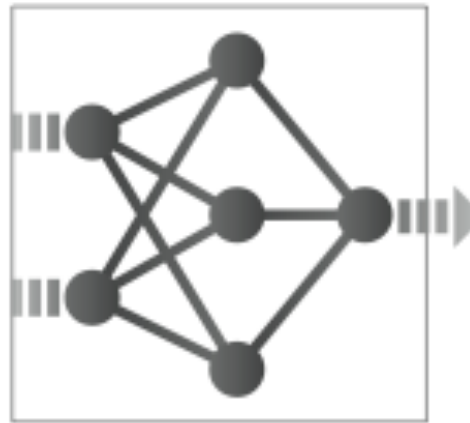
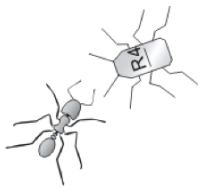


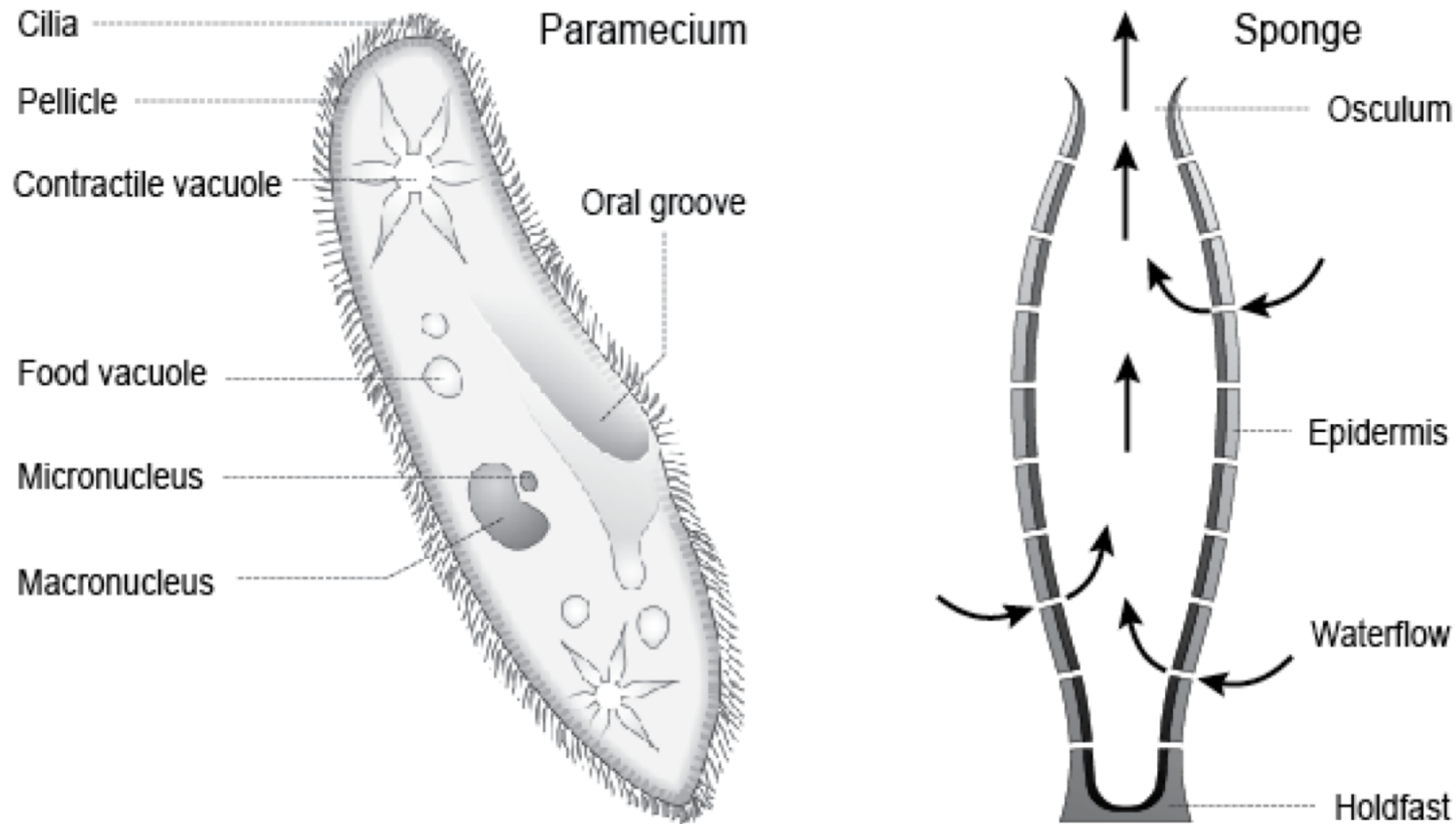
# Neural Systems



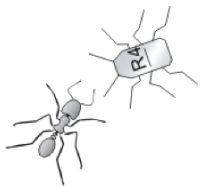
## Part 1



# Do animals need nervous systems?

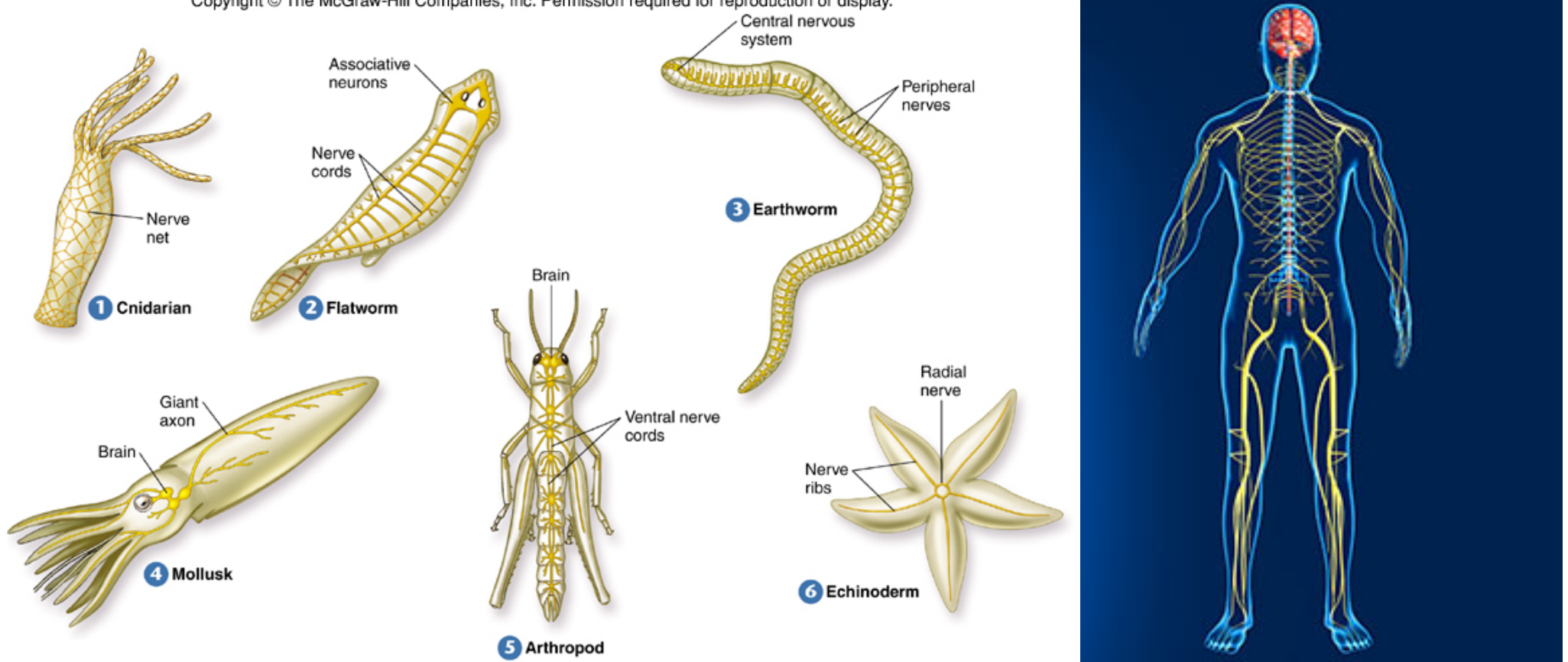


Not all animals have nervous systems; some use only chemical reactions  
Paramecium and sponge move, eat, escape, display habituation

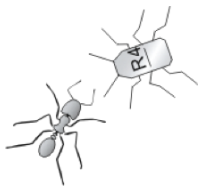


# Why Nervous Systems?

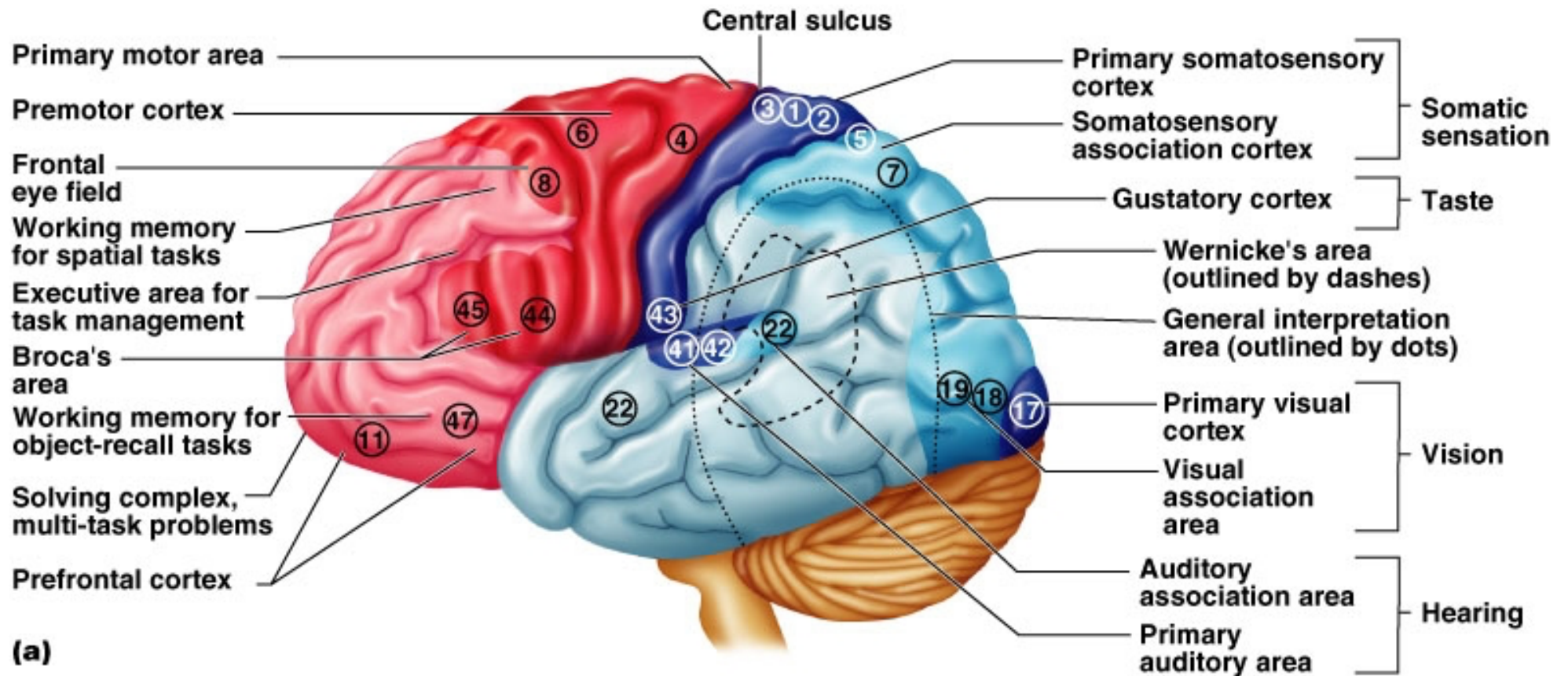
Copyright © The McGraw-Hill Companies, Inc. Permission required for reproduction or display.



