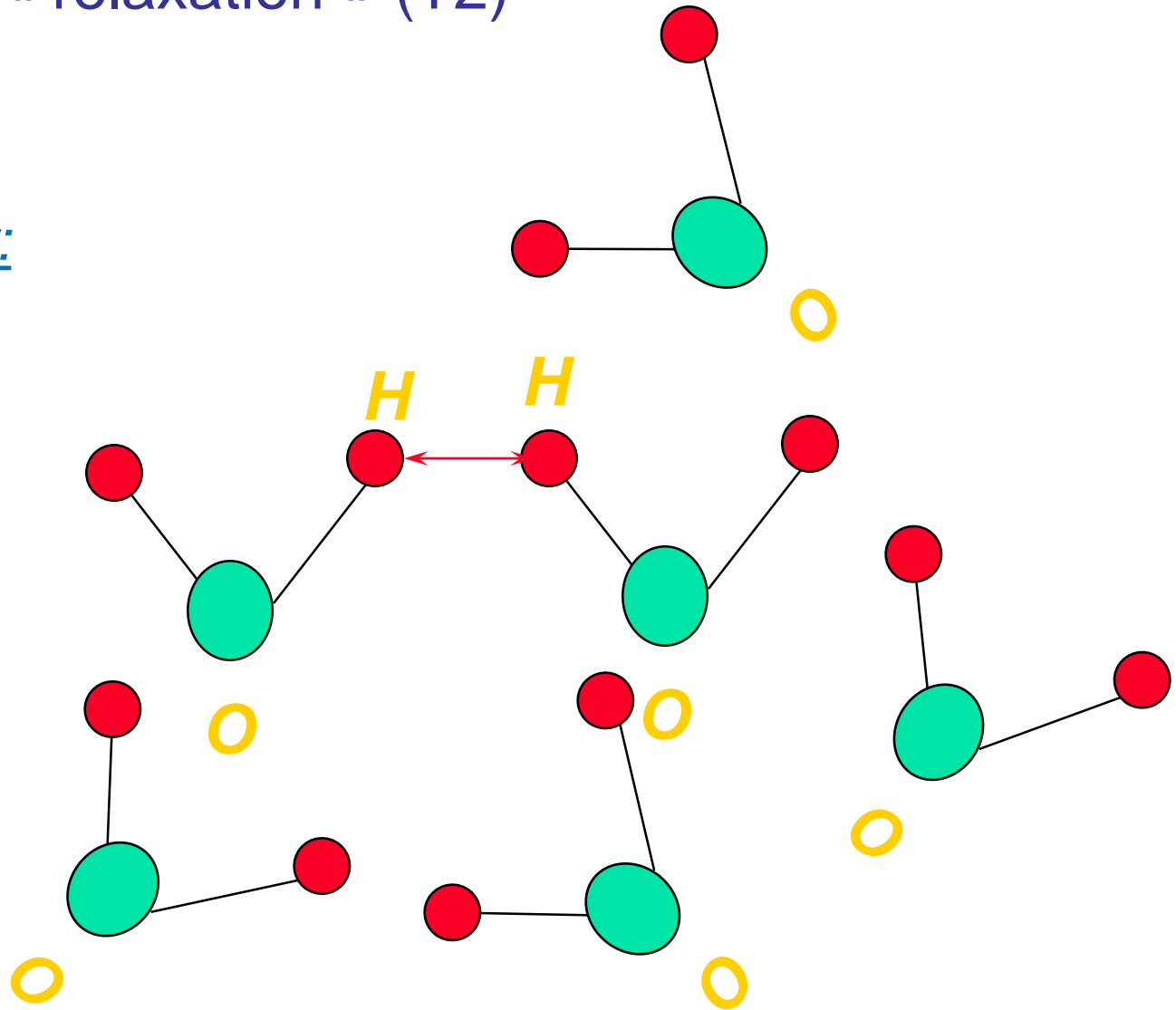
Large molecules (protein)



Slow movements → Short T2

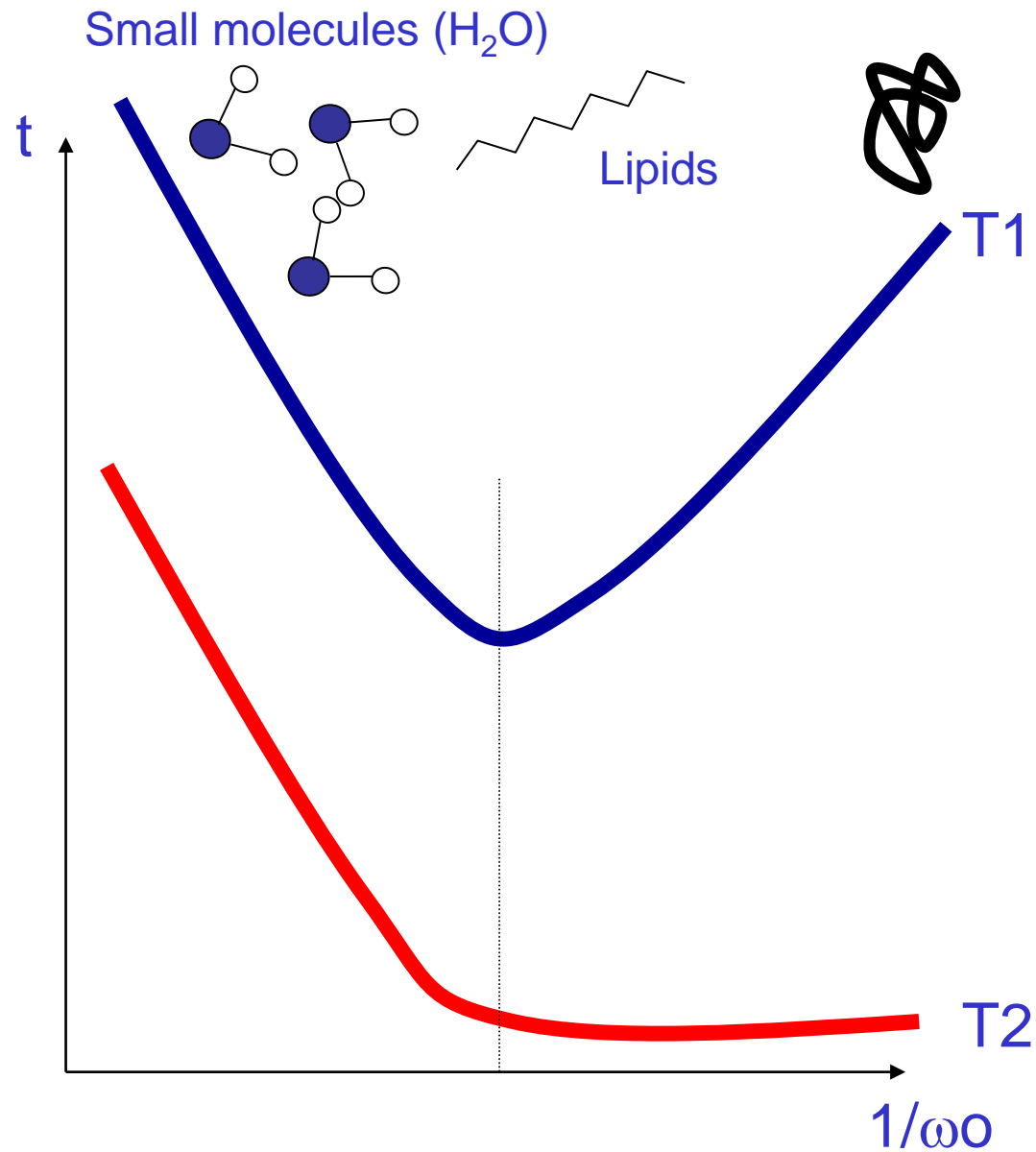
Transverse « relaxation » (T2)

water:



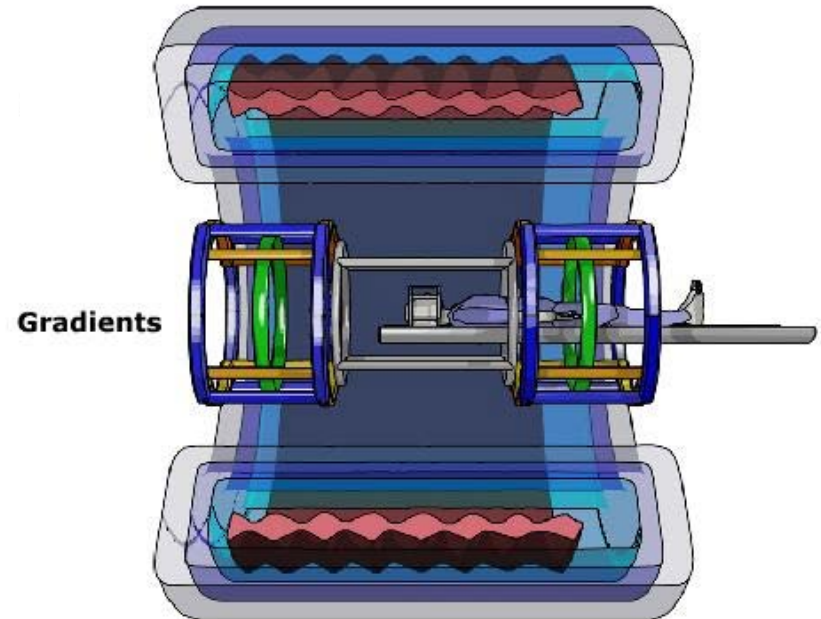
fast movements → averaging of field variations → long T2

T1 and T2 as a function of molecular dynamic

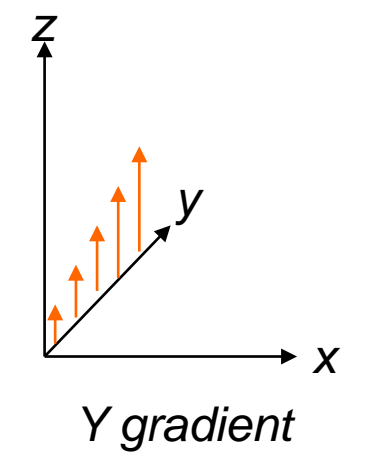
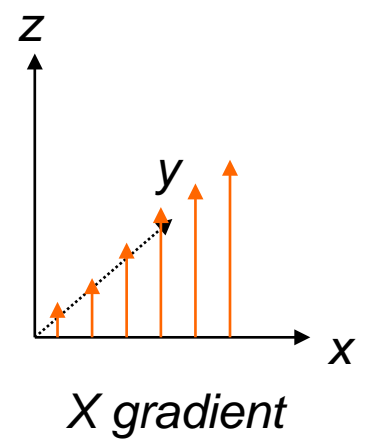
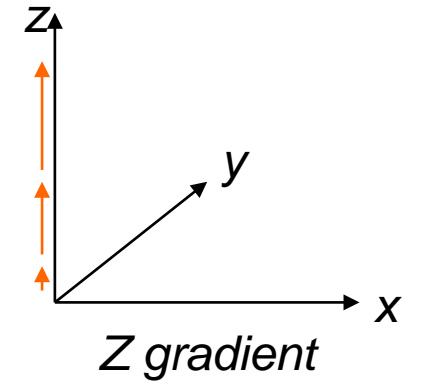
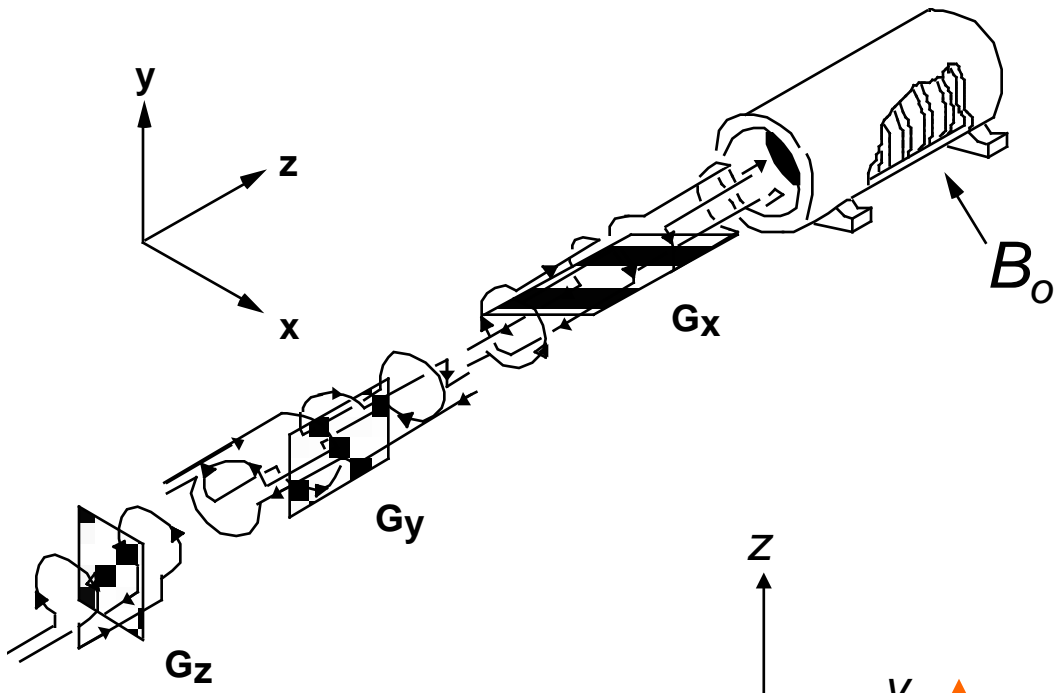


