$\frac{\text{Design Technologies for Integrated Systems} - \text{EPFL}}{\text{Exercise 5}} \\ \frac{25/10/2018}{}$

Problem 1

Consider the Boolean function G = a'c'd + a'cd + ab'c' + abc + ac. The positional cube notation can be used to compute cofactors, tautology, and implicant containment. Use it to show which of the following implicants are contained by G:

- (a) *cd*
- (b) ad

Problem 2

Given the constraint mapping A, find the minimum encoding matrix E that satisfies the constraints of A.

$$A = \begin{pmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{pmatrix} \tag{1}$$

- (a) Write the dichotomies considering that the columns in A correspond to the operations AND, OR, JMP and ADD.
- (b) Write the seed dichotomies.
- (c) Find the compatible seed dichotomies and draw the compatibility graph.
- (d) Find the prime dichotomies.
- (e) Write the covering matrix and find a minimum cover.
- (f) Write the encoding matrix.