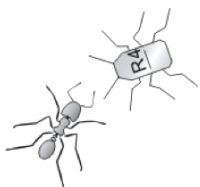
- 1) Faster reaction times = competitive advantage
- 2) Selective transmission of signals across distant areas = more complex bodies
- 3) Generation of non-reactive behaviors
- 4) Complex adaptation = survival in changing environments



# Central Nervous System with Cortex

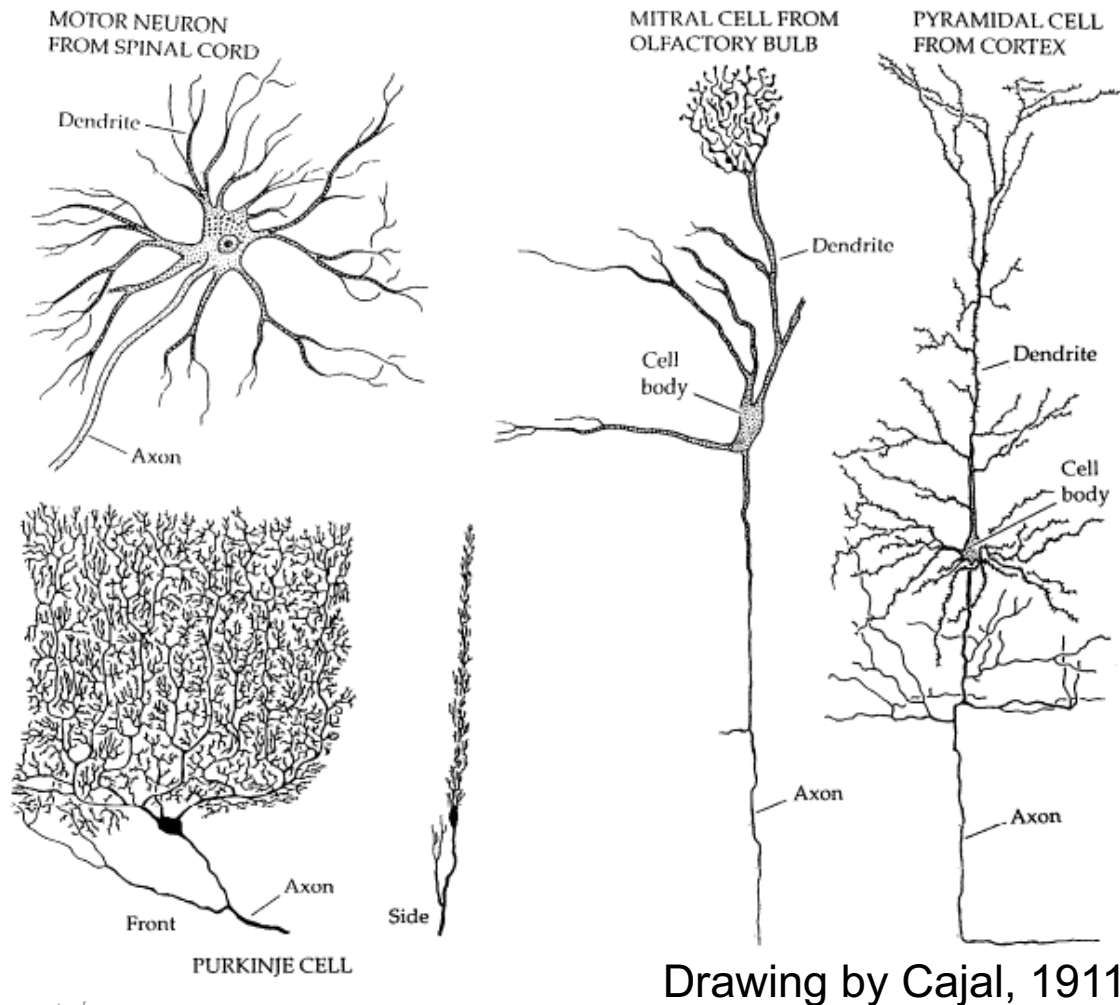


Copyright © 2004 Pearson Education, Inc., publishing as Benjamin Cummings.



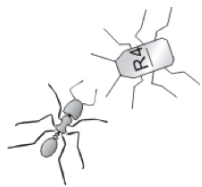
# What Does Make Brains Different?

Components and behavior of individual neurons are very similar across animal species and, presumably, over evolutionary history (Parker, 1919)

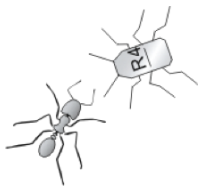
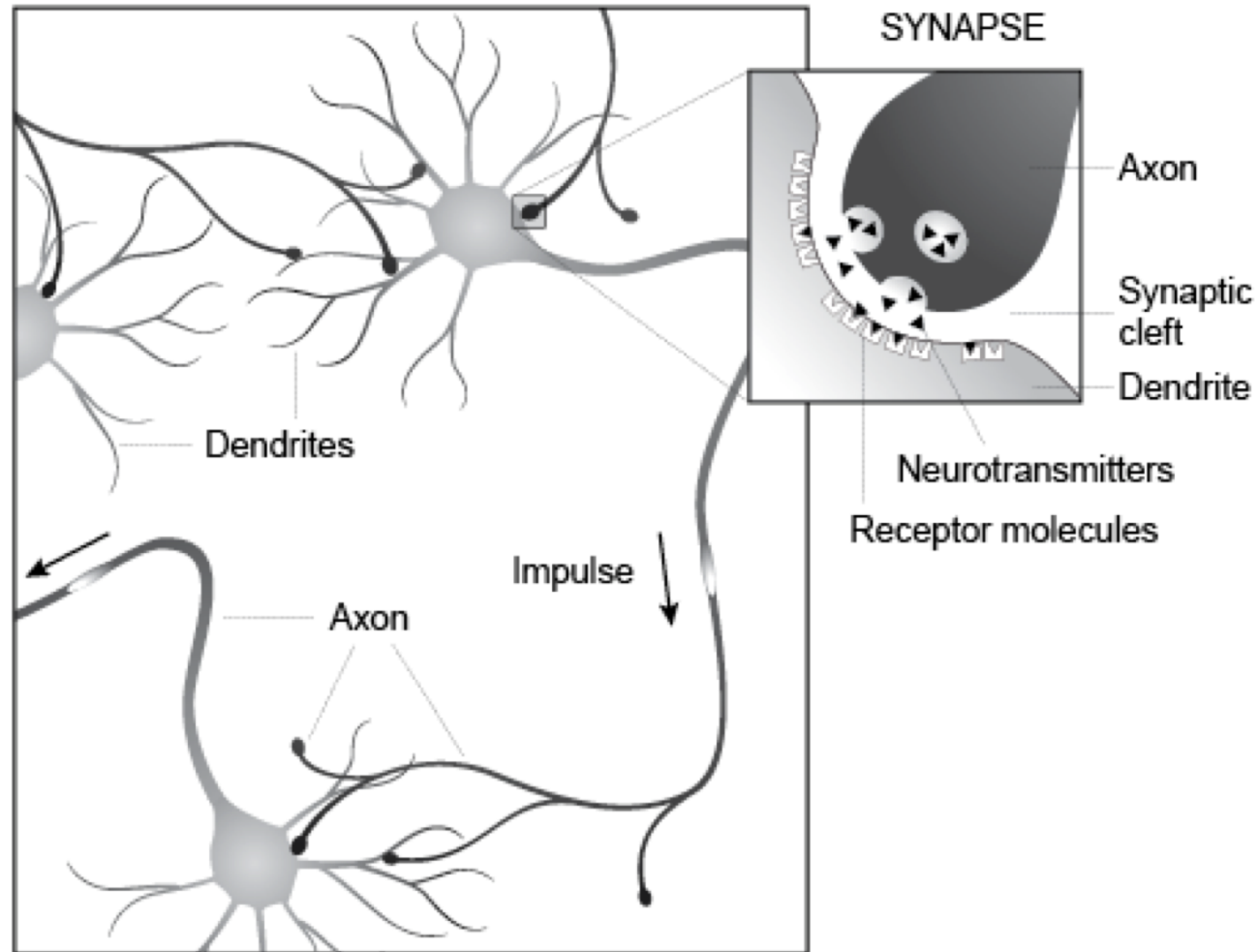


Evolution of the brain seems to occur mainly in the **architecture**, that is how neurons are interconnected.

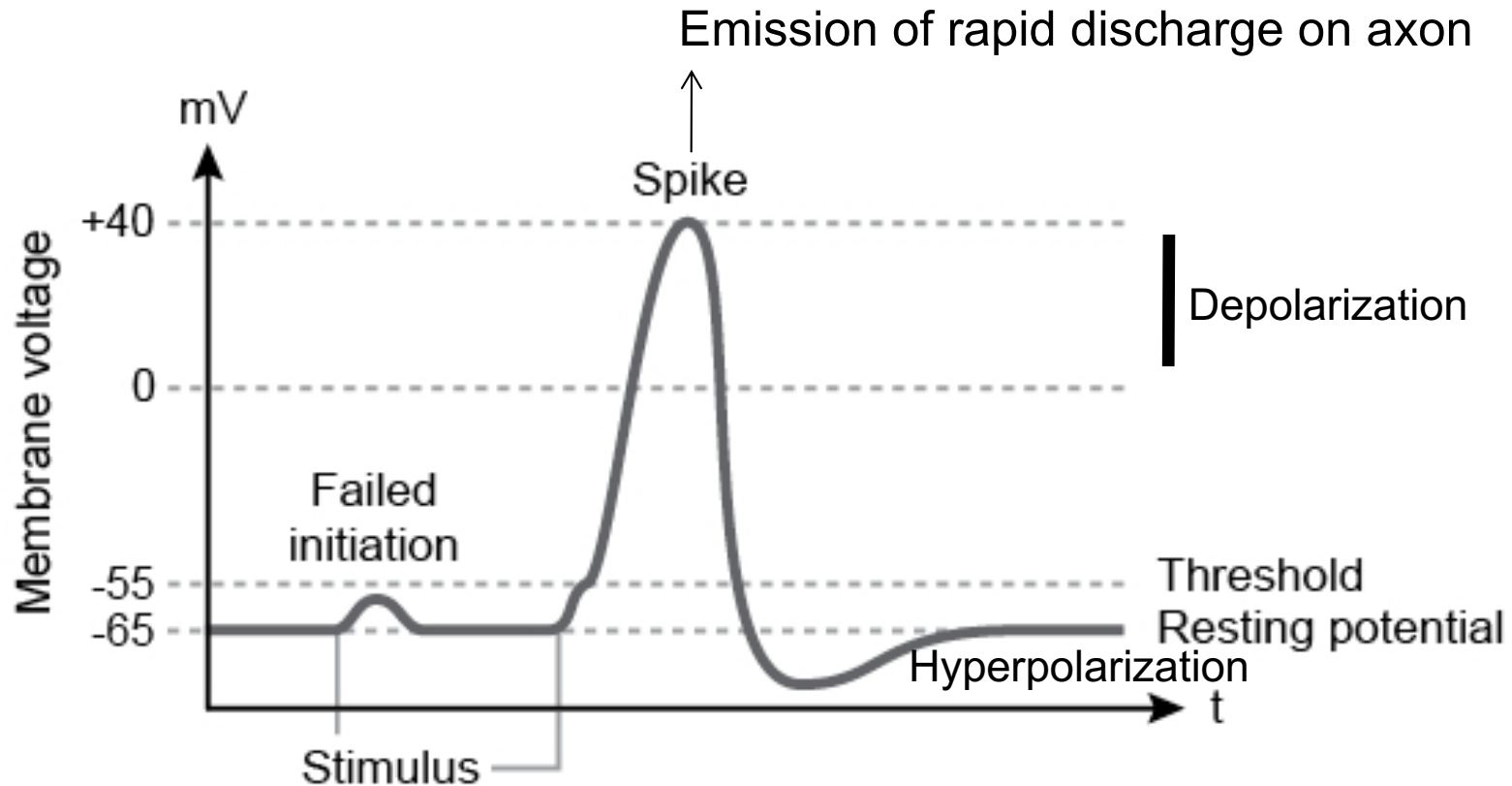
First classification of neurons by Cajal in 1911 was made according to their connectivity patterns



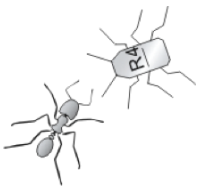
# Biological Neurons



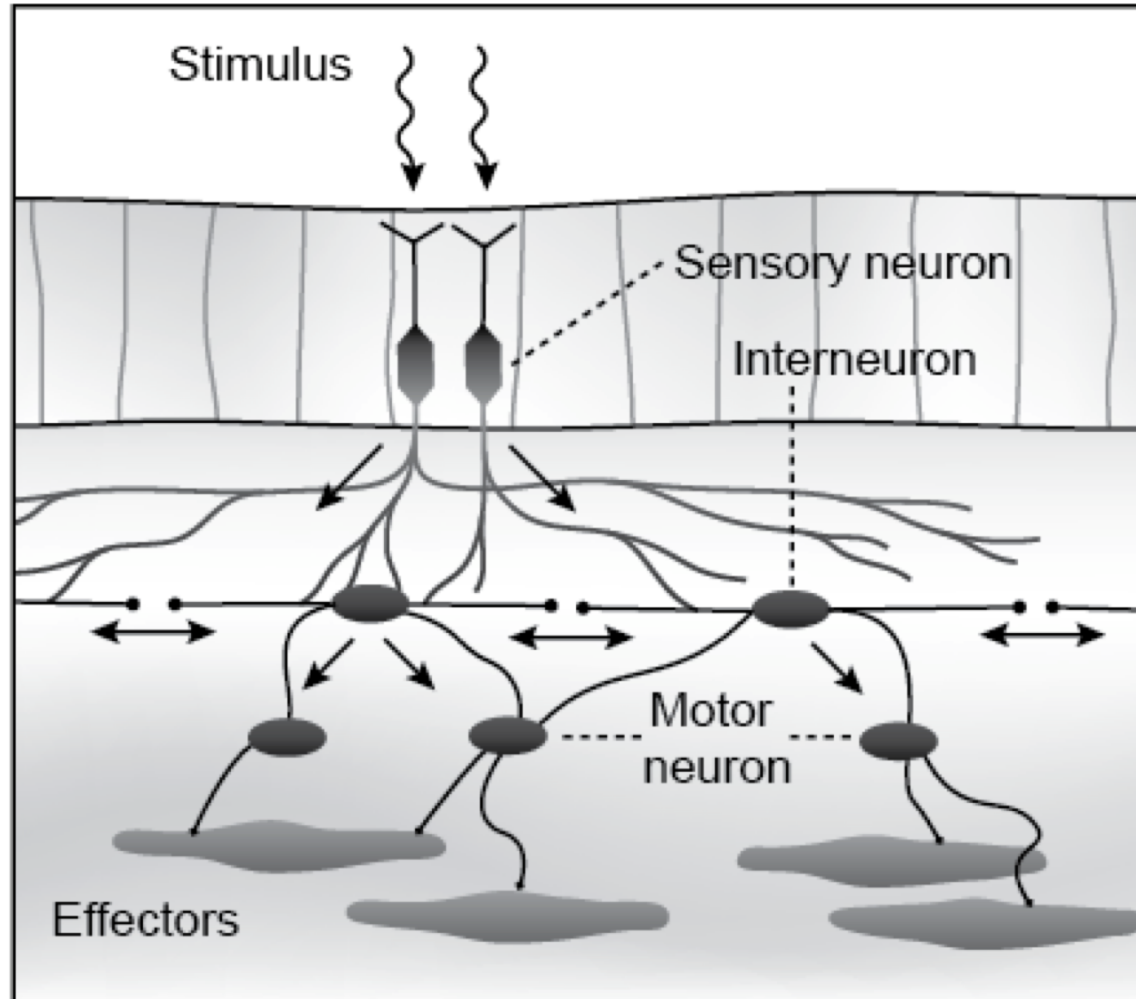
# Membrane Dynamics



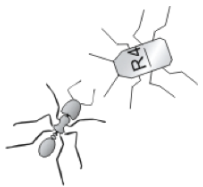
This cycle lasts approximately 3-50 ms, depending on type of ion channels involved (Hodgkin and Huxley, 1952)