Schematic of an MRI system

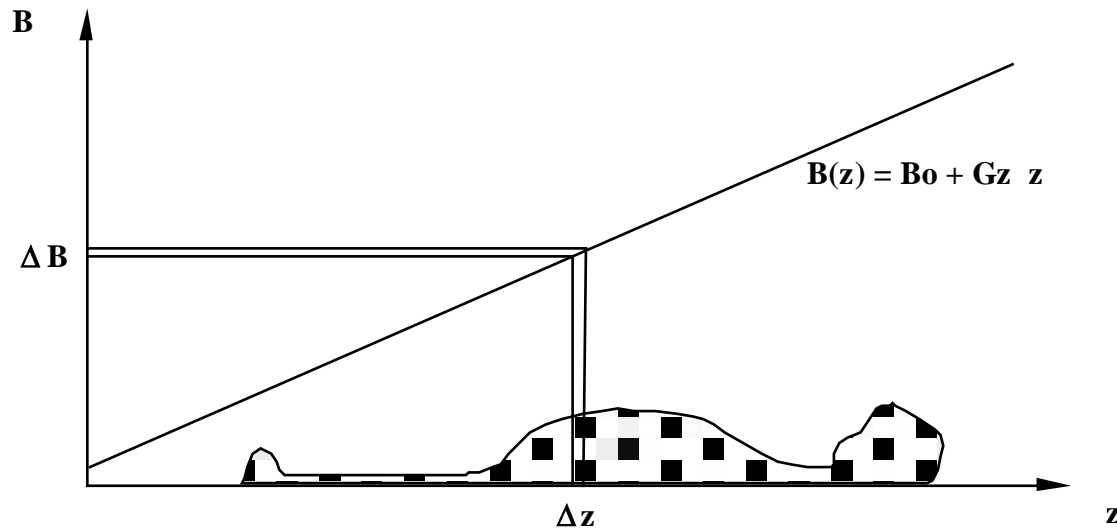
- A large magnet (static magnetic field B_0 (0.5 to 3 T in clinic)
- Three gradient coils (magnetic field B_0 that varies with position x,y,z) (a few mT/m)
- Excitation and reception antenna (magnetic field that varies with time)



From NMR to MRI



Slice selection



G_z a few $mT.m^{-1}$

Express the slice thickness D_z as a function of G_z

Tomographic technique → how to choose a slice?

Slice position : frequency value

Frequency domain

$$\Delta\omega = \gamma \cdot G_z \cdot \Delta z$$

Bandwidth of the rf : $\Delta\nu = \Delta\omega/2\pi$

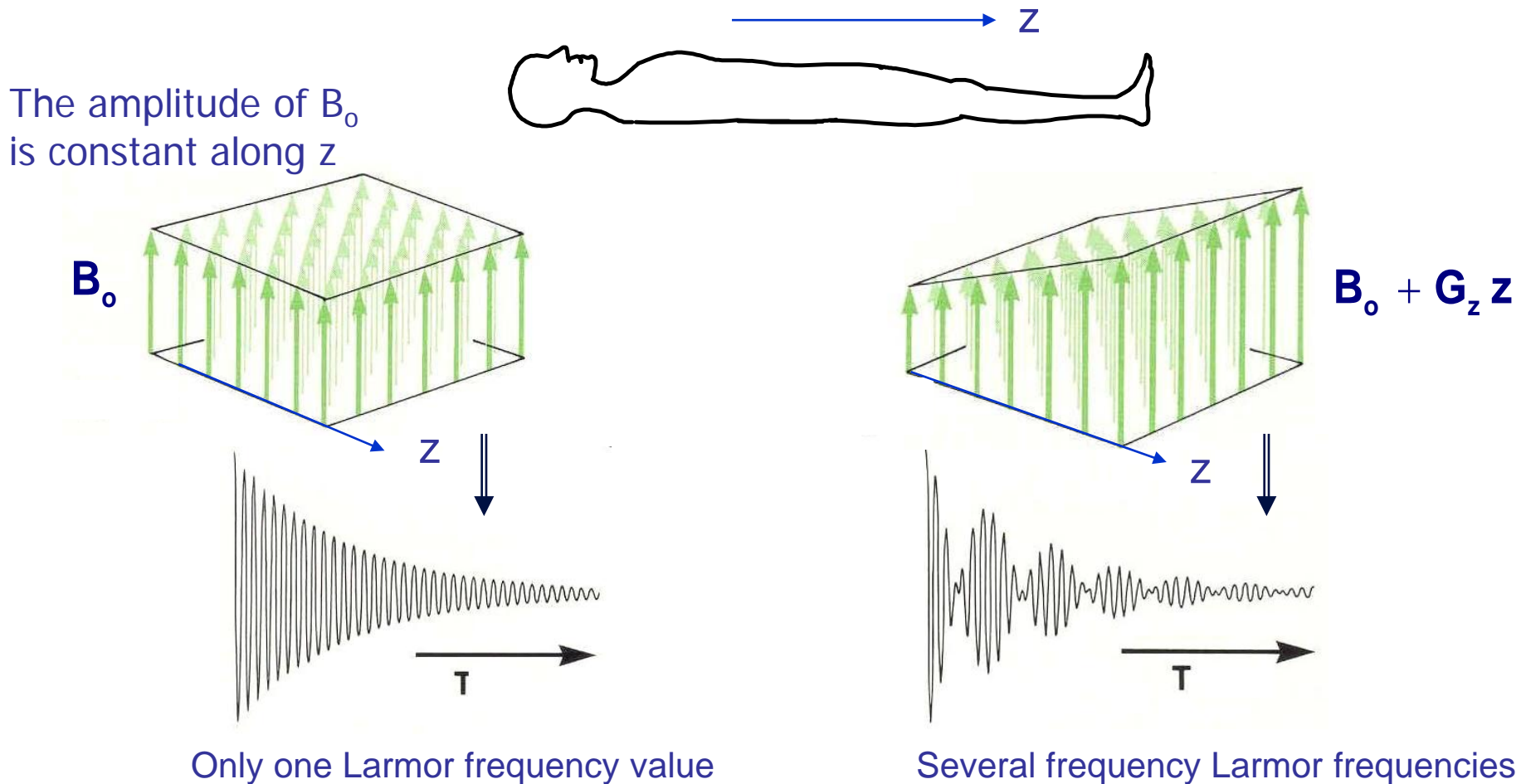


Slice thickness :

$$\Delta z = 2\pi \Delta\nu / (\gamma \cdot G_z)$$

Tomographic technique → how to choose a slice?

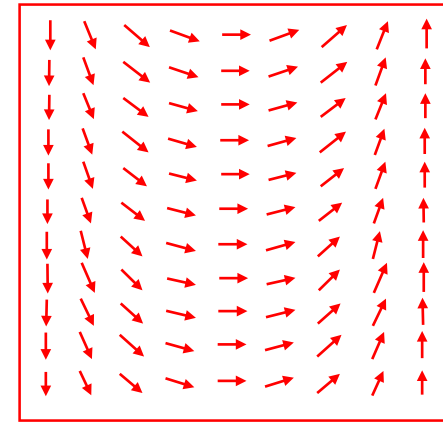
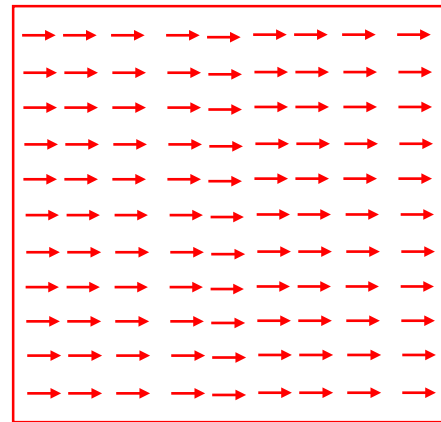
- During the excitation apply a magnetic gradient field \perp to the slice plane
- Selective rf excitation to only tilt spin within the selected slice



Encoding of the information

Phase space (k-space)

9×9 pixels

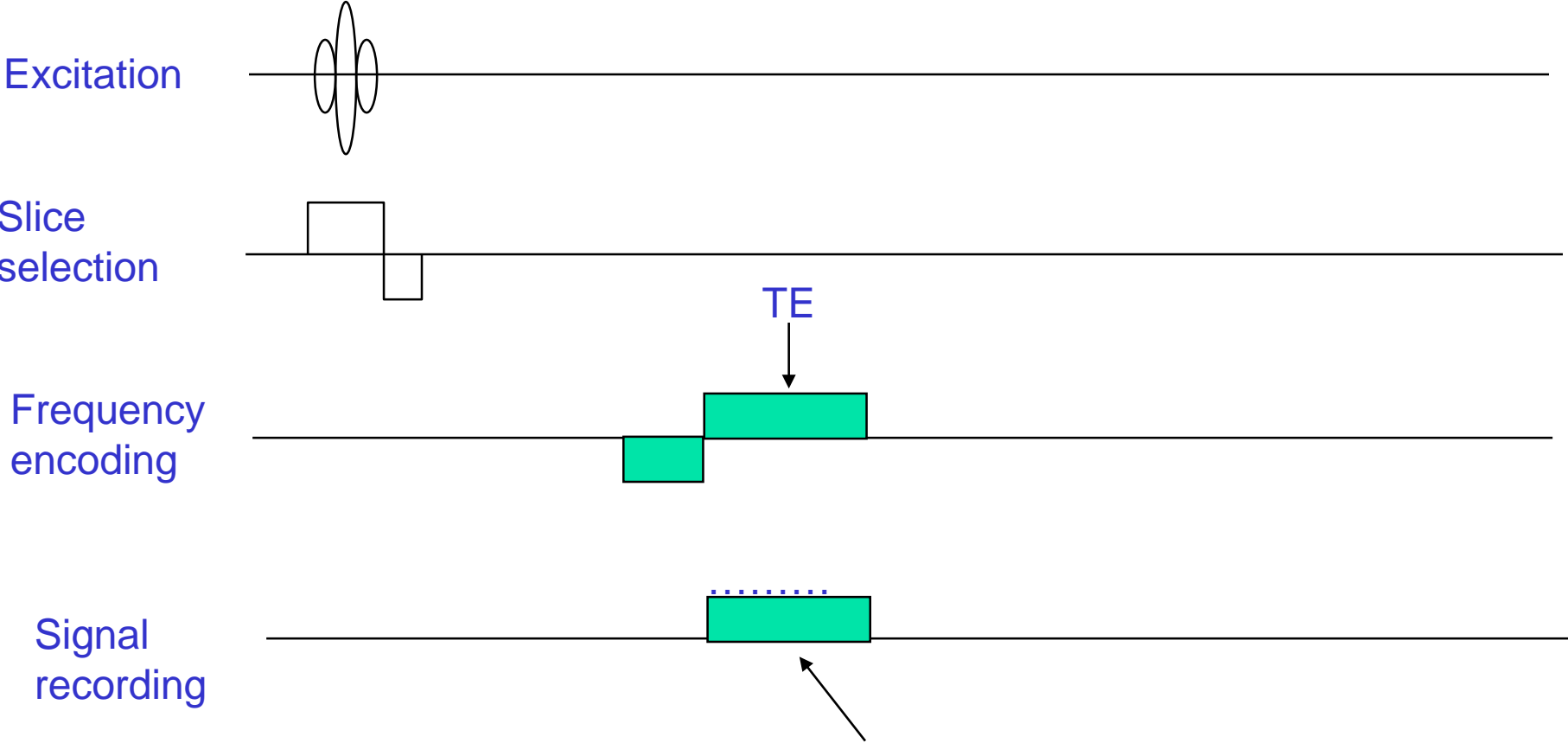


Before encoding

After encoding
(use of two other gradients
than slice selection)