# Types of Neurons

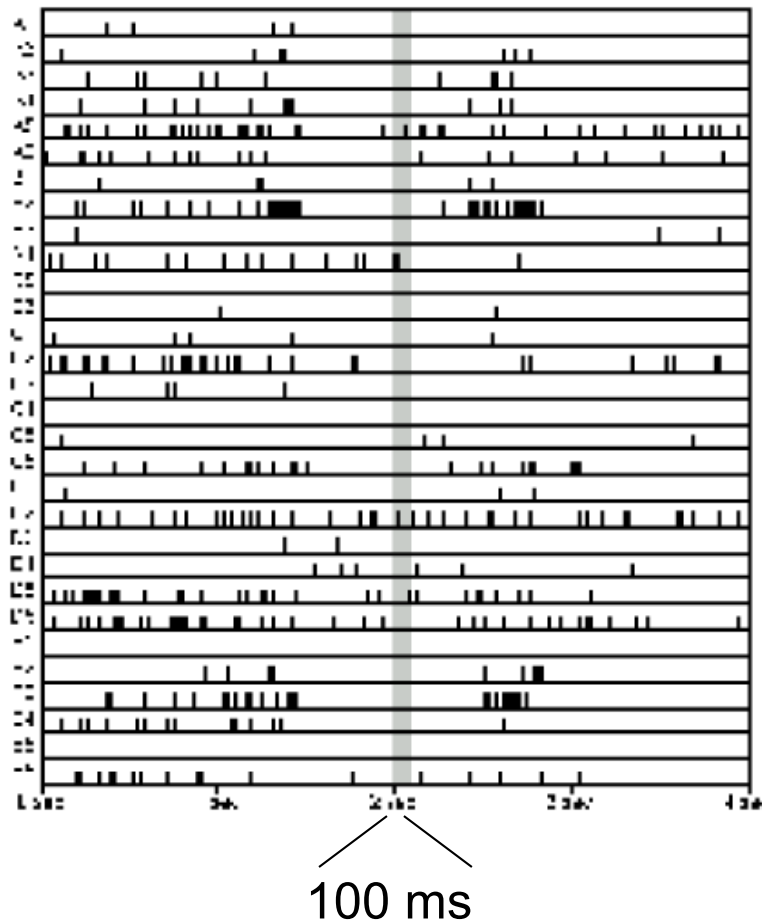


Interneurons can be  
1- Excitatory  
2- Inhibitory



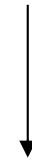


# How Do Neurons Communicate?



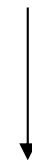
Firing rate

Firing time



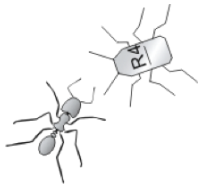
McCulloch-Pitts

Spiking neurons



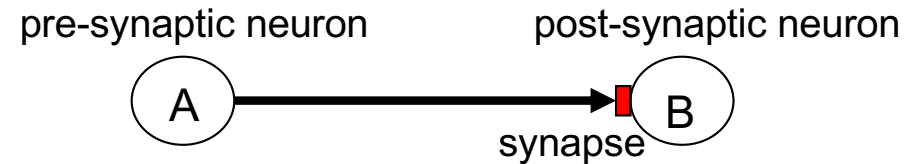
Connectionism

Computational  
Biology



# How Do Neurons Learn?

They learn by means of synaptic change



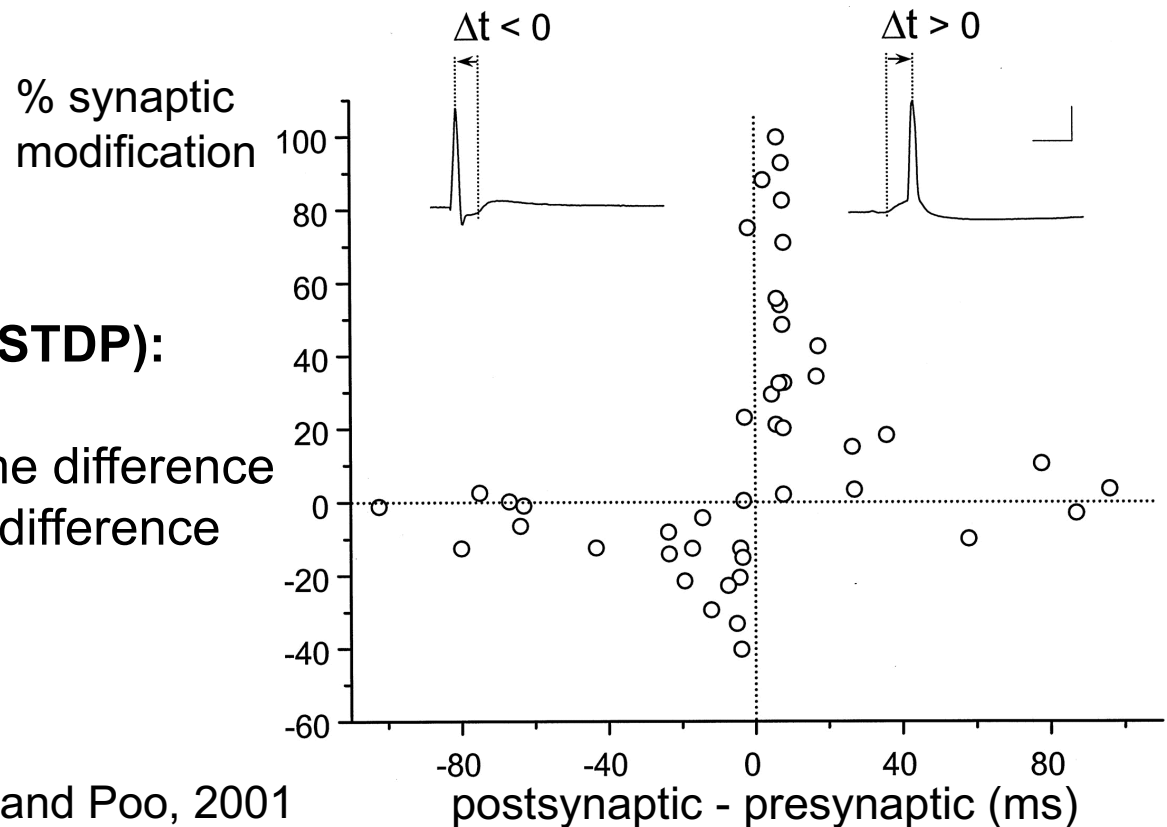
## Hebb rule (1949):

Synaptic strength is increased if cell A consistently contributes to firing of cell B

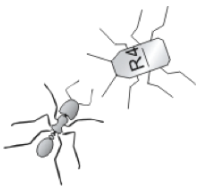
This implies a temporal relation: neuron A fires first, neuron B fires second

## Spike Time Dependent Plasticity (STDP):

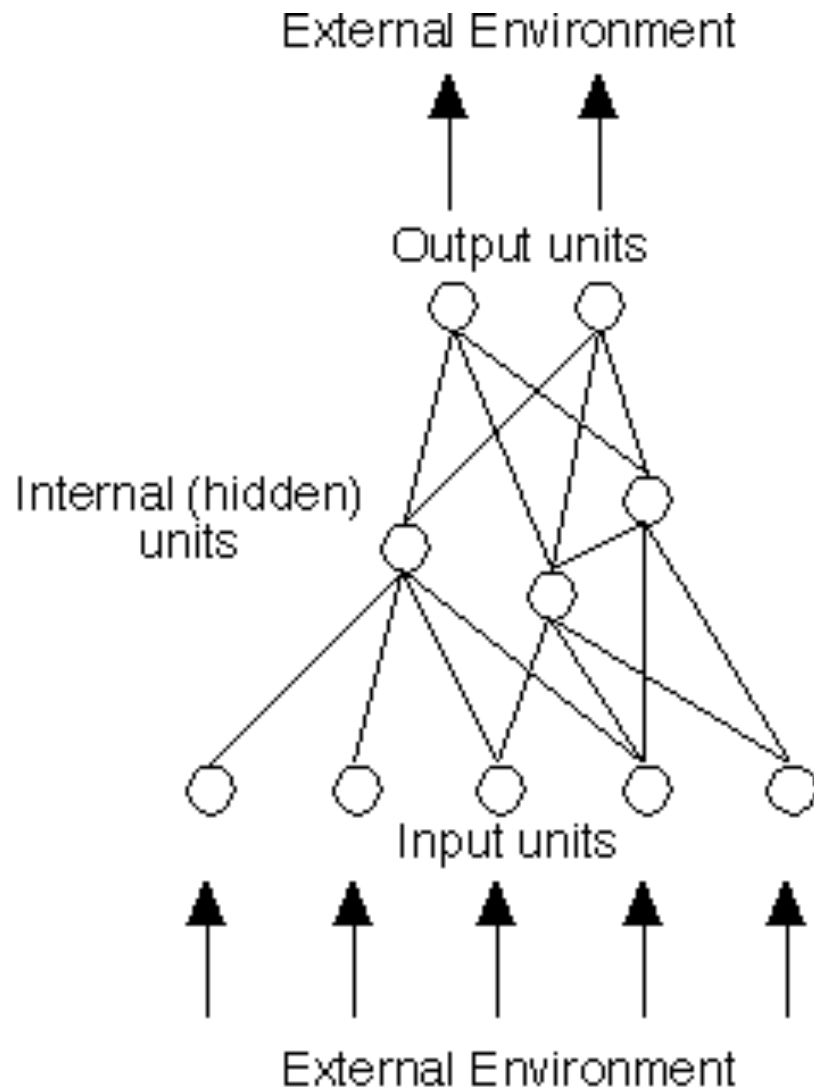
- Small time window
- Strengthening (LTP) for positive time difference
- Weakening (LTD) for negative time difference



From Bi and Poo, 2001



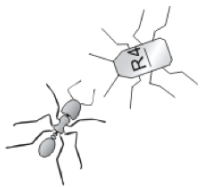
# An Artificial Neural Network



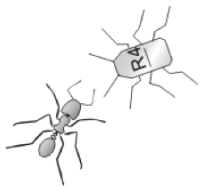
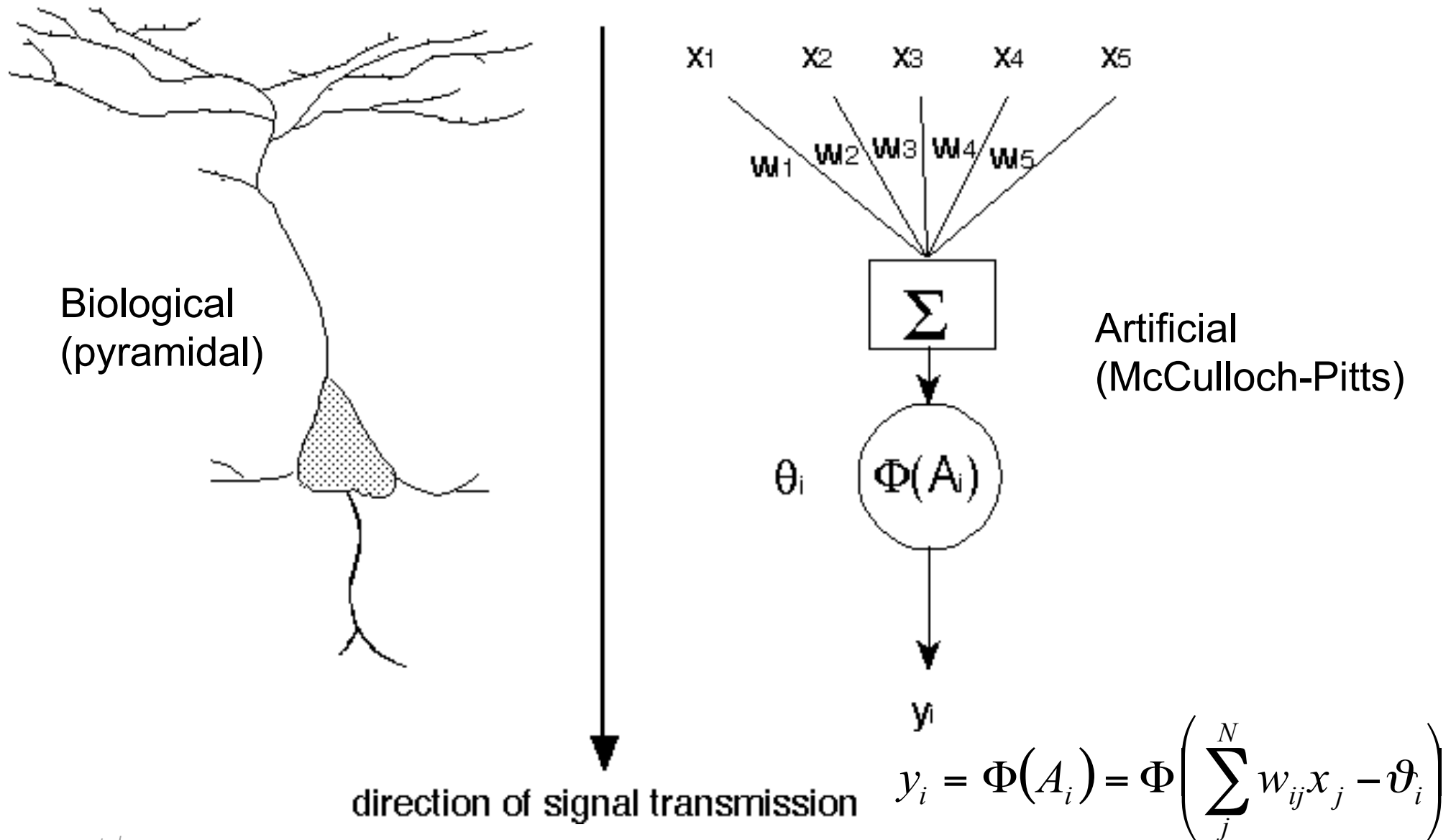
A neural network communicates with the environments through input units and output units. All other elements are called internal or hidden units.

Units are linked by uni-directional connections.

A connection is characterized by a weight and a sign that transforms the signal.

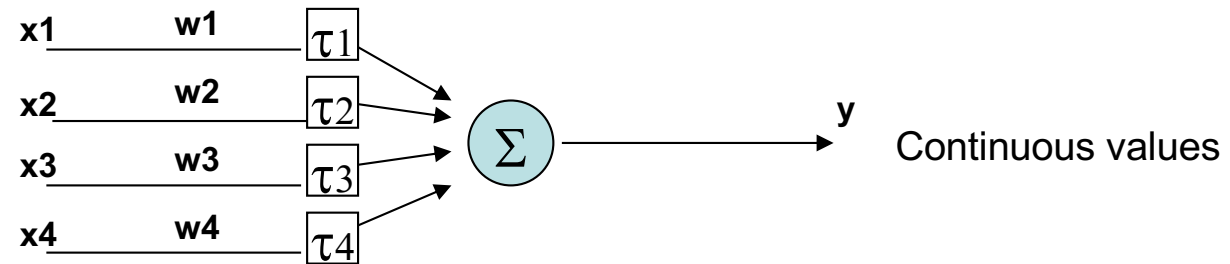


# Biological and Artificial Neurons

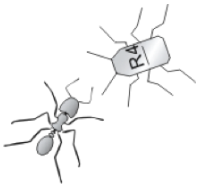
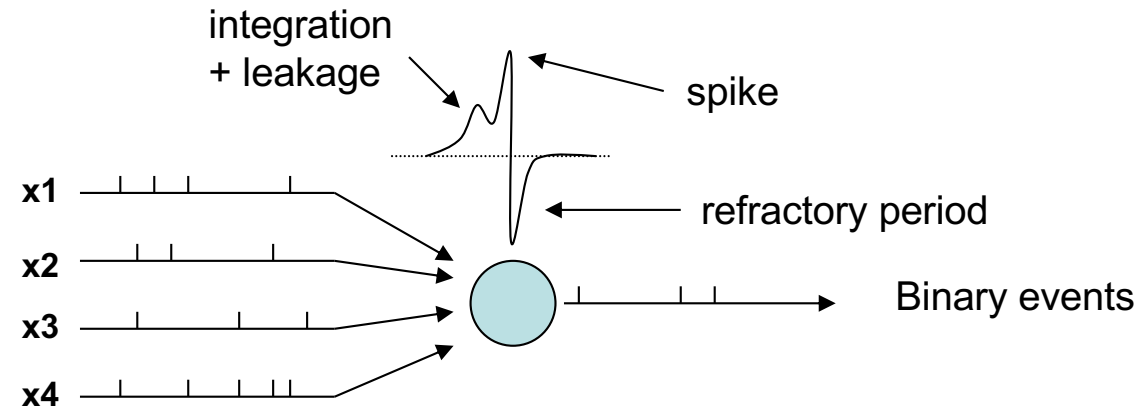


# Neuron models

McCulloch-Pitts



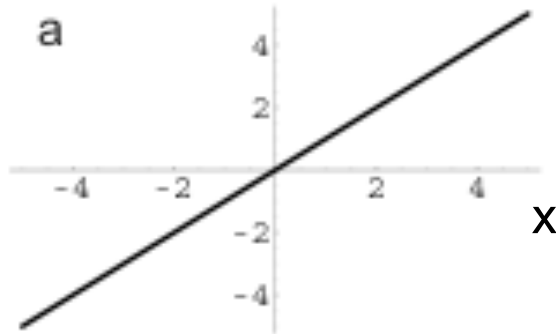
Spiking



# Output functions

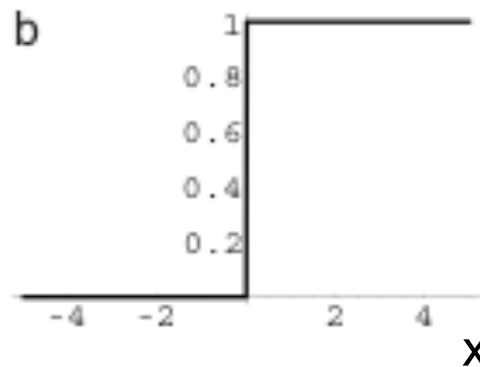
Identity

$\Phi(x)$



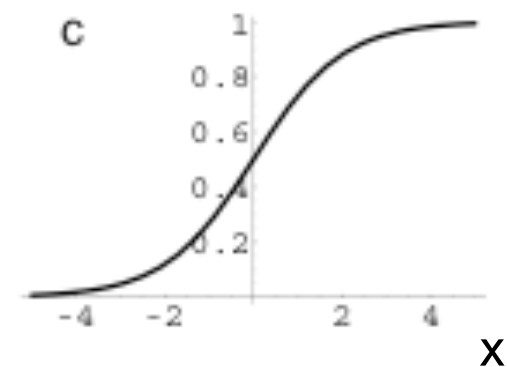
Step

$\Phi(x)$



Sigmoid

$\Phi(x)$

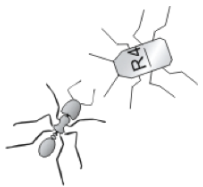


**Sigmoid function:**

- continuous
- non-linear
- monotonic
- bounded
- asymptotic

$$\Phi(x) = \frac{1}{1 + e^{-kx}}$$

$$\Phi(x) = \tanh(kx)$$



# Neurons signal “familiarity”

The output of a neuron is a measure of similarity between its input pattern and its pattern of connection weights.

1. Output of a neuron in linear algebra notation:

$$y = a \left( \sum_i^N w_i x_i \right), \quad a = 1 \longrightarrow y = \mathbf{w} \cdot \mathbf{x}$$

2. Distance between two vectors is:

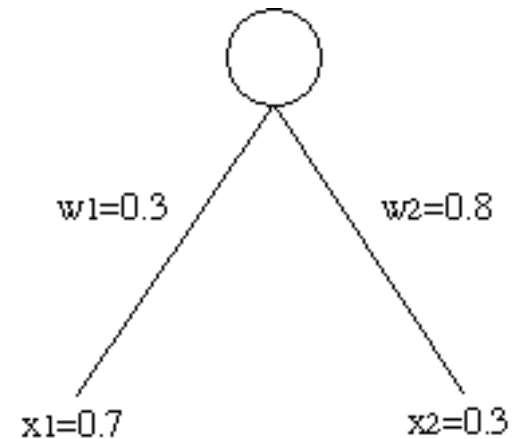
$$\cos \vartheta = \frac{\mathbf{w} \cdot \mathbf{x}}{\|\mathbf{w}\| \|\mathbf{x}\|}, \quad 0 \leq \vartheta \leq \pi$$

where the vector length is:

$$\|\mathbf{x}\| = \sqrt{\mathbf{x} \cdot \mathbf{x}} = \sqrt{x_1^2 + x_2^2 + \dots + x_n^2}$$

3. Output signals input familiarity

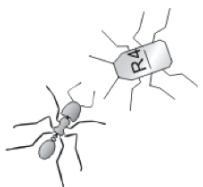
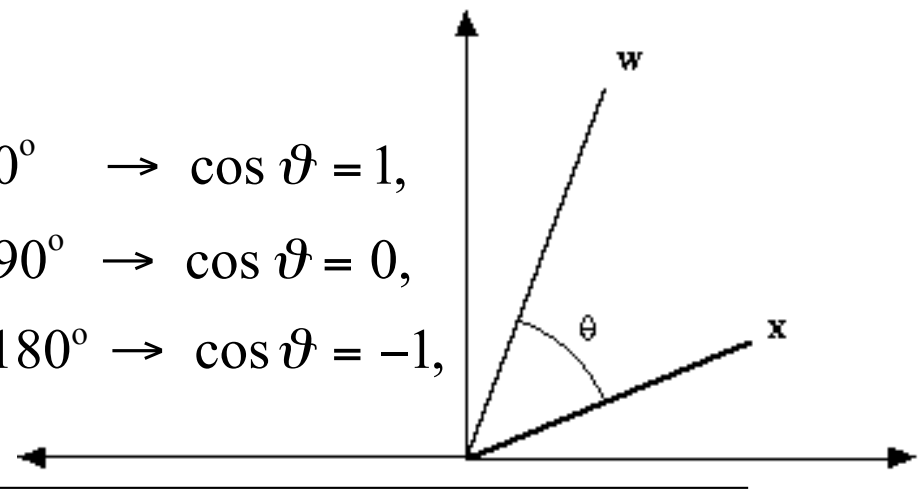
$$\mathbf{w} \cdot \mathbf{x} = \|\mathbf{w}\| \|\mathbf{x}\| \cos \vartheta$$



$$\vartheta = 0^\circ \rightarrow \cos \vartheta = 1,$$

$$\vartheta = 90^\circ \rightarrow \cos \vartheta = 0,$$

$$\vartheta = 180^\circ \rightarrow \cos \vartheta = -1,$$

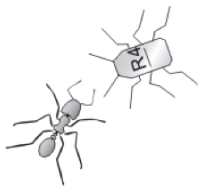
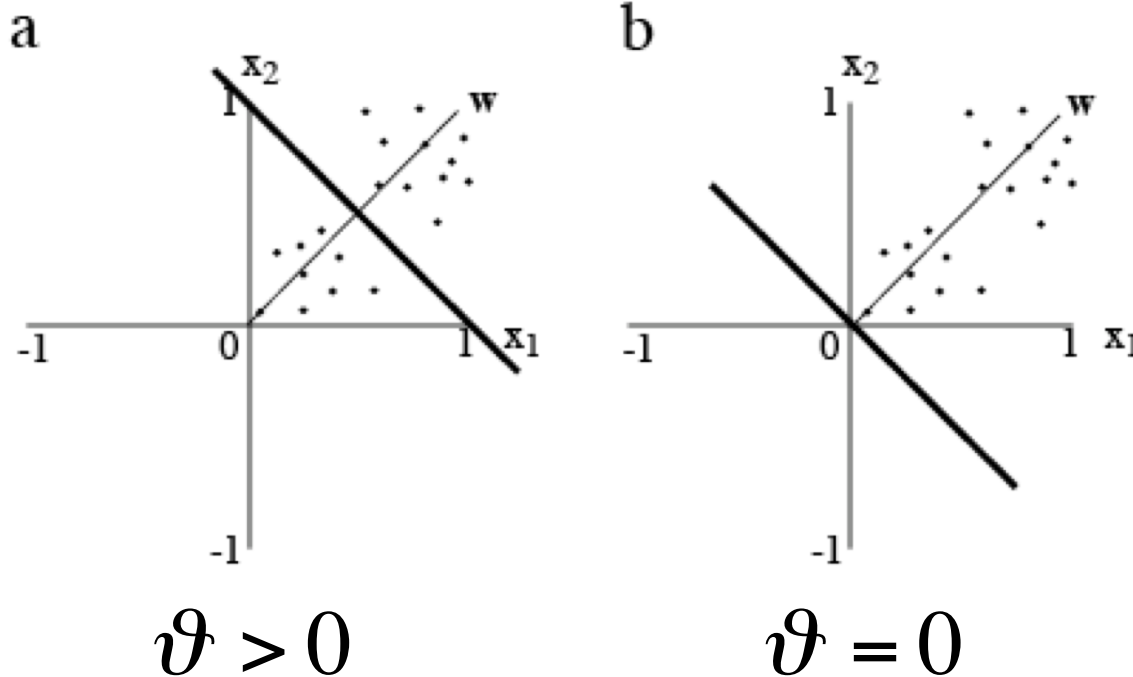


# Neurons as classifiers

A binary neuron divides the input space in two regions, one where weighted input sum  $\geq 0$  and one where weighted input sum  $< 0$ .