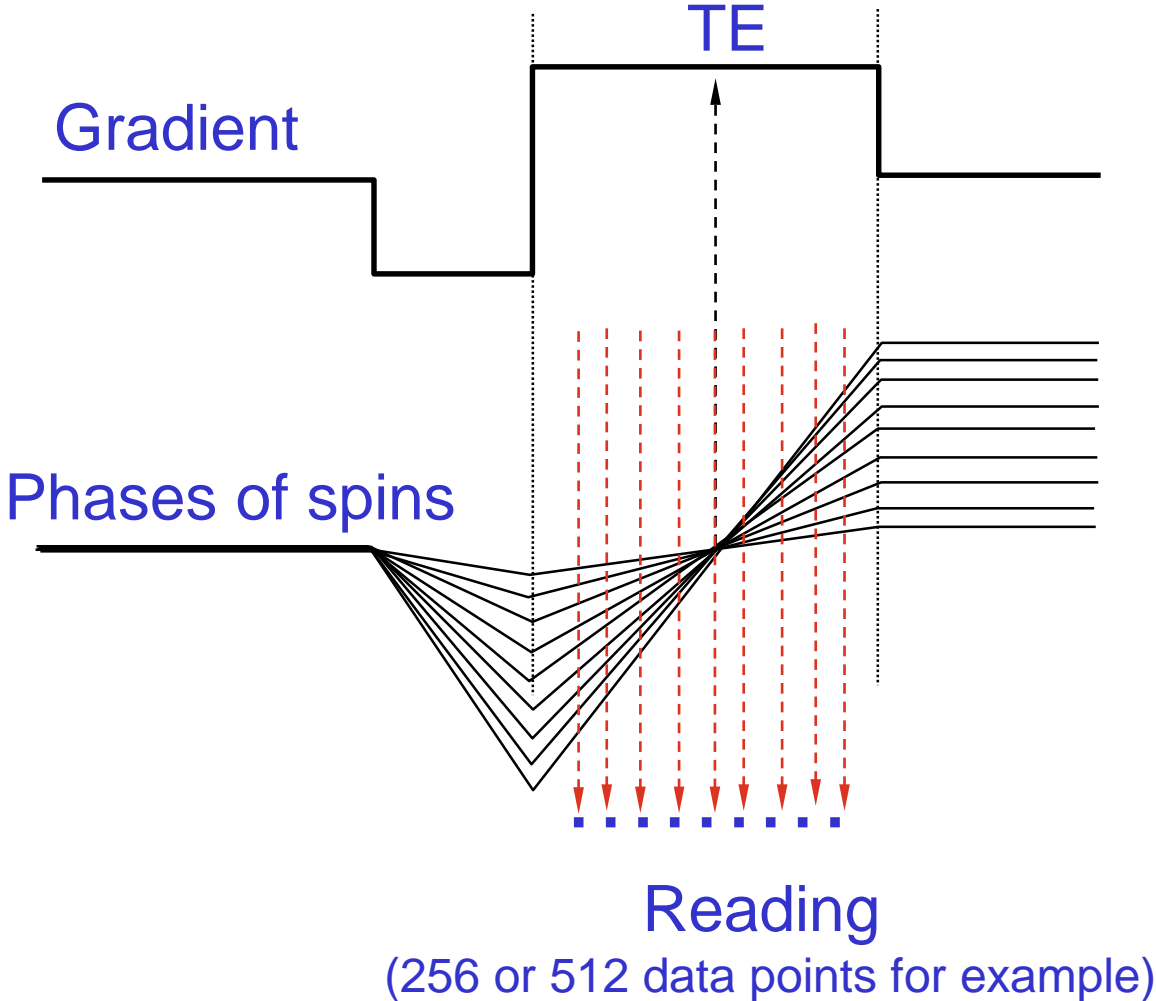
Goal to code each pixel position in terms of frequency and phase of the spin

Frequency encoding : during data acquisition



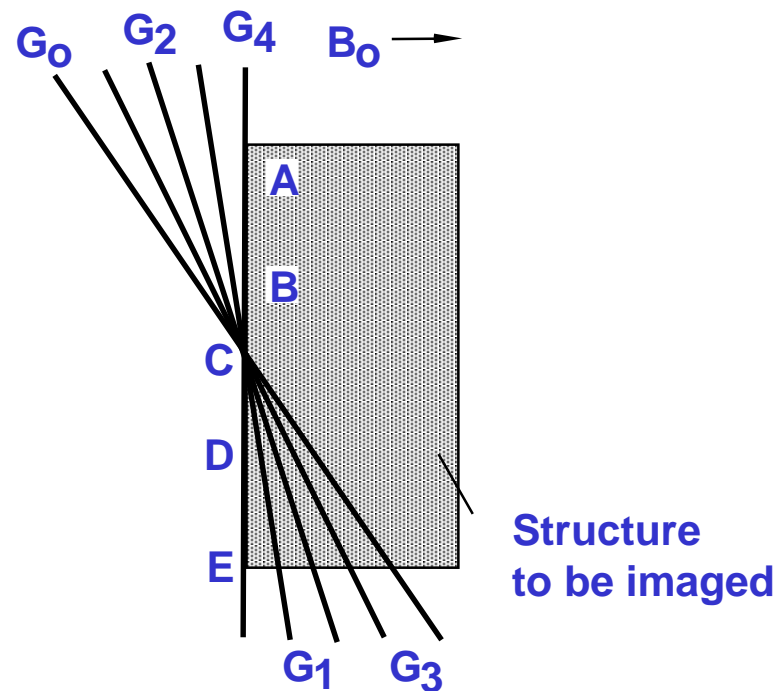
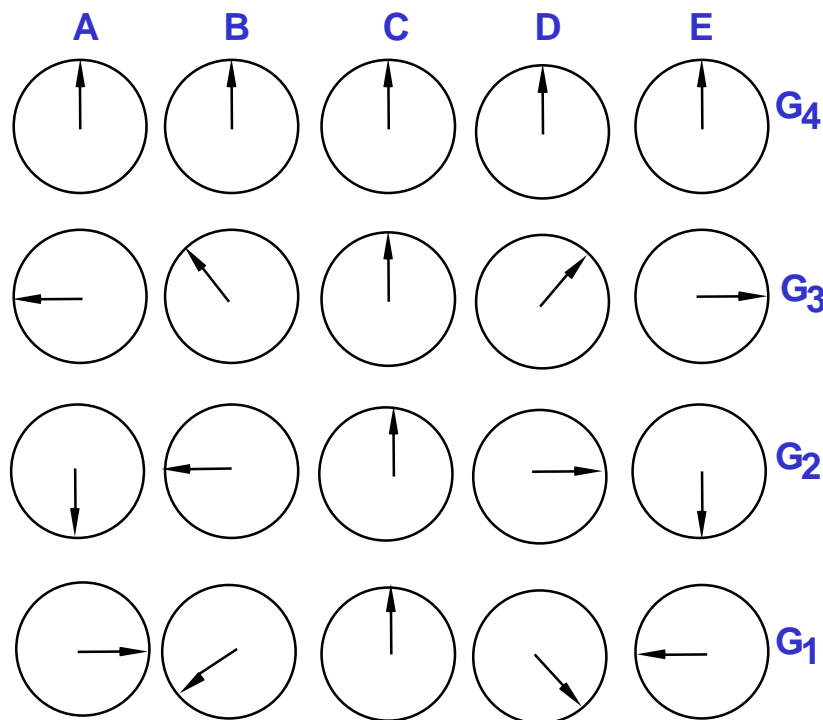
Sampling of the data : 1 line of the raw data