The separation line is defined by the synaptic weights:

$$w_1 x_1 + w_2 x_2 - \vartheta = 0 \quad x_2 = \frac{\vartheta}{w_2} - \frac{w_1}{w_2} x_1$$



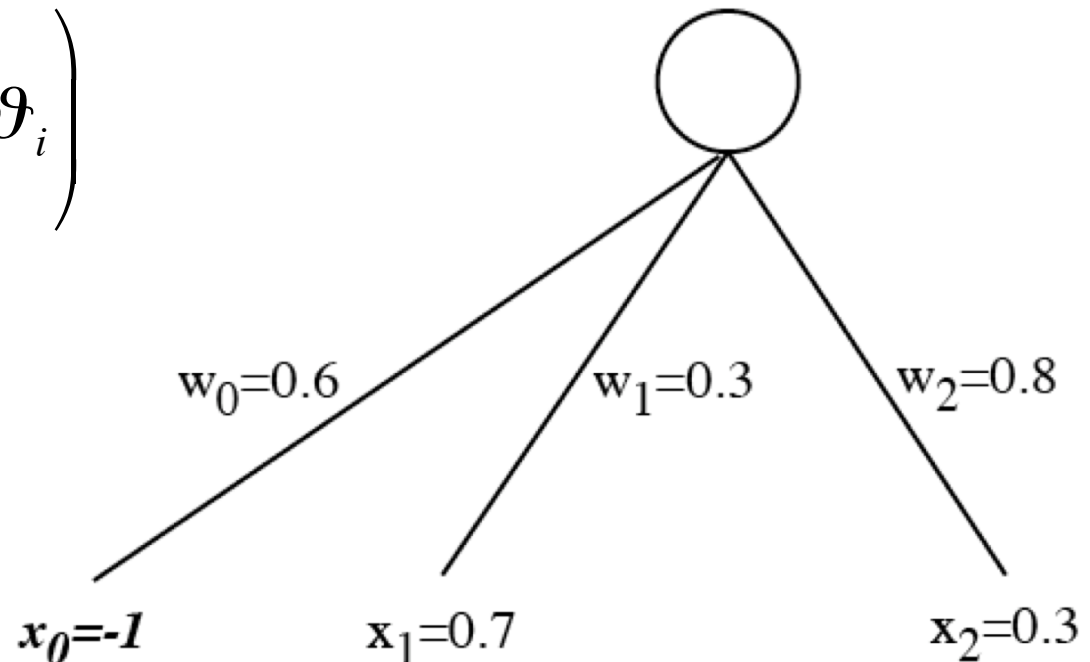


# From Threshold to Bias unit

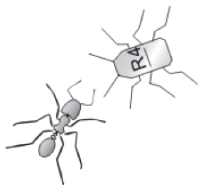
The threshold can be expressed as an additional weighted input from a special unit, known as bias unit, whose output is always -1.

$$y_i = \Phi(A_i) = \Phi\left(\sum_{j=1}^N w_{ij} x_j - \vartheta_i\right)$$

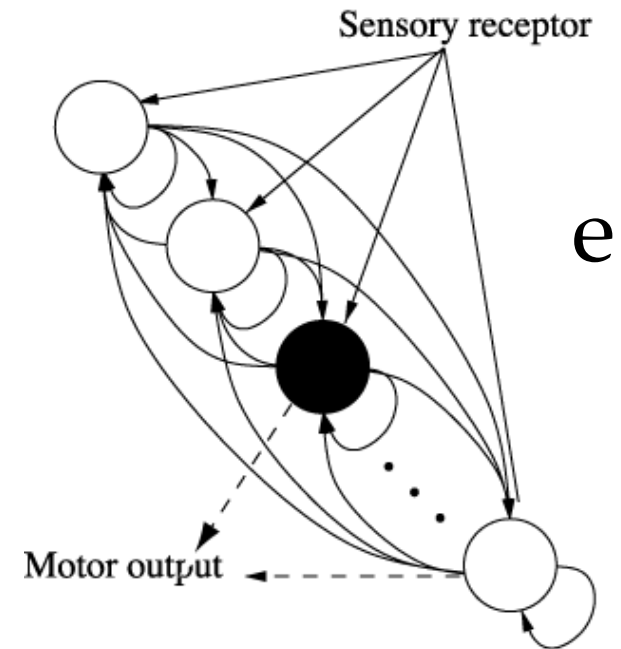
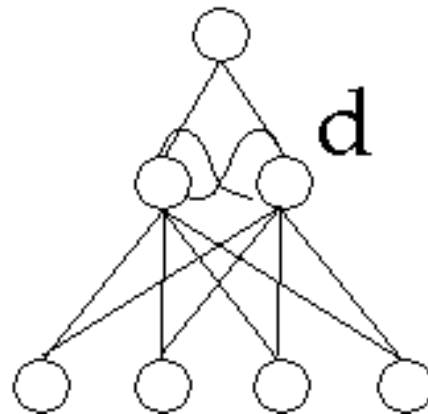
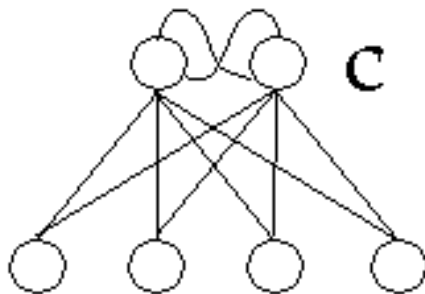
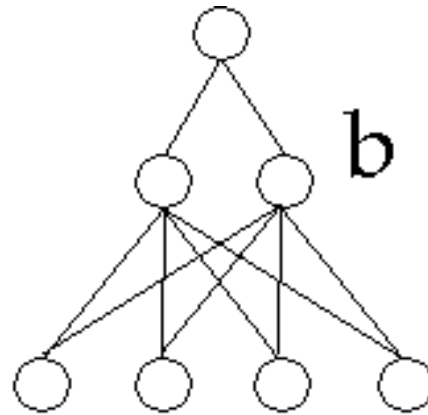
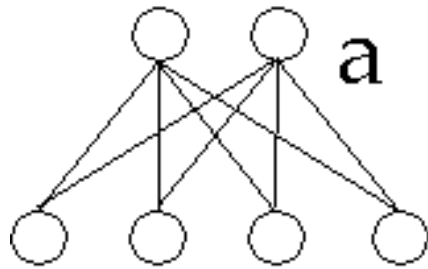
$$y_i = \Phi(A_i) = \Phi\left(\sum_{j=0}^N w_{ij} x_j\right)$$



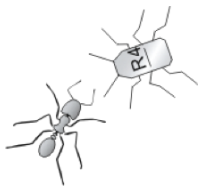
- Easier to express/program
- Threshold is adaptable like other weights



# Architectures

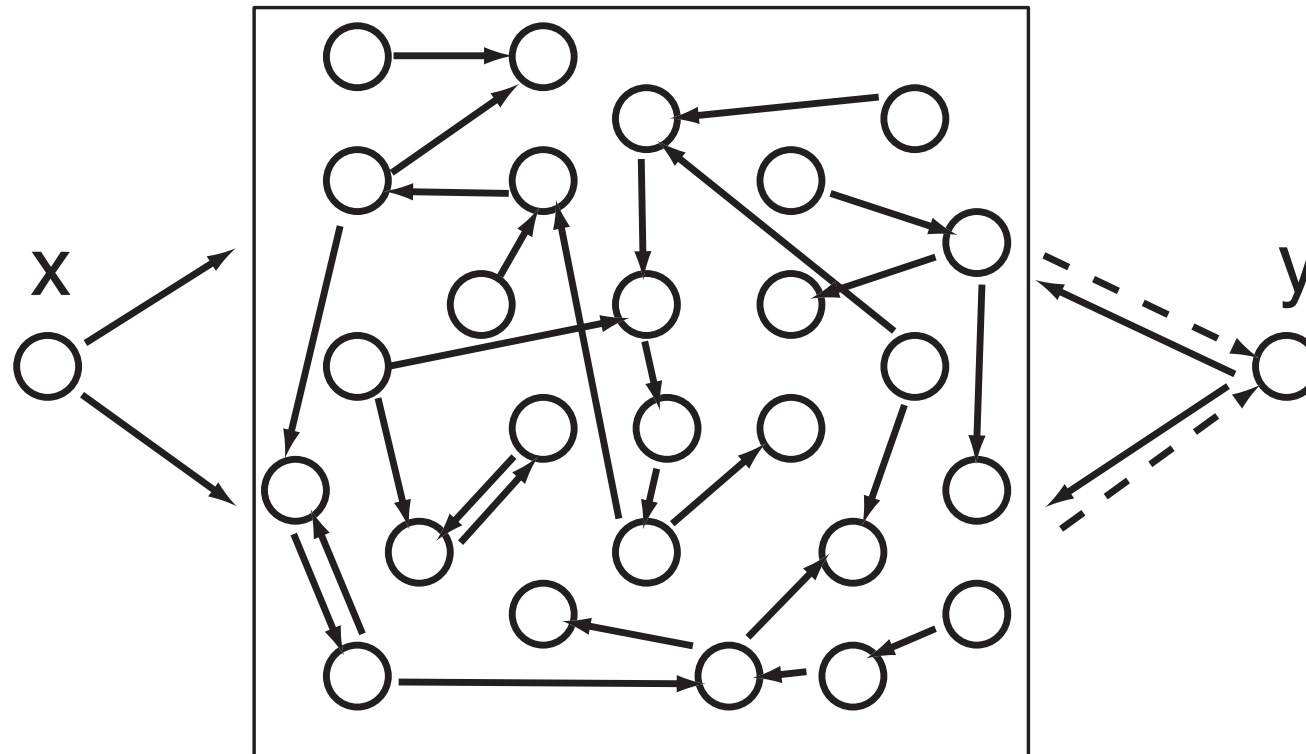


- a) feed-forward
- b) feedforward multilayer
- c, d) recurrent
- e) fully connected



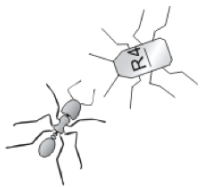
# Reservoir Architectures

Exploit rich dynamics in the reservoir of hundreds of randomly interconnected neurons with low connectivity (0.01, e.g)

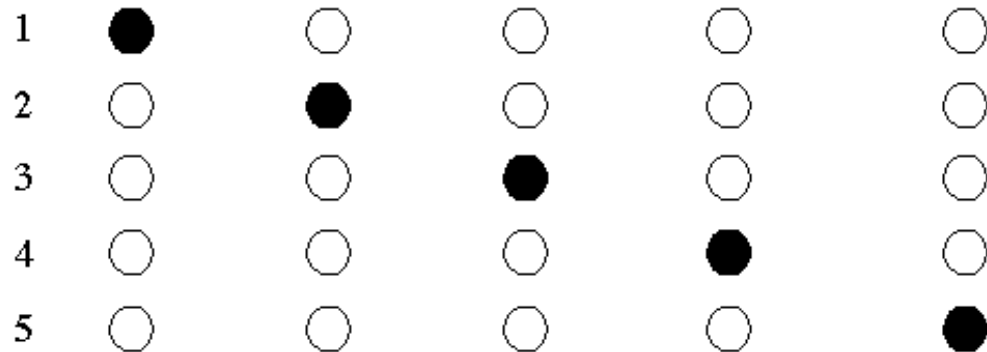


Liquid State Machines (Maas et al, 2002)

Echo State Networks (Jaeger et Haas, 2004)

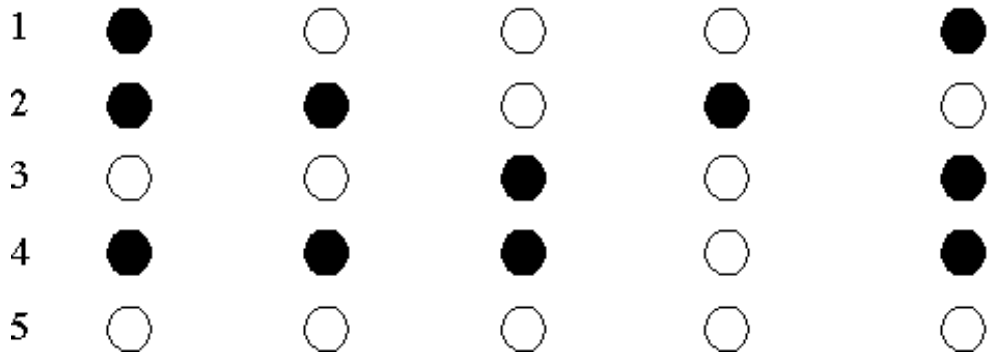


# Local vs Distributed Input Encoding



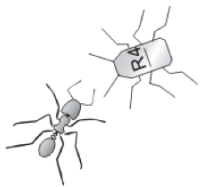
## LOCAL

- One neuron stands for one item
- Extremely sparse coding
- Grandmother cells
- Scalability problem
- Robustness problem



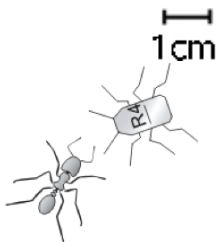
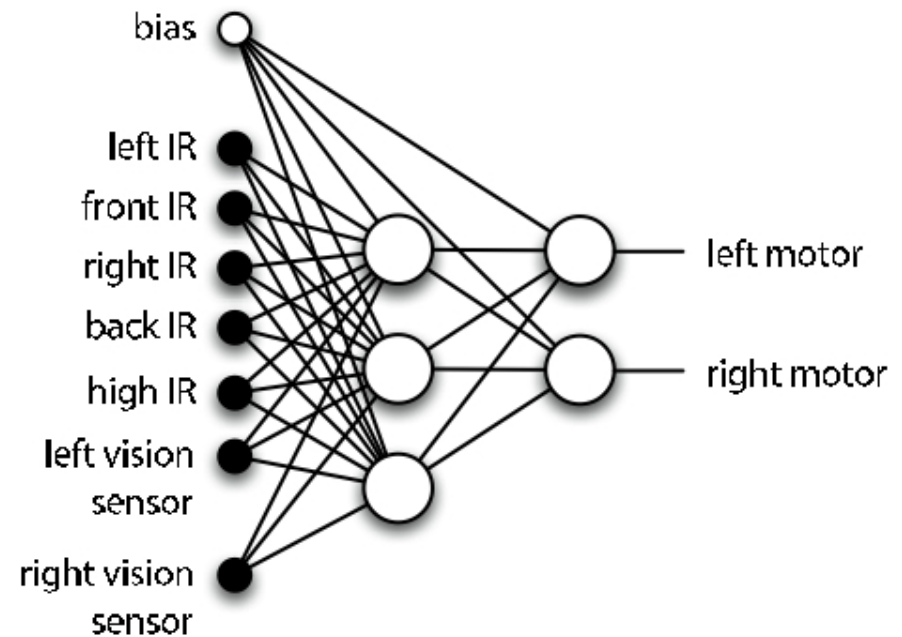
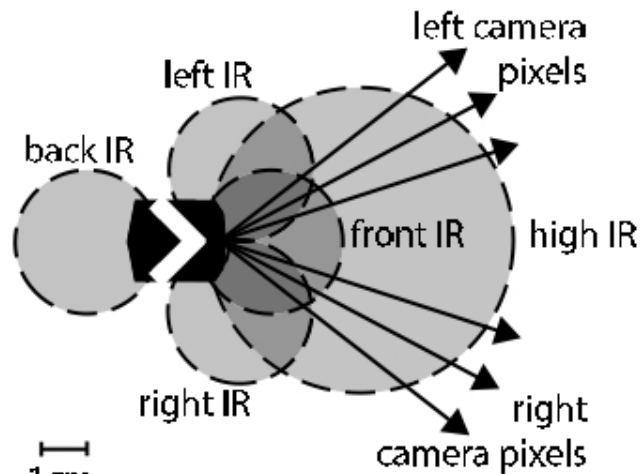
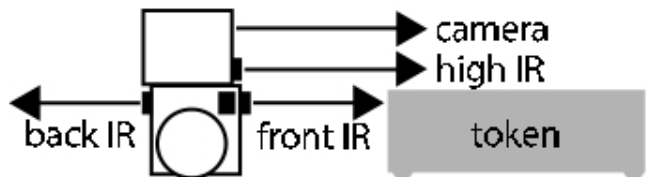
## DISTRIBUTED

- Neurons encode features
- One neuron may stand for >1 item
- One item may activate >1 neuron
- Robust to damage
- Sparsity can vary

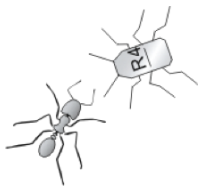
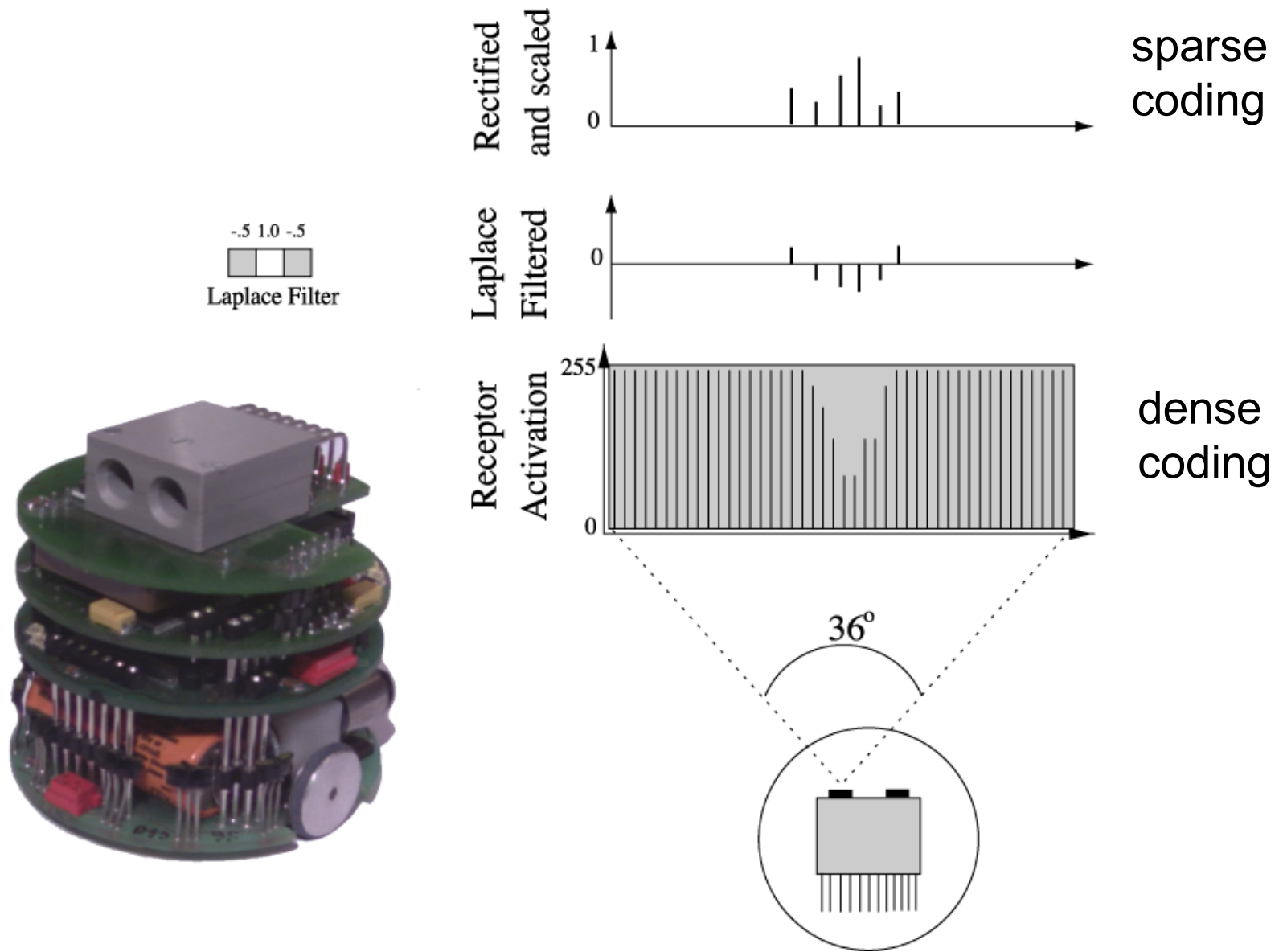


# Input Normalisation

$$x'_i = \frac{x_i}{\sqrt{\sum_{j=1}^N x_j^2}}$$

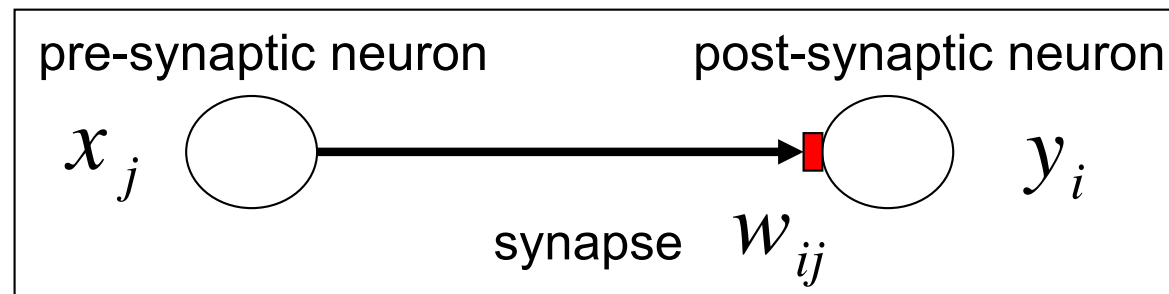


# Contrast Detection



# Learning

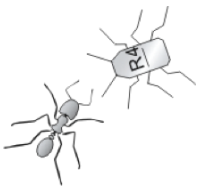
Learning is experience-dependent modification of connection weights



$$\Delta w_{ij} = x_j y_i$$

Hebb's rule (1949)

Learning is a gradual process and requires many input-output comparisons



# Learning cycle

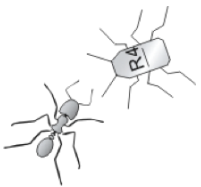
1. Initialize weights (e.g., random values from normal distribution)
2. Present randomly selected input pattern to network
3. Compute values of output units
4. Compute weight modifications
5. Update weights

*Standard weight update*

$$w_{ij}^t = w_{ij}^{t-1} + \eta \Delta w_{ij}$$

$\eta$   $\swarrow$   
*learning rate [0,1]*

6. Repeat from 2. until weights do not change anymore





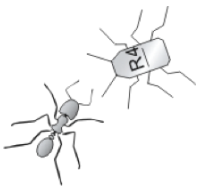
# *Learning modalities*

Unsupervised learning

Supervised learning

Reinforcement learning

Evolutionary (learning)



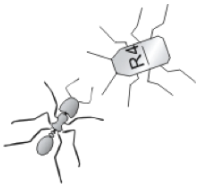
# Unsupervised learning

The weight change depends only on the activity of the pre-synaptic and of the postsynaptic neurons

$$\Delta w_{ij} = x_j y_i$$

Unsupervised learning is used for

- Detecting statistical features of the input distribution
- Information compression and reconstruction
- Discovery of topological relationships in the input data
- Memorization

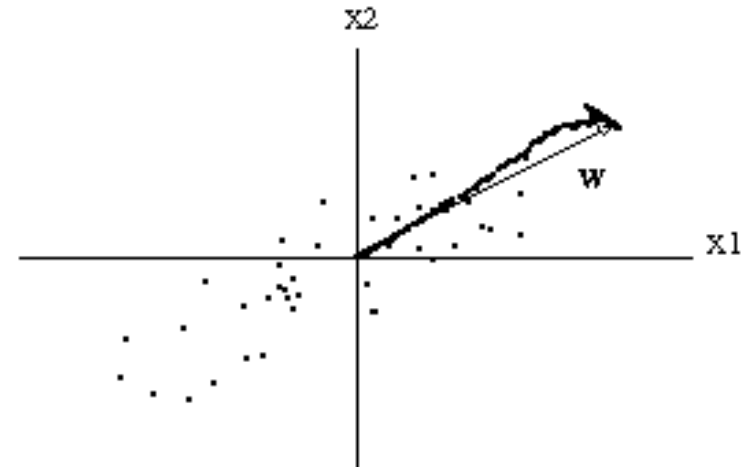
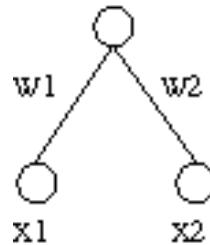


# Oja's learning rule

Hebb's rule suffers from **self-amplification** (unbounded growth of weights).  
Biological synapses cannot grow indefinitely

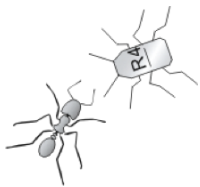
Oja (1982) introduced self-limiting growth factor in Hebb rule

$$\Delta w_j = \eta y (x_j - w_j y)$$



As a result, the weight vector develops along the direction of maximal variance of the input distribution.