Frequency encoding : during data acquisition

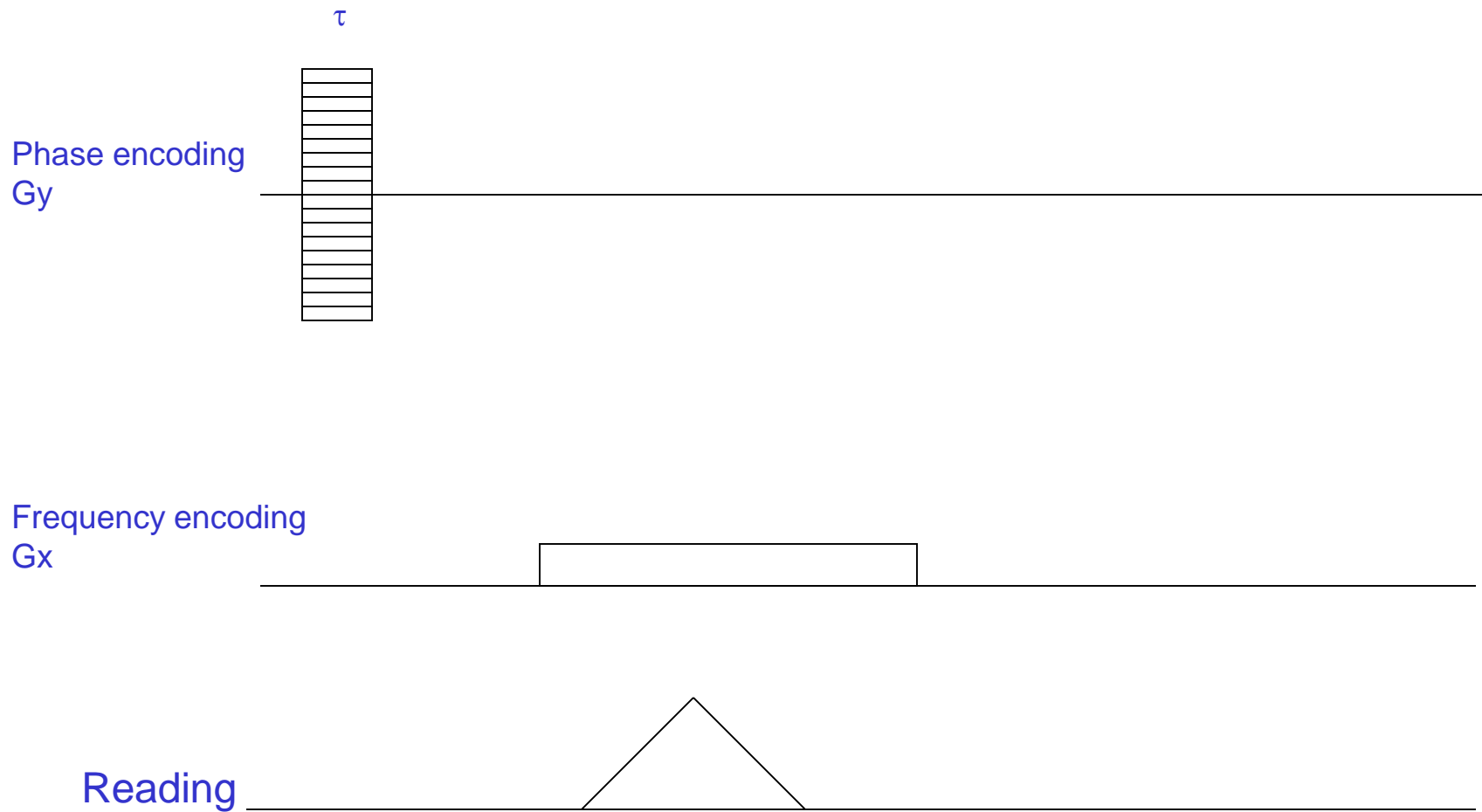


Phase encoding : before data acquisition

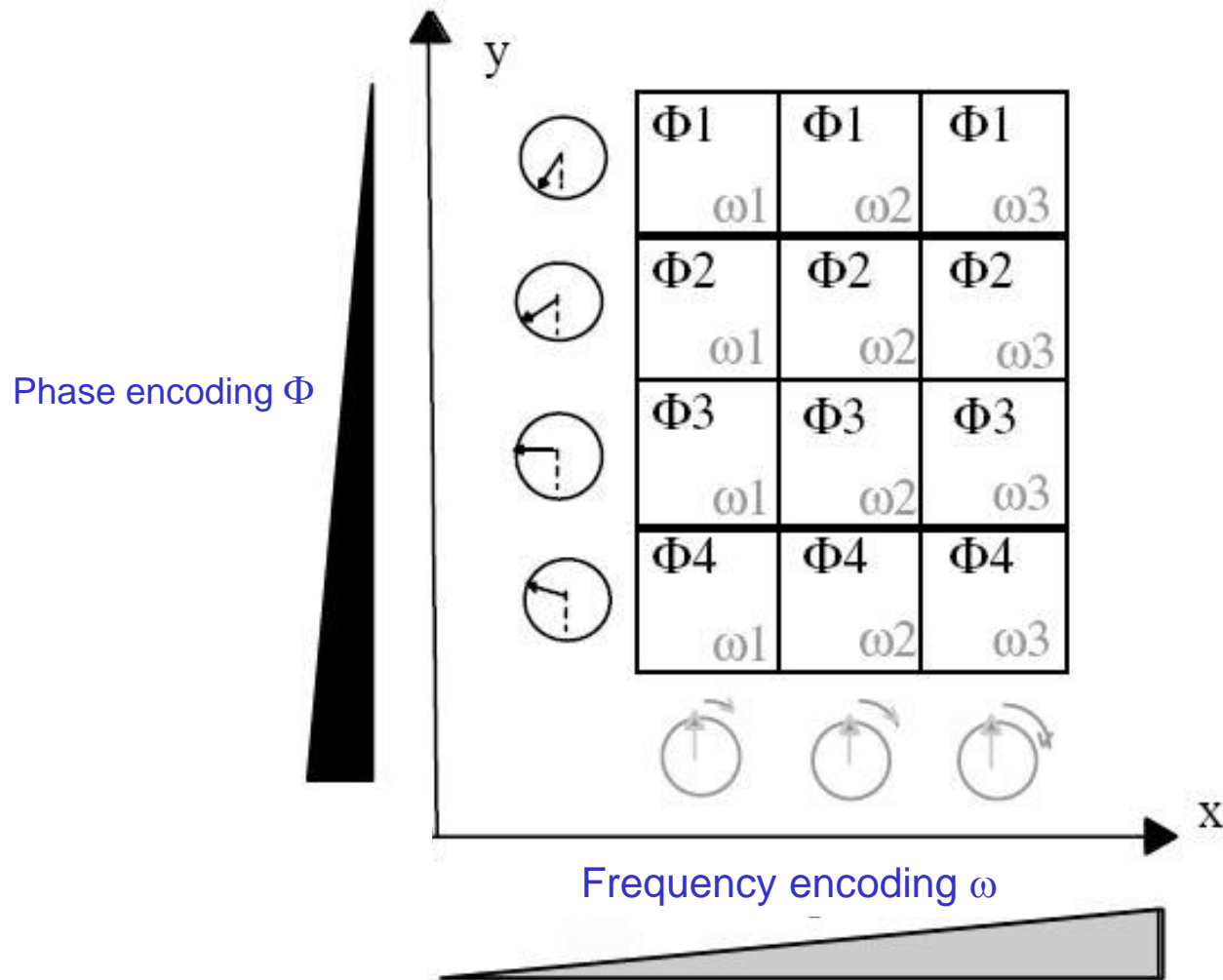
Each spin is tagged with a phase as a function of its position



Part of the sequence to encode the image



Result of image encoding



Mathematics of the spin-warp

$$S(t, G_y) = \iint M(x, y) e^{2\pi i \gamma G_x x t} \cdot e^{2\pi i \gamma G_y y \tau} dx dy$$

t and G_y produce phase differences: only one type of variable

$$k_x = \gamma G_x t \rightarrow t = n \Delta t = \frac{n \Delta k_x}{\gamma G_x}$$

$$k_y = \gamma G_y \tau \rightarrow G_y = \frac{m \Delta k_y}{\gamma \tau}$$

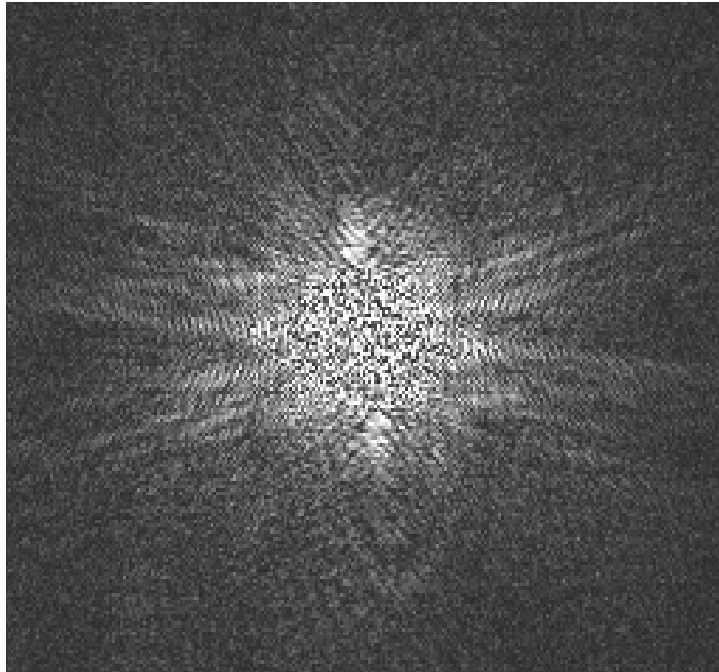
$$S(n \Delta k_x, m \Delta k_y) = \sum \sum M(x, y) e^{2\pi i (x n \Delta k_x + y m \Delta k_y)} dx dy$$

$$\Delta k_x = \frac{1}{N_x \Delta x} = \frac{1}{X} \quad \Delta k_y = \frac{1}{N_y \Delta y} = \frac{1}{Y}$$

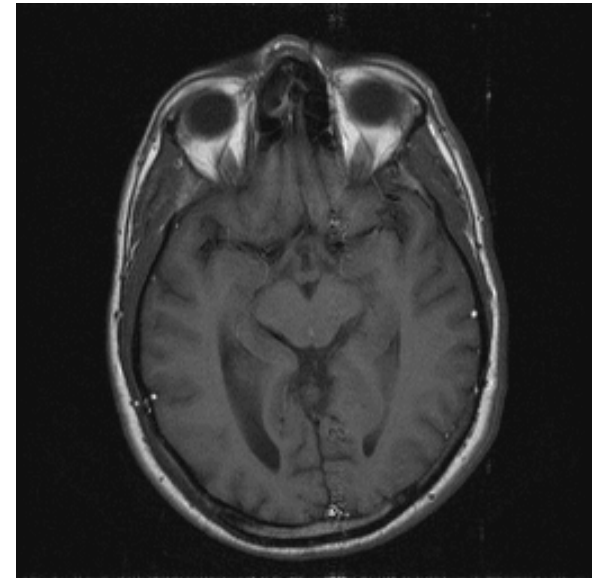
This method produce a elegant way of coding the data since it directly produces the Fourier transform of the image

$$M(x, y) = \sum \sum S(n \Delta k_x, m \Delta k_y) e^{-2\pi i (x n \Delta k_x + y m \Delta k_y)} \Delta k_x \Delta k_y$$

Summary

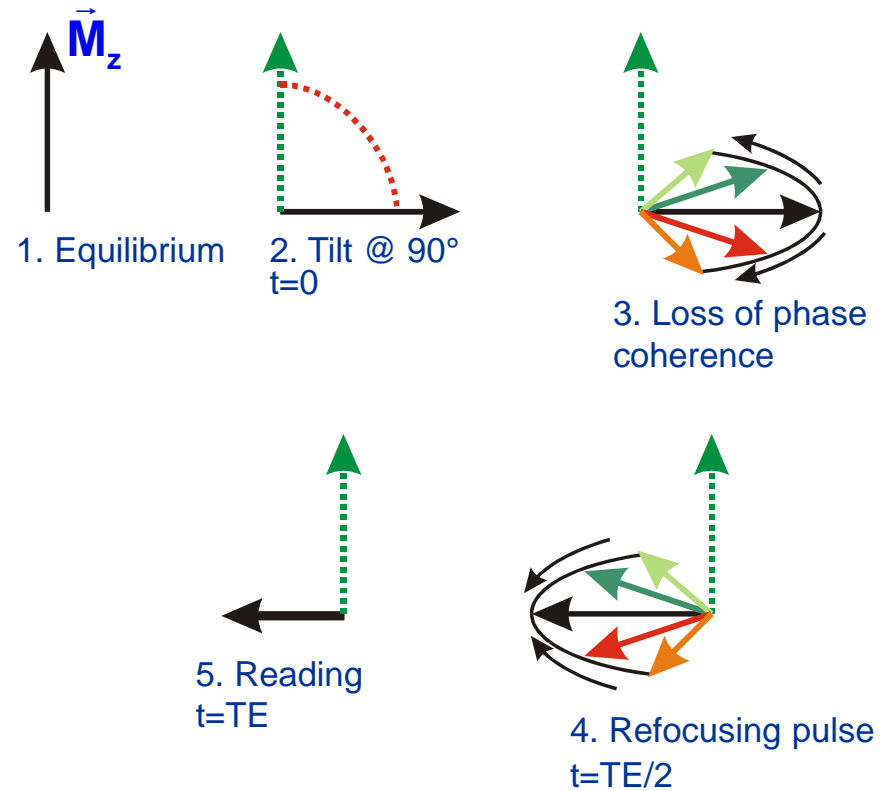
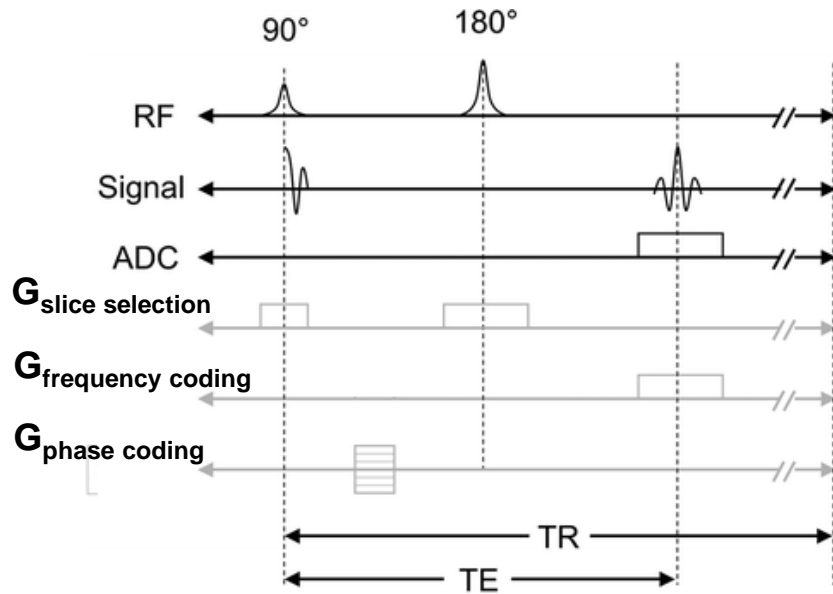


Fourier transform

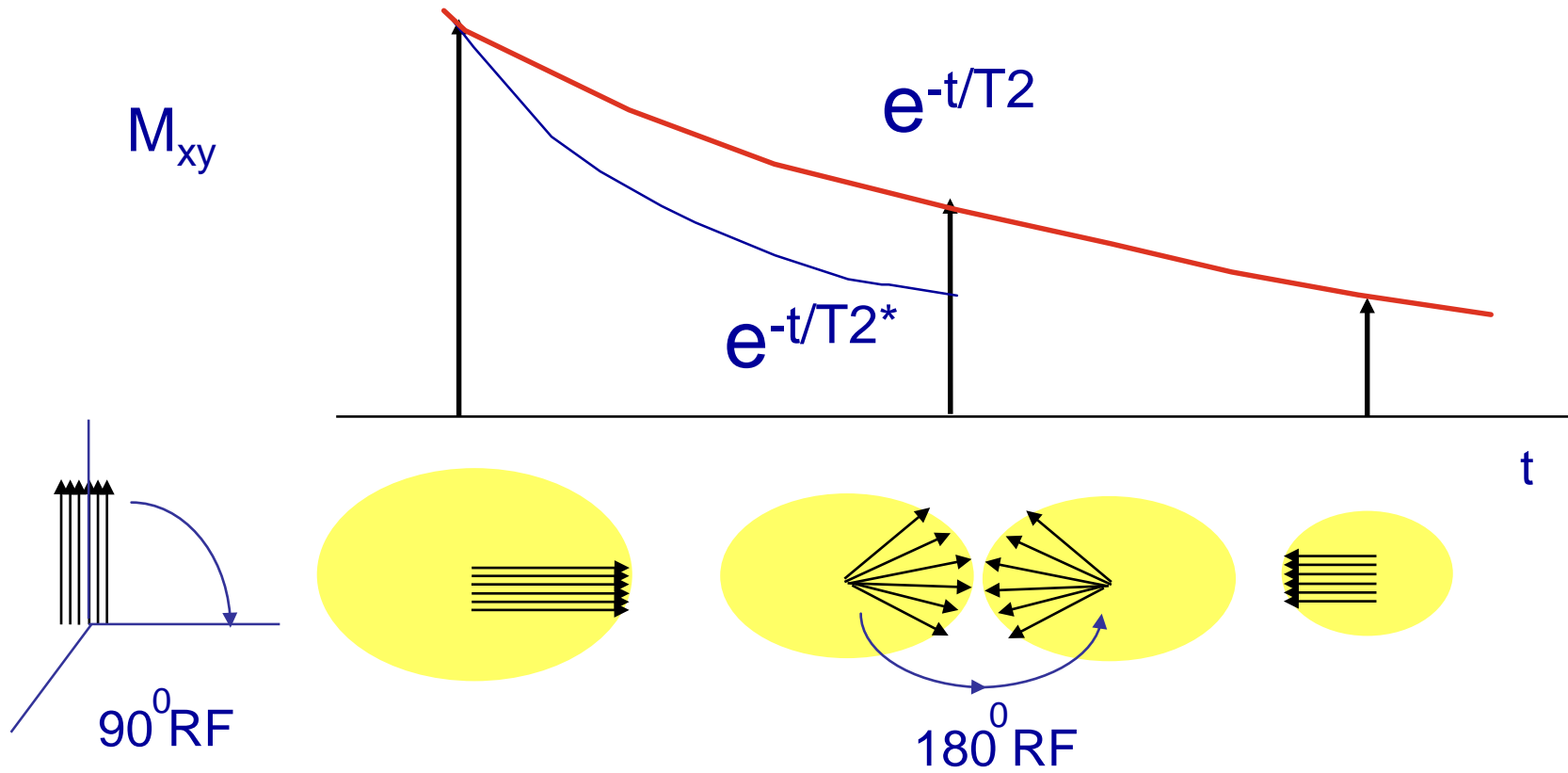


$$M(x, y) = \sum \sum S(n \Delta k_x, m \Delta k_y) e^{-2\pi i(xn \Delta k_x + ym \Delta k_y)} \Delta k_x \Delta k_y$$

Basic sequence : spin echo



Basic sequence : spin echo

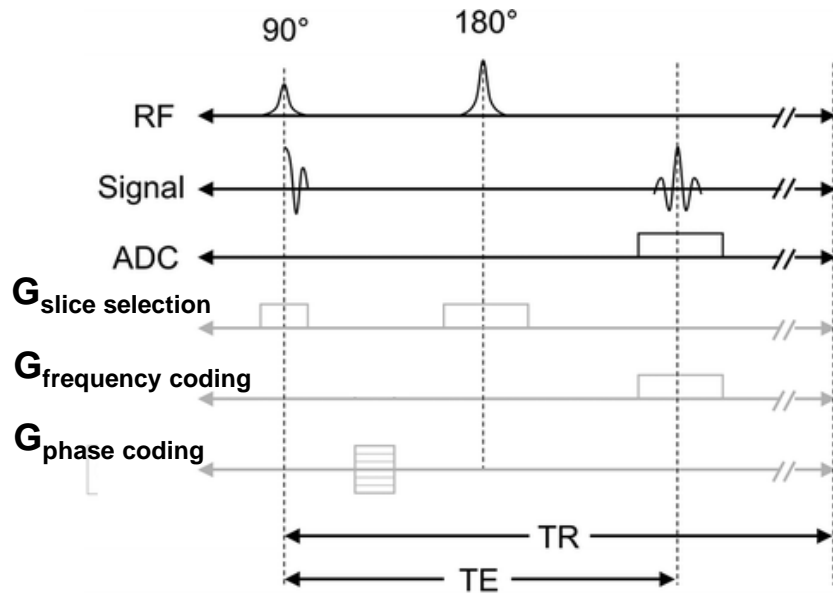


MRI sequence

- Sequence of rf and magnetic gradient as a function of time to build the image aiming to enhance a particular contrast:
 - T1 contrast (image of the anatomy)
 - T2 contrast (“ + « pathology »)
 - What would be the effect of an oedema in T2 ?

MRI sequence

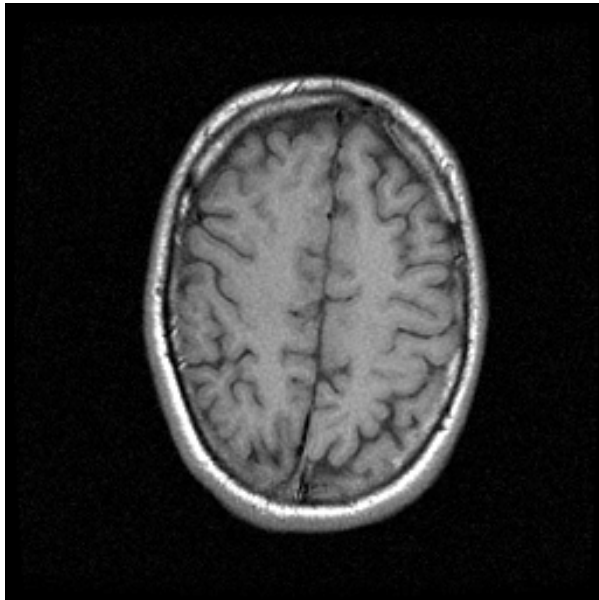
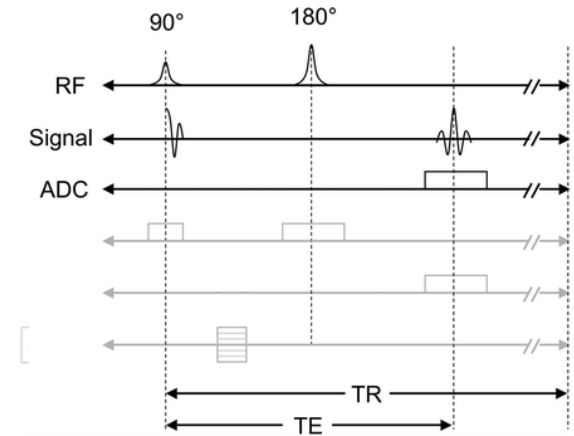
Control over the image contrast



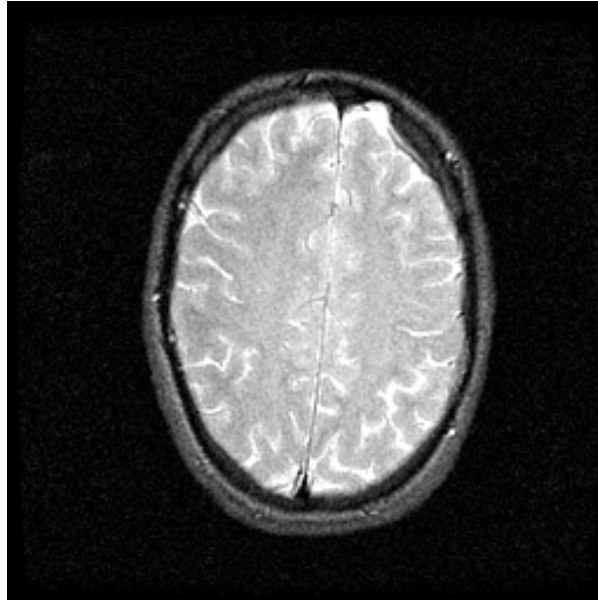
		TR	
		Short	Long
TE	Short	T1	Protons density
	Long	T1, T2	T2

$$S(TR, TE) \propto \rho(1 - e^{-TR/T_1})e^{-TE/T_2}$$

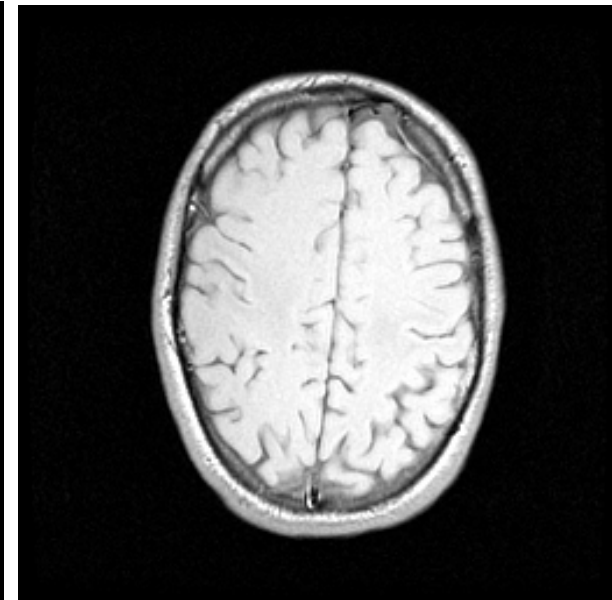
Contrast variation



T1 Contrast
 $T_E = 14 \text{ ms}$
 $T_R = 400 \text{ ms}$

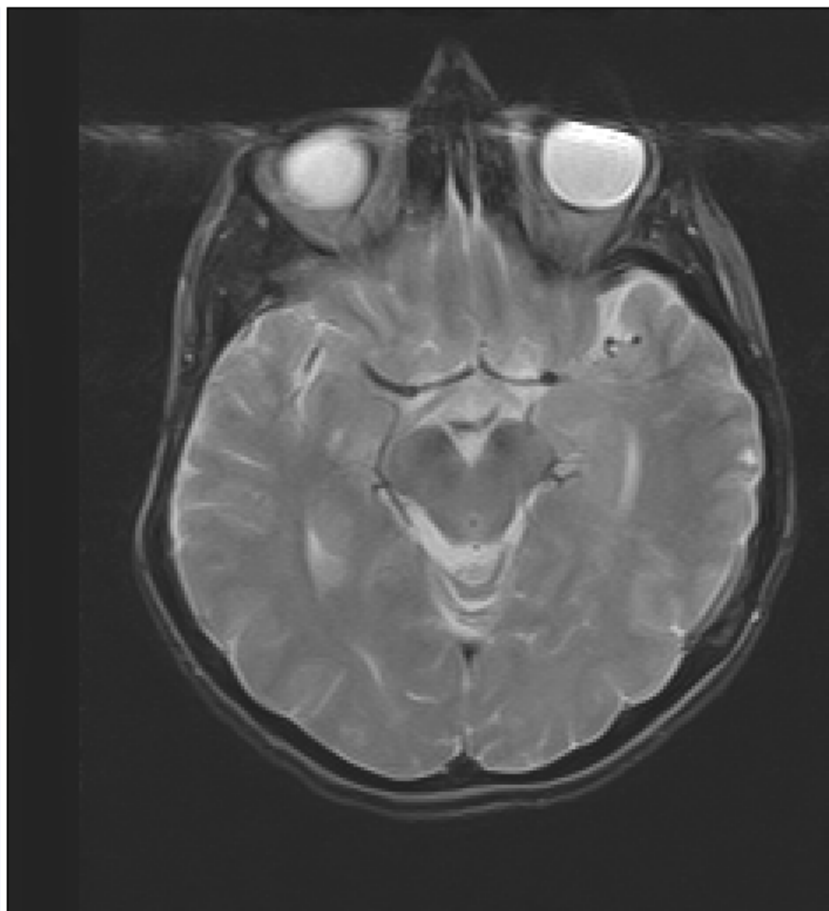
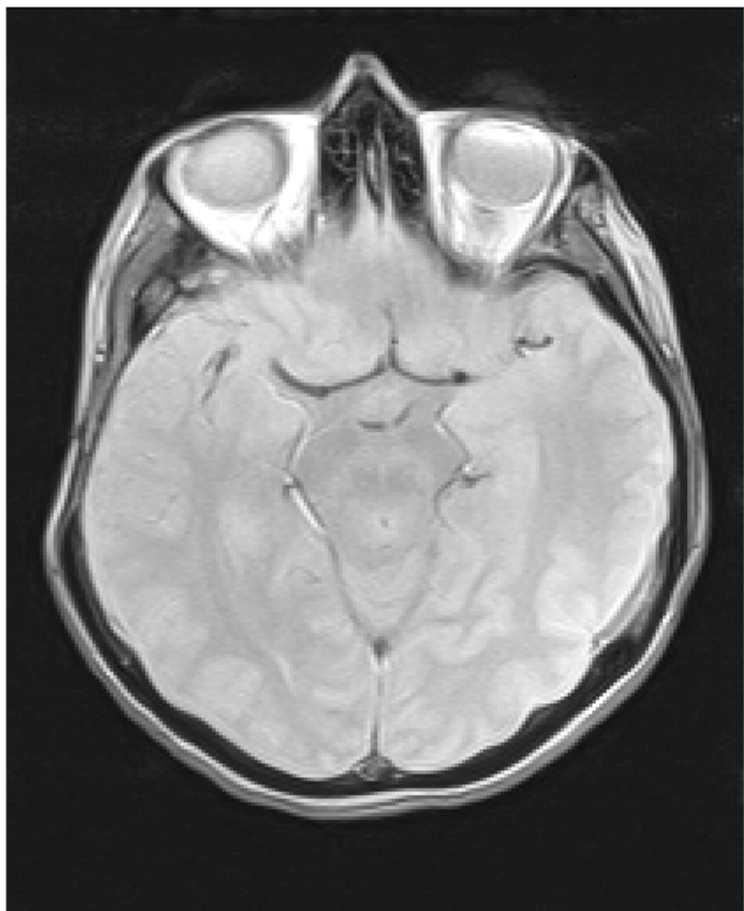