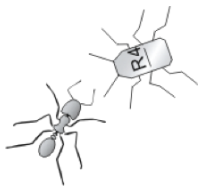
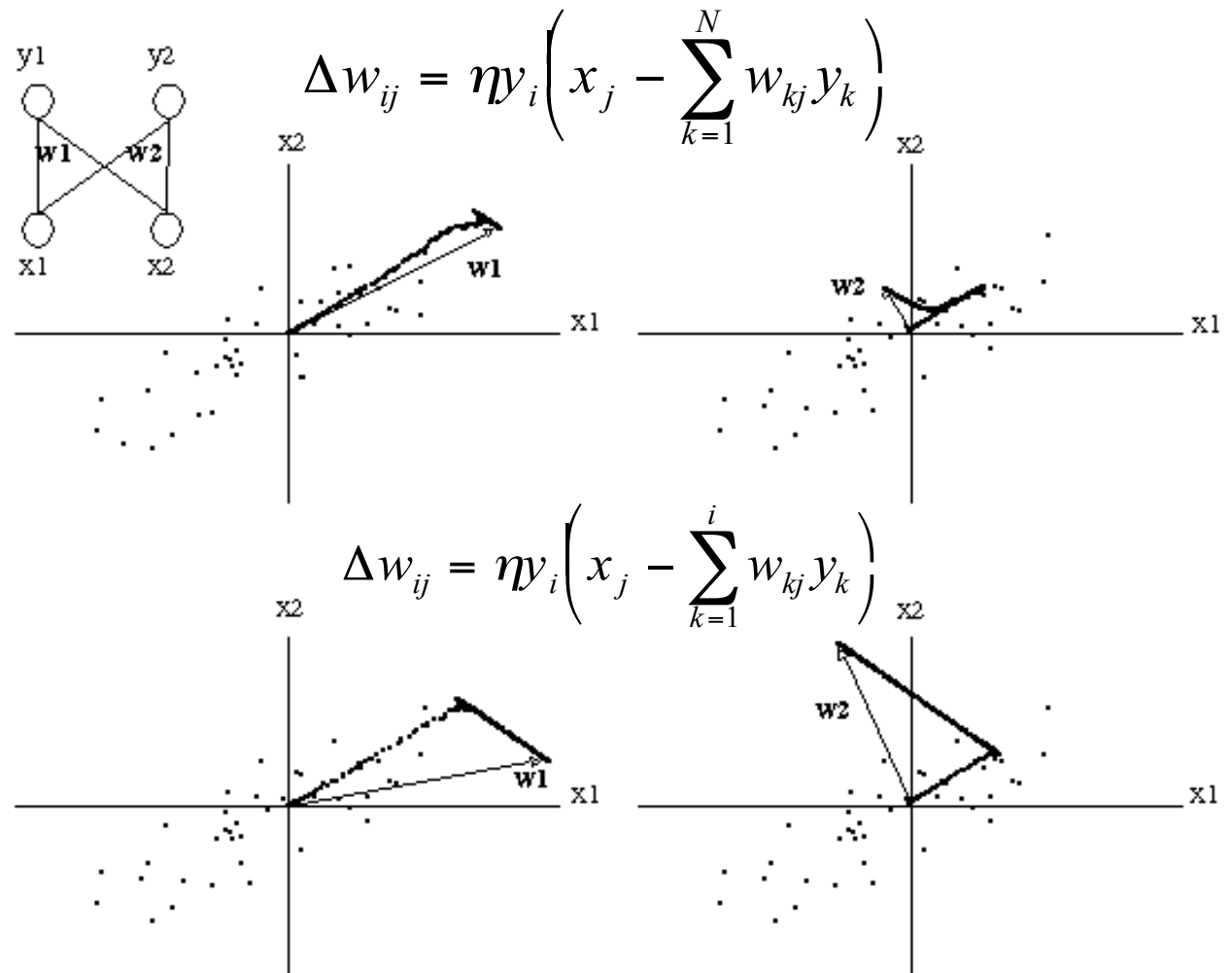
Neuron learns **how familiar** a new pattern is: input patterns that are closer to this vector elicit stronger response than patterns that are far away.



# Principal Component Analysis

**Oja rule** for N output units develops weights that span the sub-space of the N principal components of the input distribution.

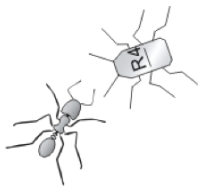
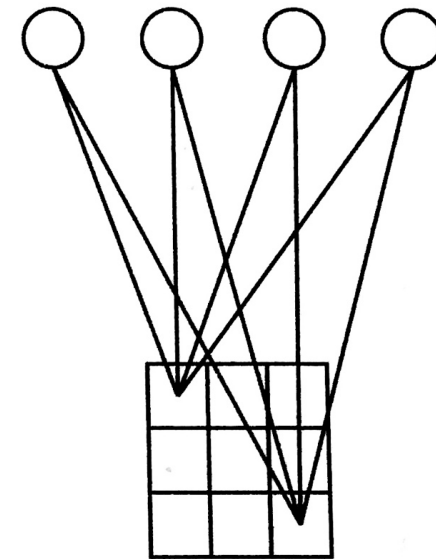
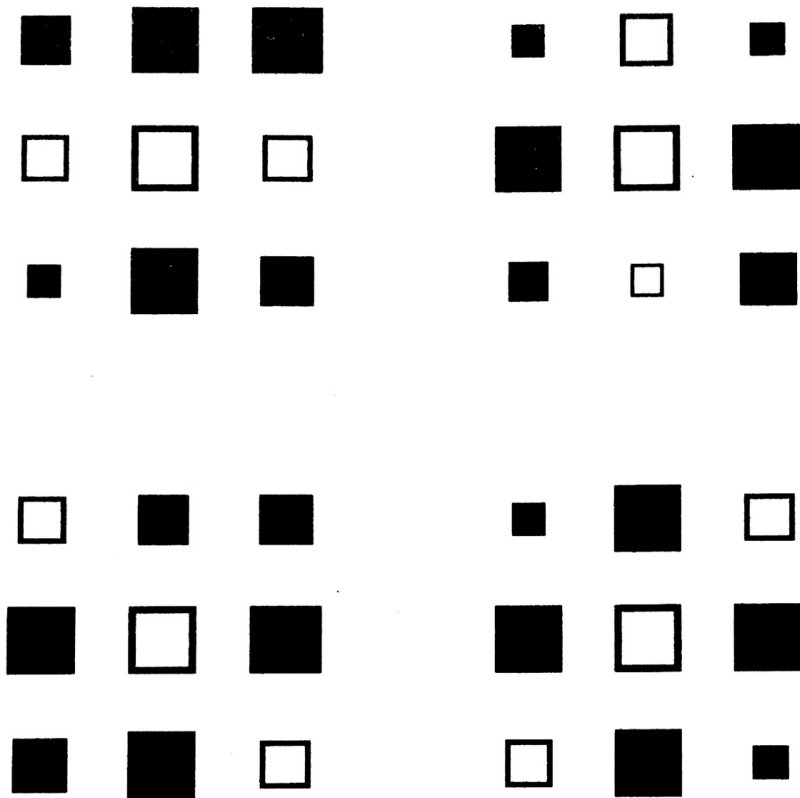
**Sanger rule** for N output units develops weights that correspond to the N principal components of the input distribution.



# Receptive Fields

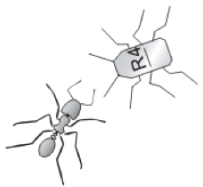
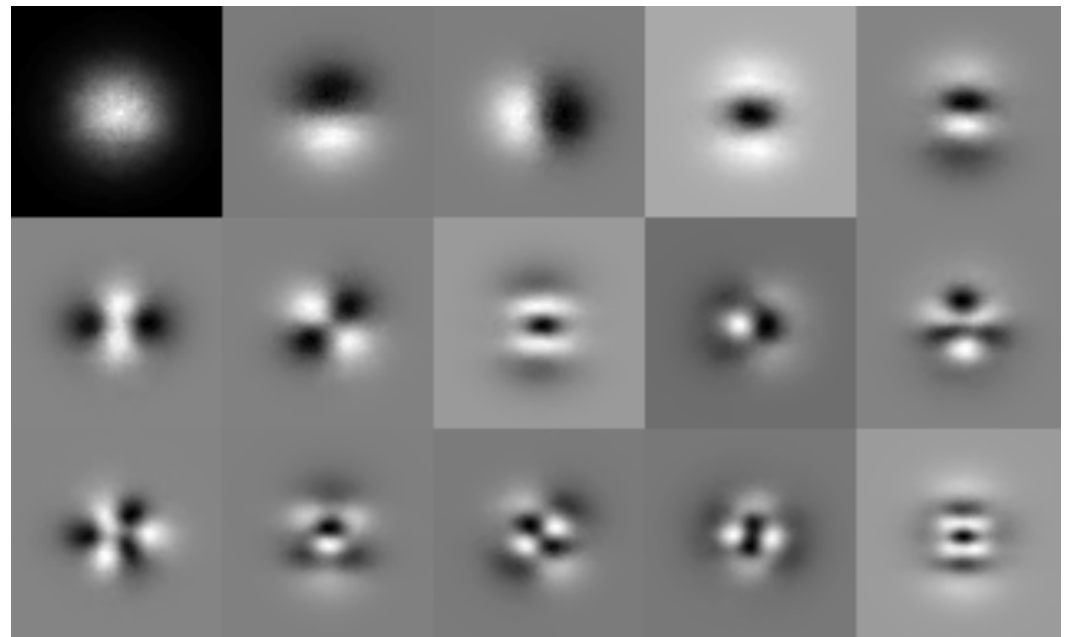
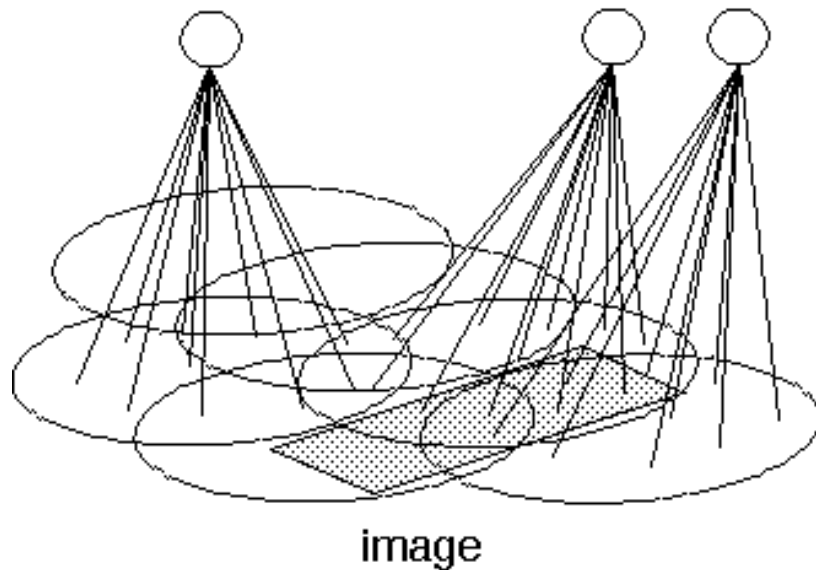
The **Receptive Field** indicates the input area subtended by a neuron *and* the input pattern that generates the strongest activation.

RF can be visualized by plotting the weight pattern in the input space.



# Do brains compute PCA?

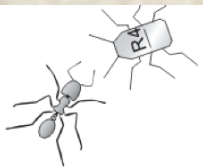
An Oja network with multiple output units exposed to a large set of natural images develops receptive fields similar to those found in the visual cortex of all mammals [Hancock et al., 1992]



Mammals are born with pre-formed hierarchically-organized feature detectors. But they never saw anything in the womb: how can it be?

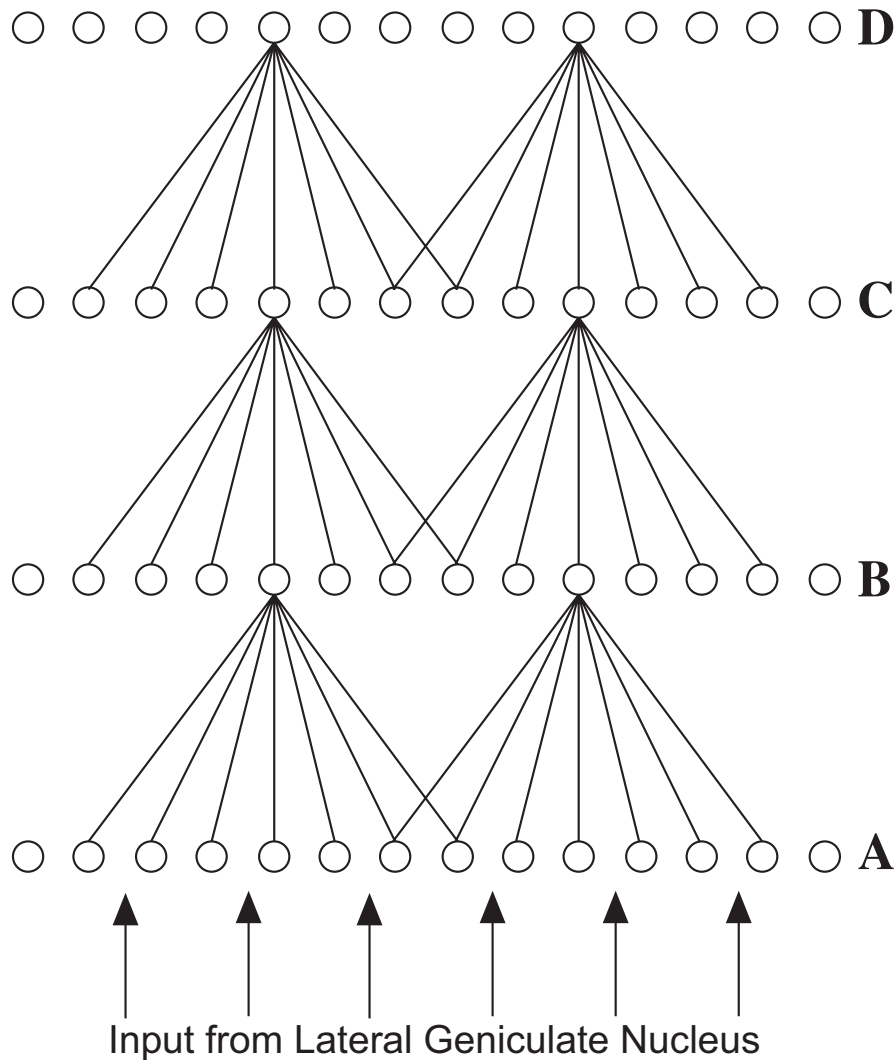


Image: Kelly Frankenburg



# Multilayer Feature Detection

Linsker (1986)