T2 Contrast
 $T_E = 100 \text{ ms}$
 $T_R = 1500 \text{ ms}$

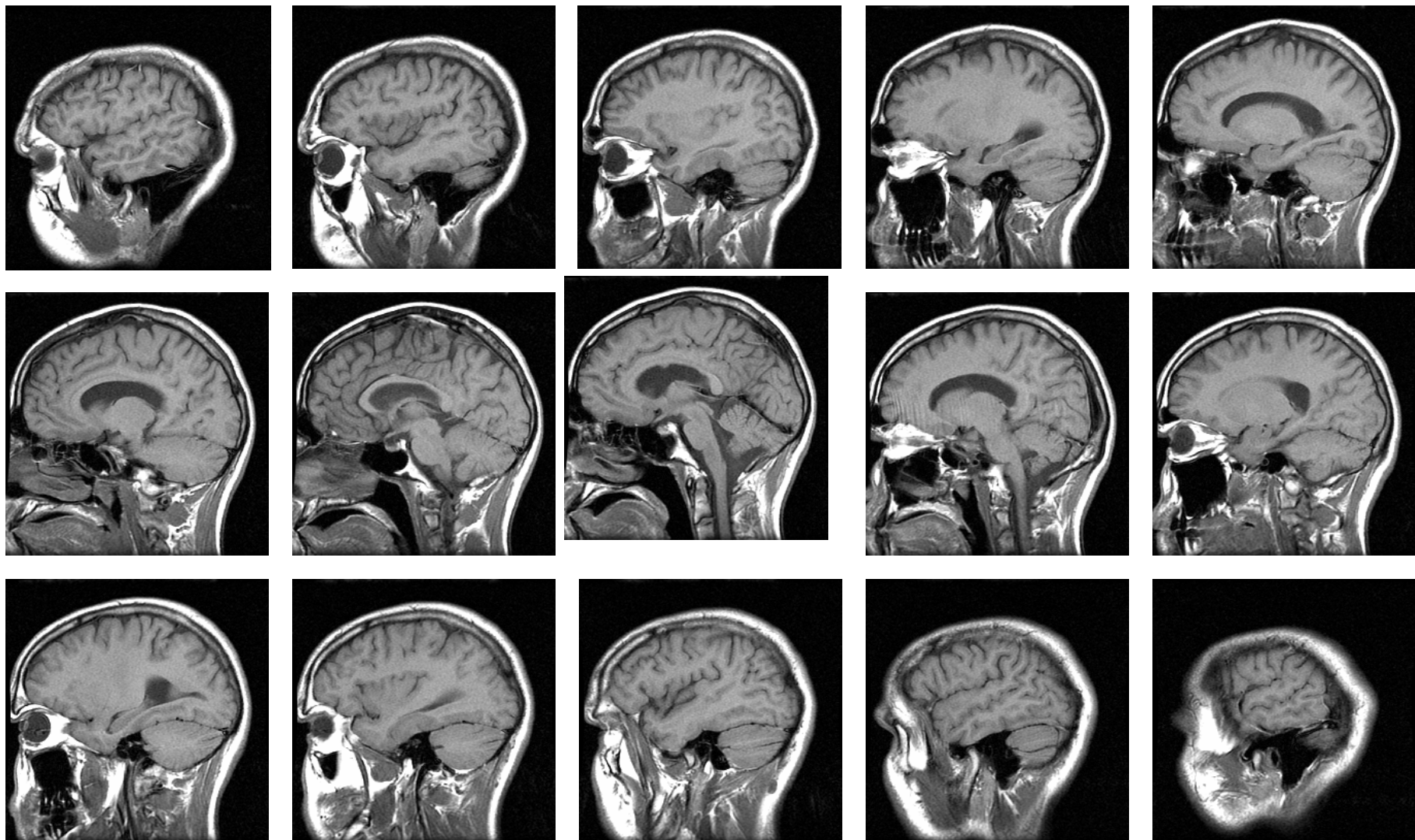


Proton density
 $T_E = 14 \text{ ms}$
 $T_R = 1500 \text{ ms}$

T2 weighting SE (double echo)

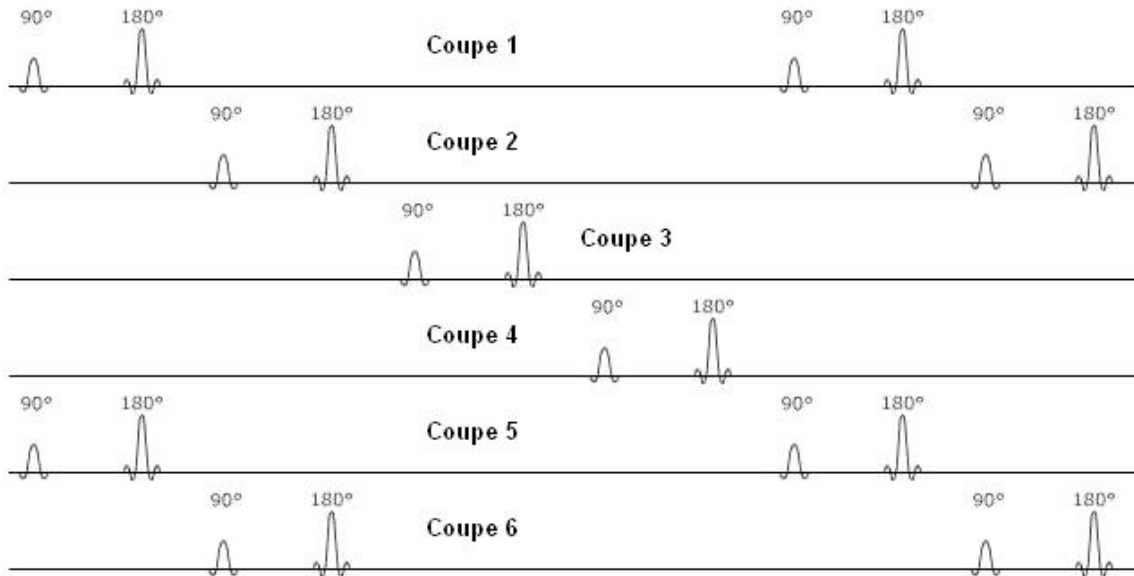


Slice in whatever plane

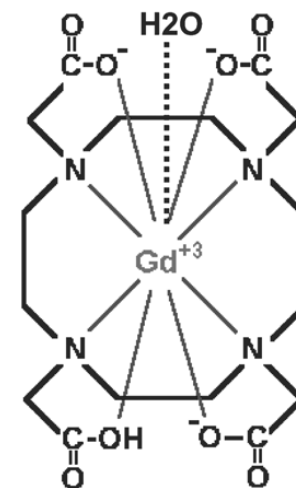


What can we do during TR?

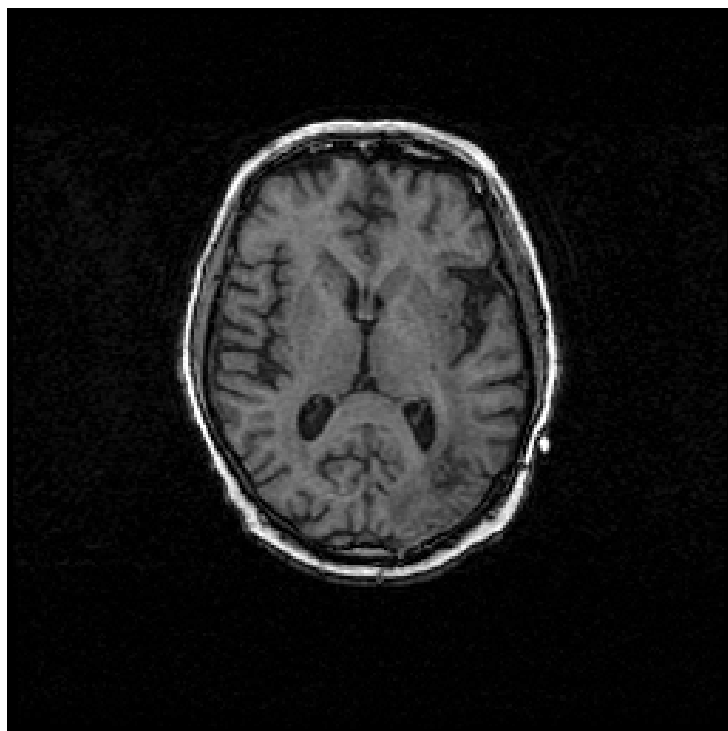
Multi-slice acquisition



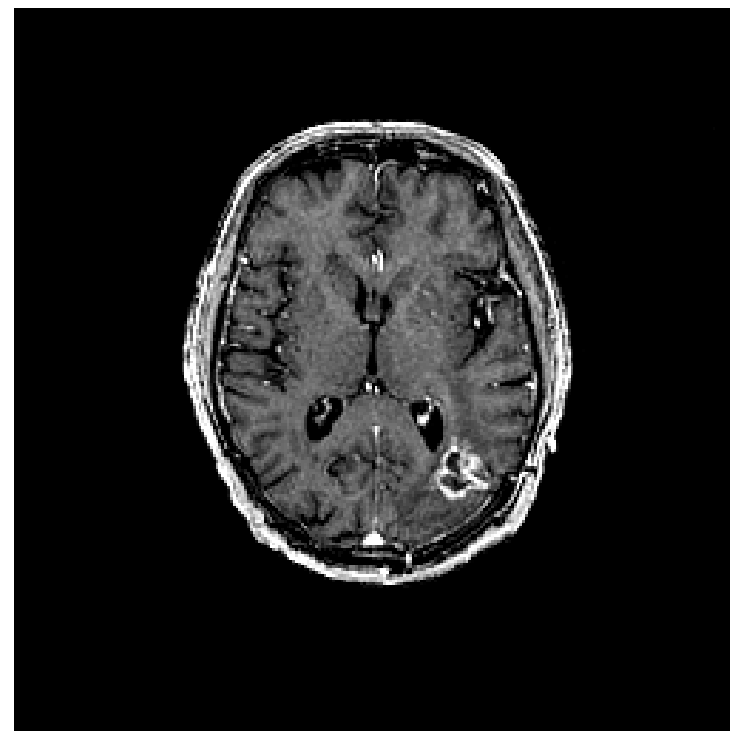
Contrast media : T1 reduction



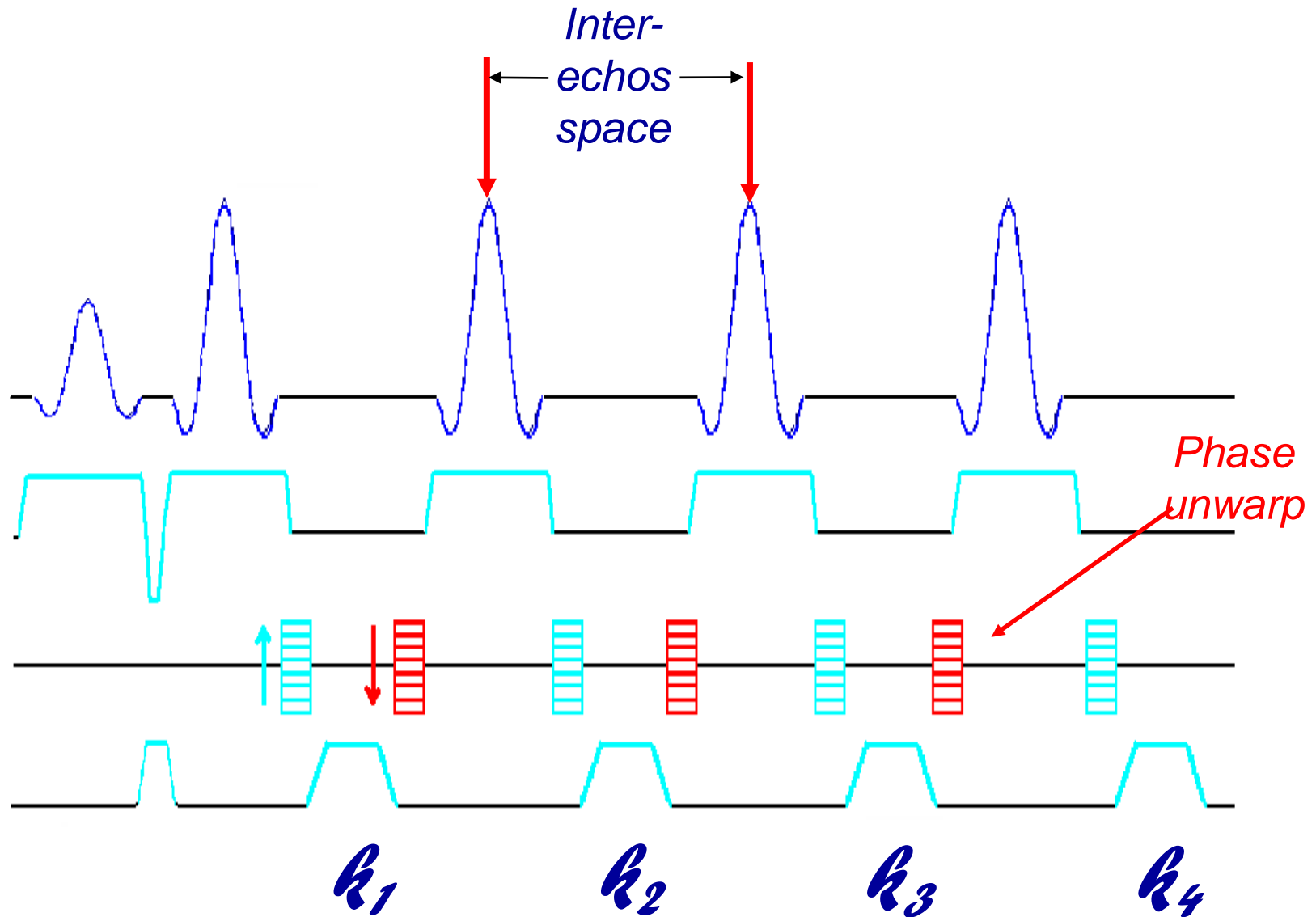
Native T1



T1 + Gd



SE and FSE what differences?



Contrast in FSE

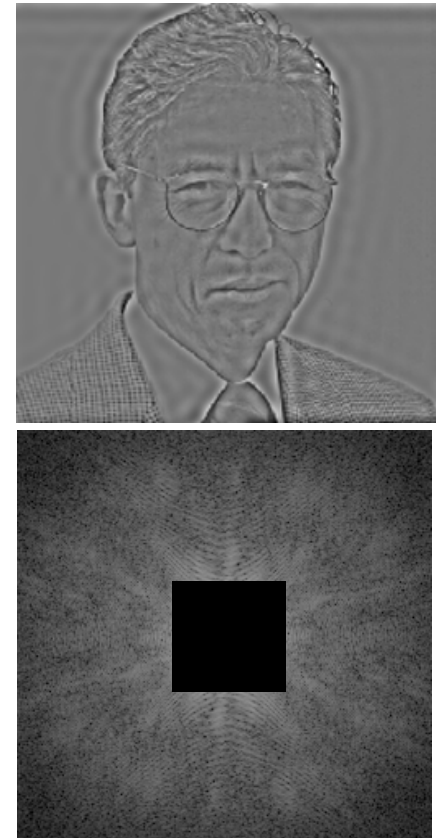
Complete image



Center of k space

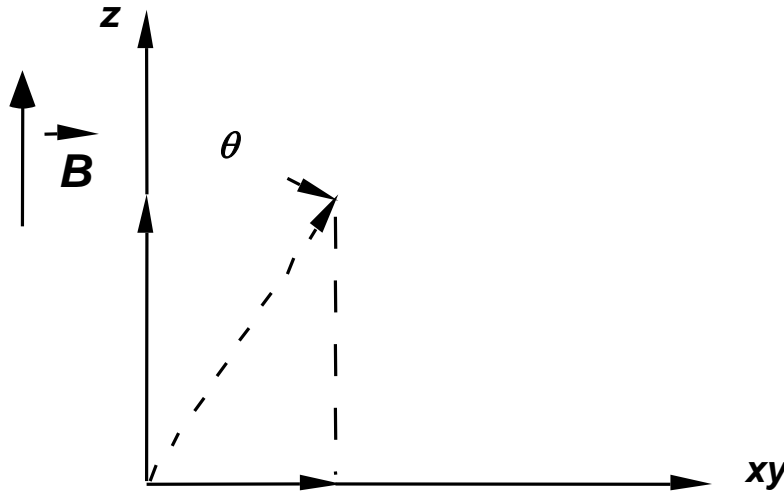


K space periphery



Acquisition time reduction: FSE (T2 contrast)
Other solution : GRE (Gradient Recalled Echo)

- *Principle : lower tip angle for M*

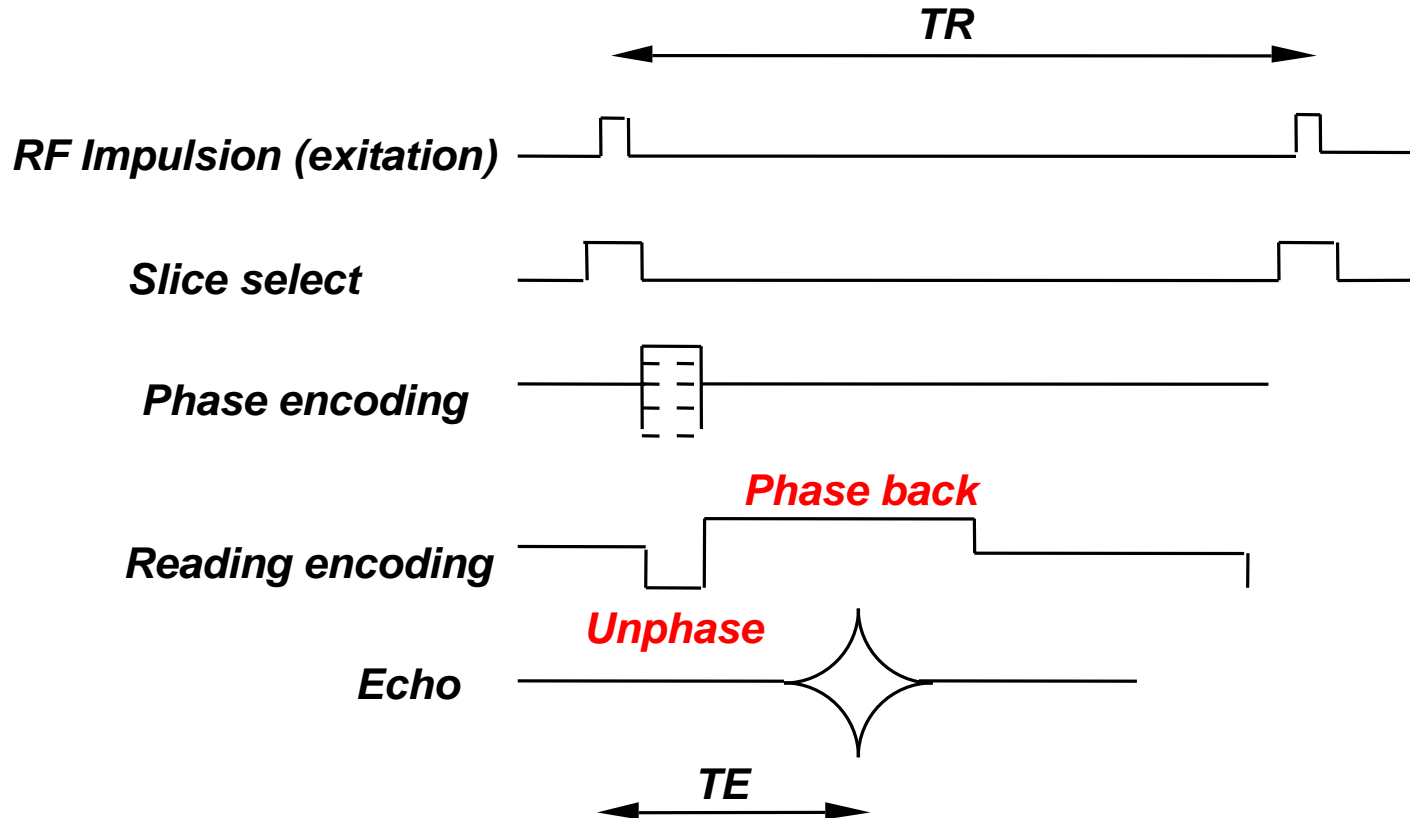


$$M_{xy} = M_o \sin \theta$$

$$M_z = M_o \cos \theta$$

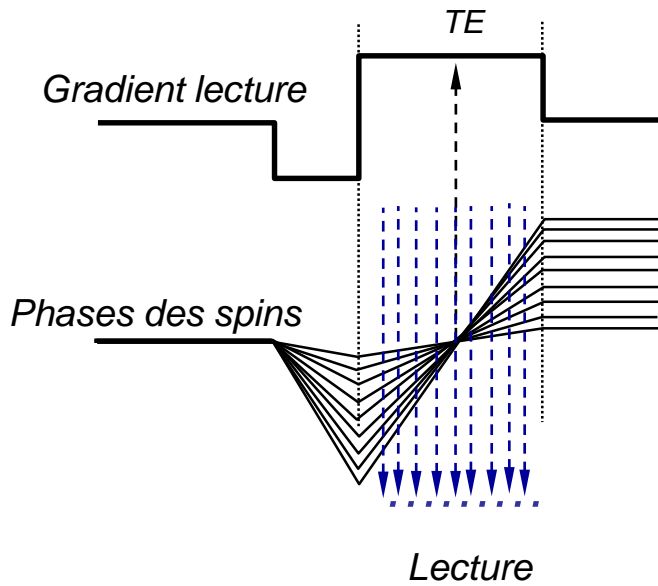
Faster T1 relaxation \rightarrow TR can be reduced

General GRE sequences



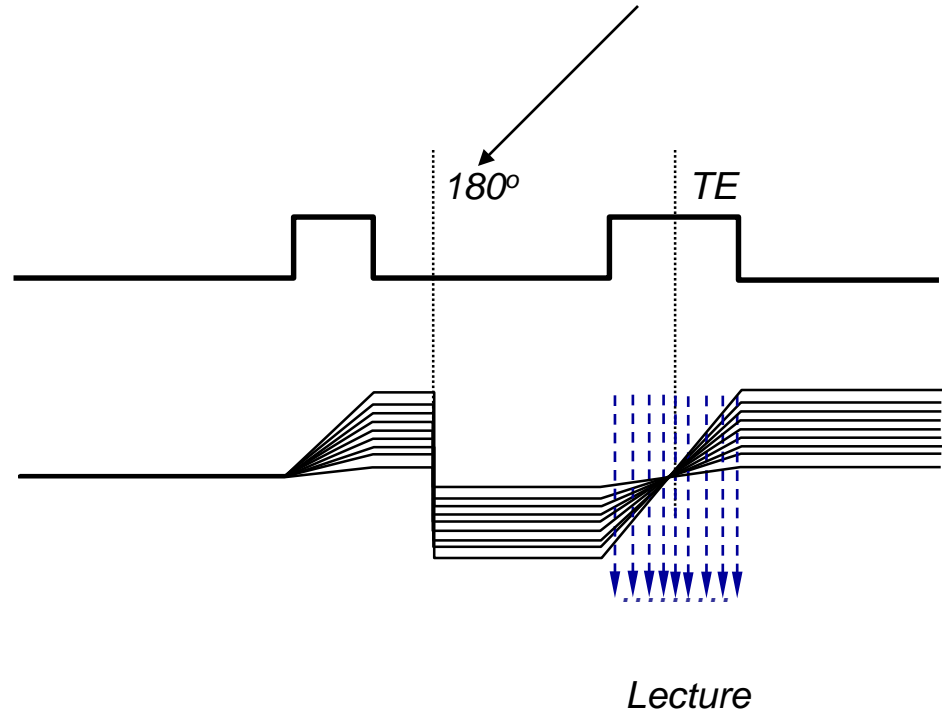
Spin behavior

GRE



$\rho, T1, T2^*$

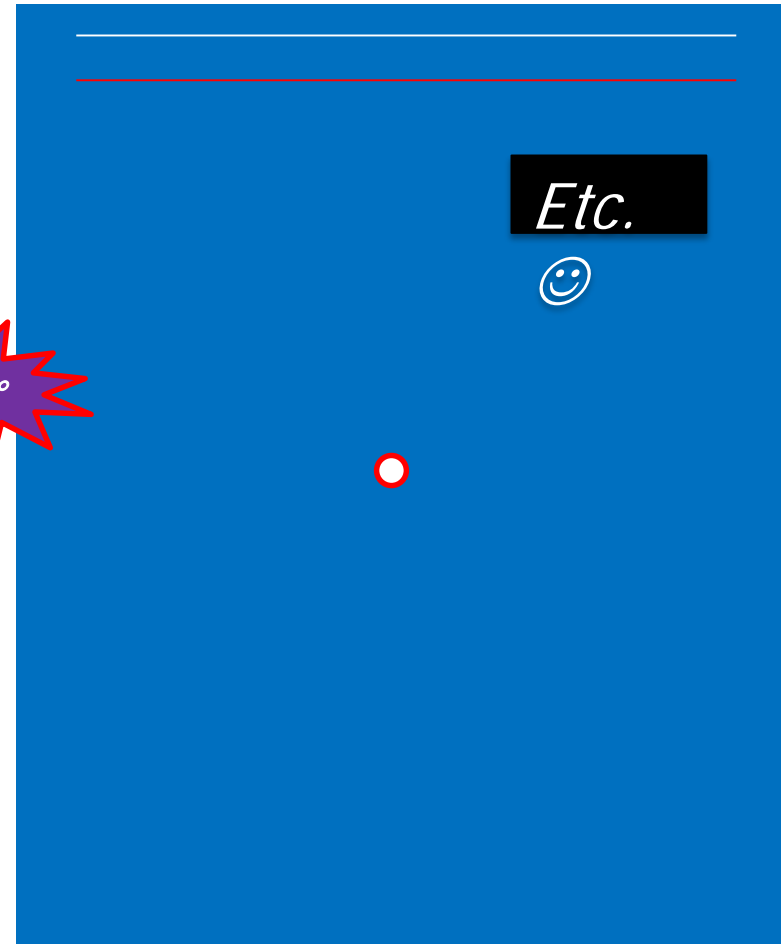
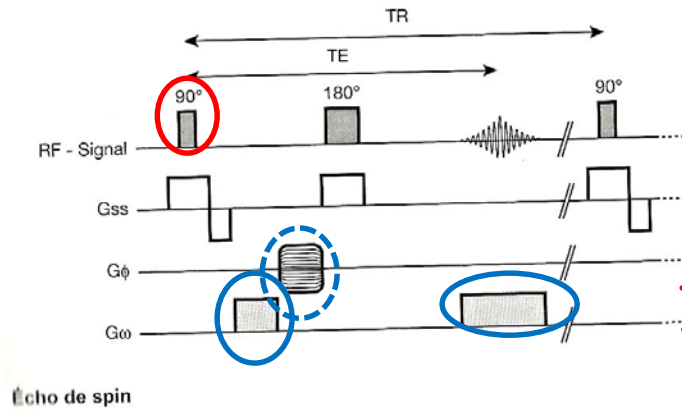
SE with refocalization impulsion



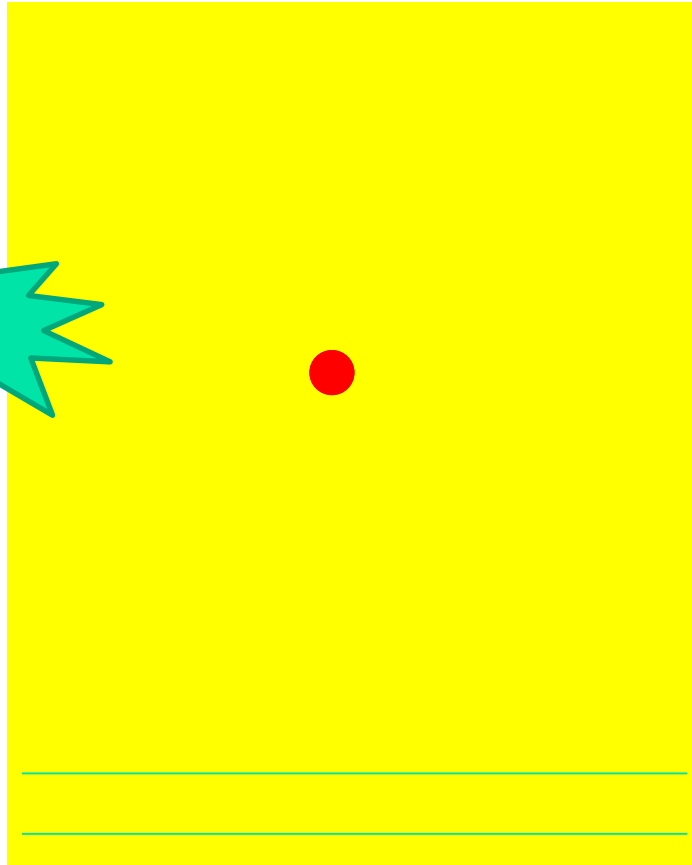
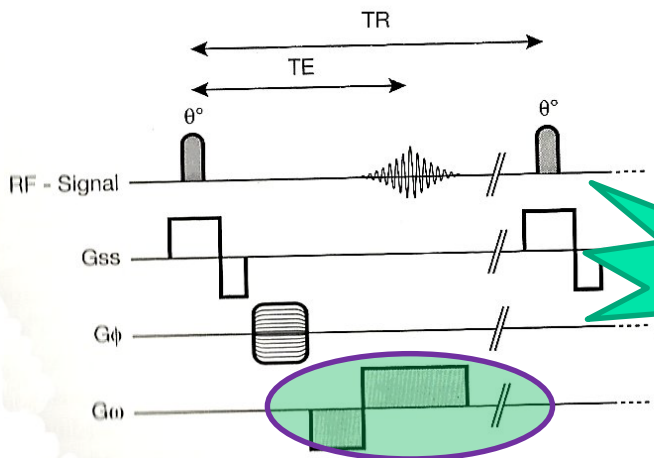
$\rho, T1, T2$

Sequence	TR		TE	
	Short	Long	Short	Long
SE	250–700	> 2000	10–25	> 60
GRE	< 50	> 100	1–5	> 10

Traveling in k space for spin echo

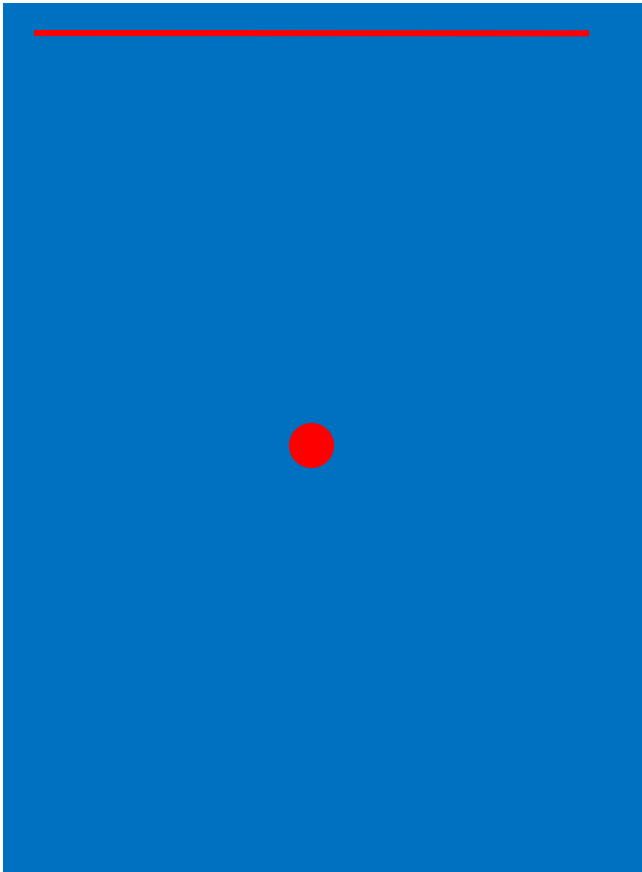


Traveling in k space for gradient echo

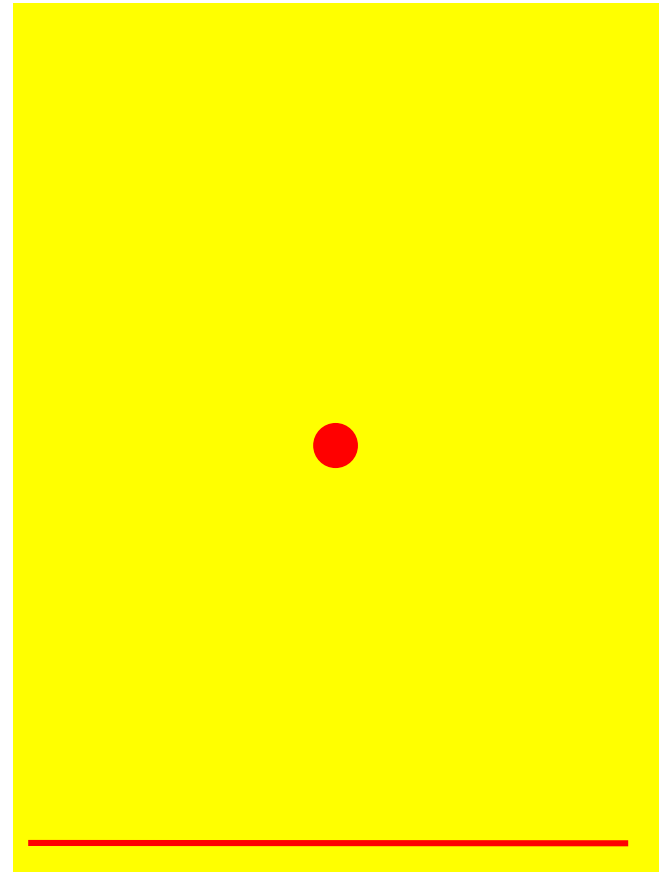


Spin echo versus gradient echo

SE

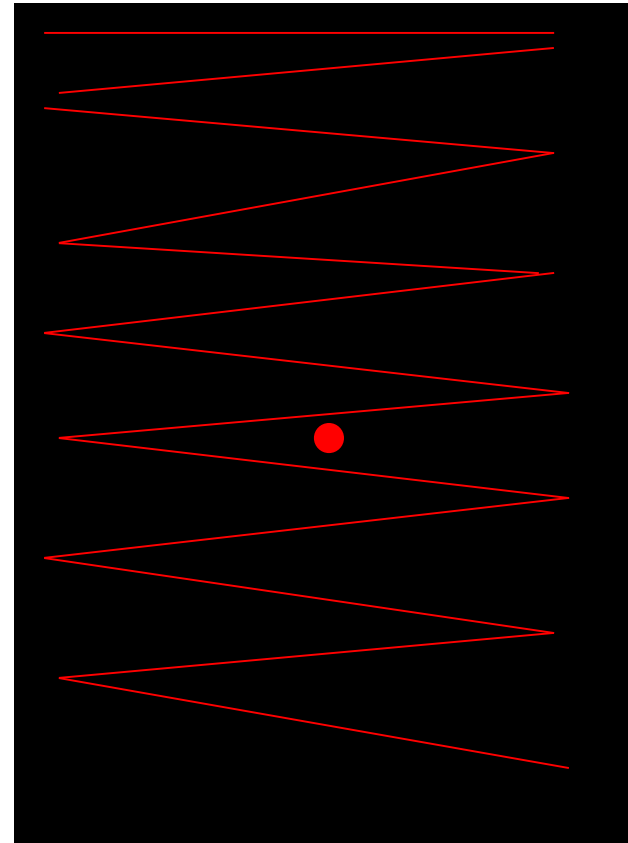


GRE



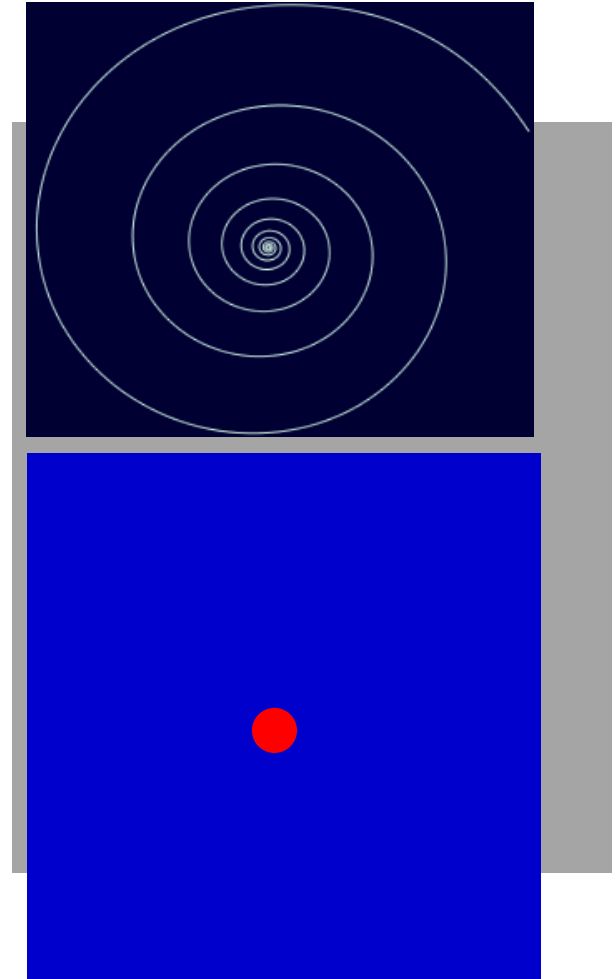
Traveling in k space for echo planar

- Excitation 90°
- Continuous G_y
- G_x alternates between positive and negative values



Traveling in k space for spiral data sampling

- Sinusoidal variation of G_y and G_x
- Variable intensity
- For what ?



Functional imaging: MR spectroscopy