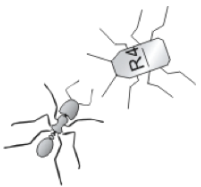


Topologically restricted connectivity

Linear activation function

Plain Hebbian learning with weight clipping at  $w_+$  and  $w_-$

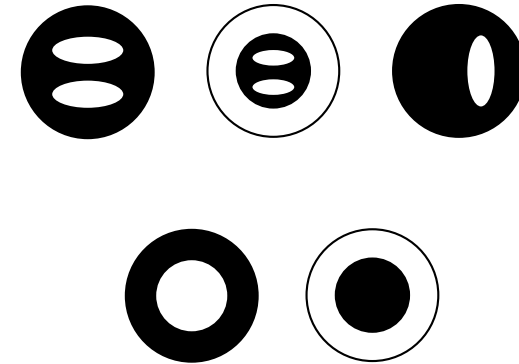
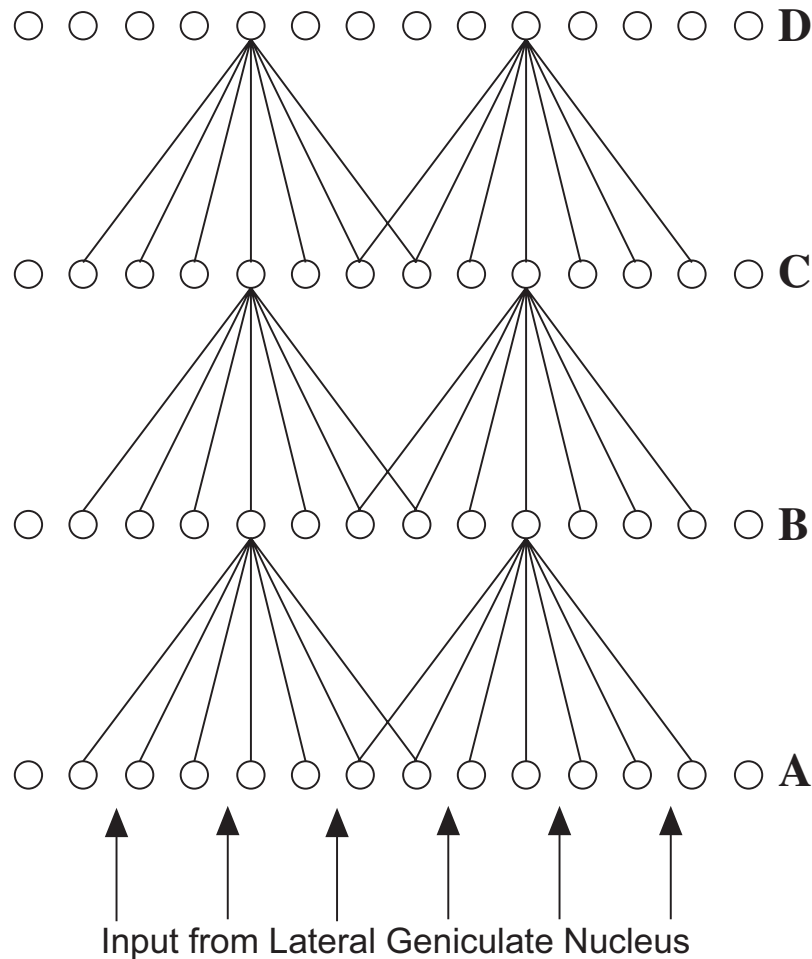
Learn one layer at a time, starting from lower layer





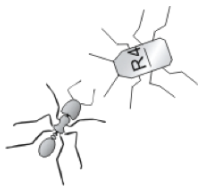
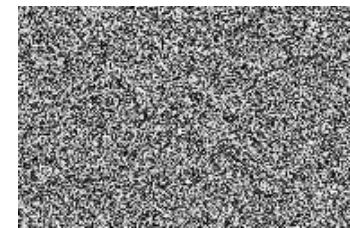
# Emerging Receptive Fields

Linsker (1986)



Average luminosity in RF

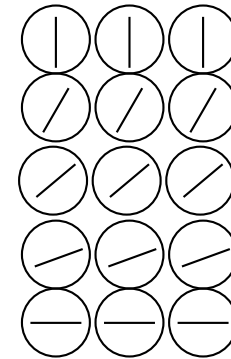
+++++



# Sensory maps

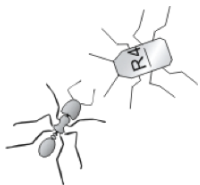
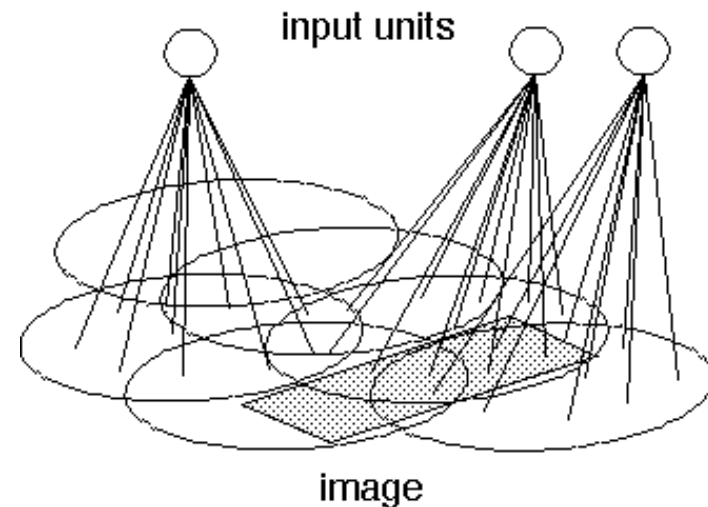
Neighbouring neurons respond to similar patterns with gradual transitions

The visual cortex is organized in specialized modules. Each module is composed by a series of columns of neurons. Neurons respond to bars of different orientation

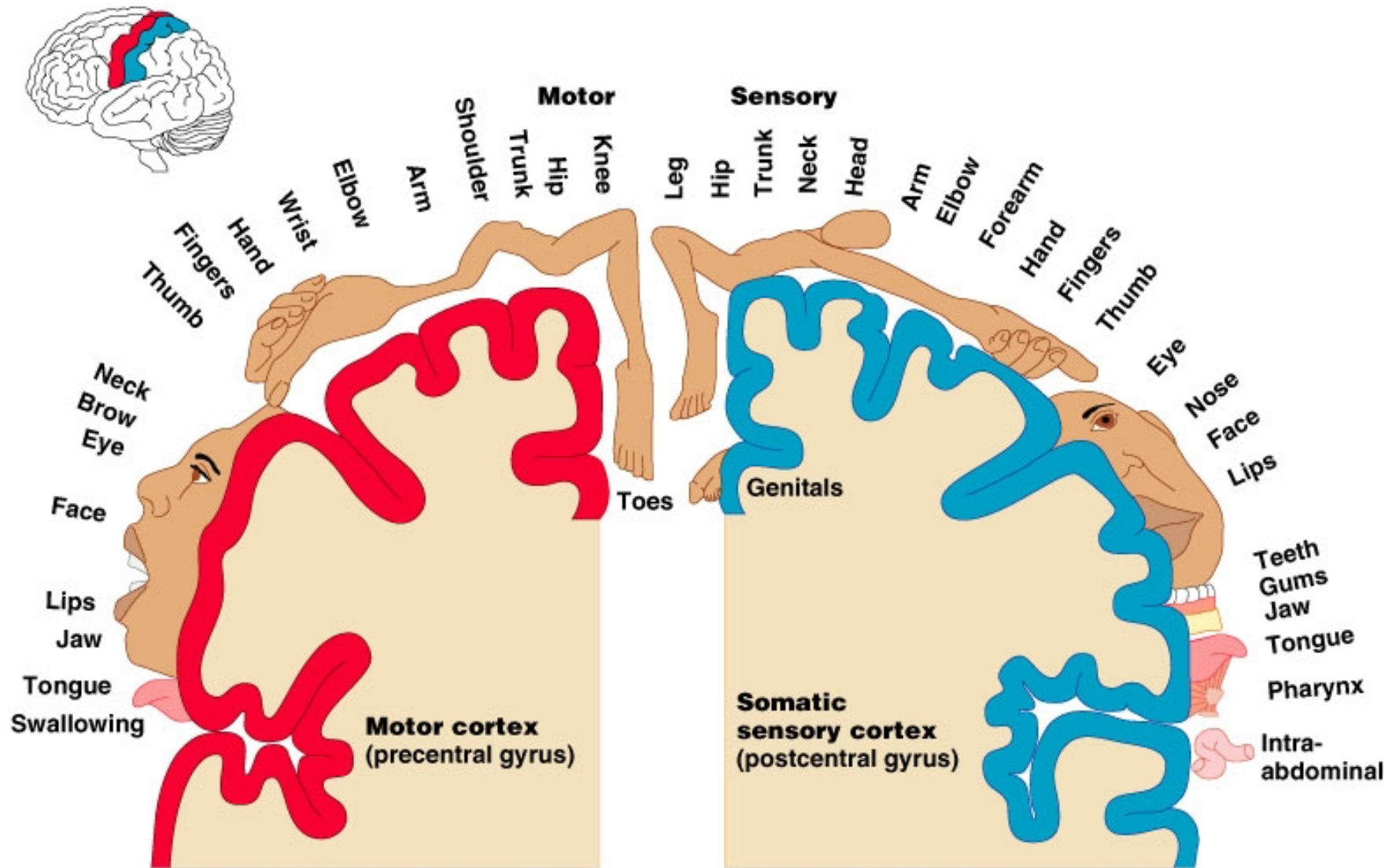


1. The bar orientation gradually varies along the column.
2. Neighbouring columns correspond to neighbouring areas of the retina (**retinotopic maps**).

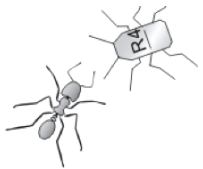
A similar structure exists in the auditory cortex (**tonotopic maps**).



# Sensory-Motor Body Map



Copyright © 2004 Pearson Education, Inc., publishing as Benjamin Cummings.



Companion slides for the book *Bio-Inspired Artificial Intelligence: Theories, Methods, and Technologies* by Dario Floreano and Claudio Mattiussi, MIT Press

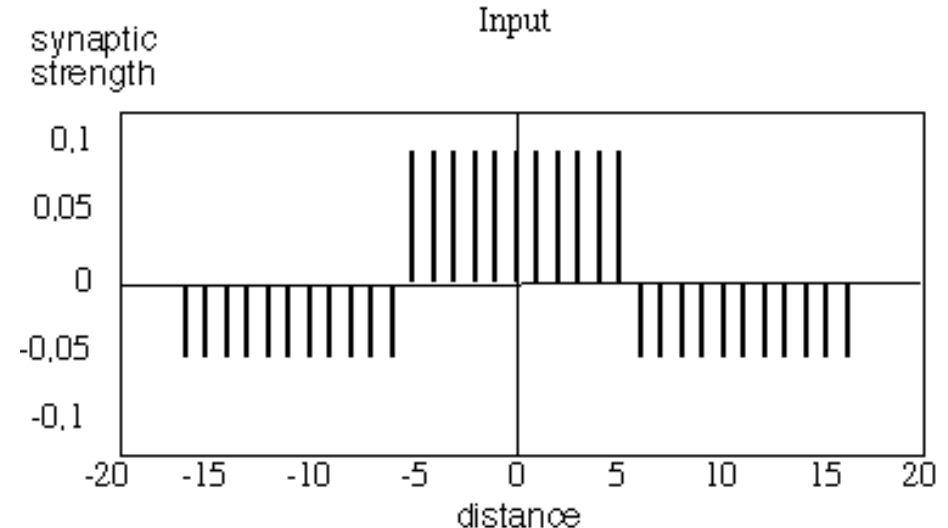
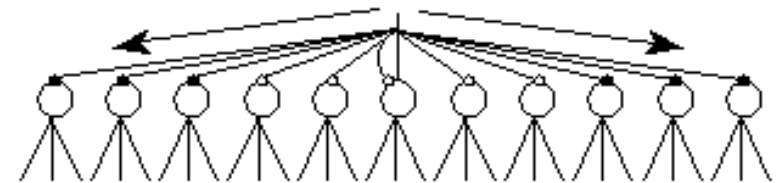
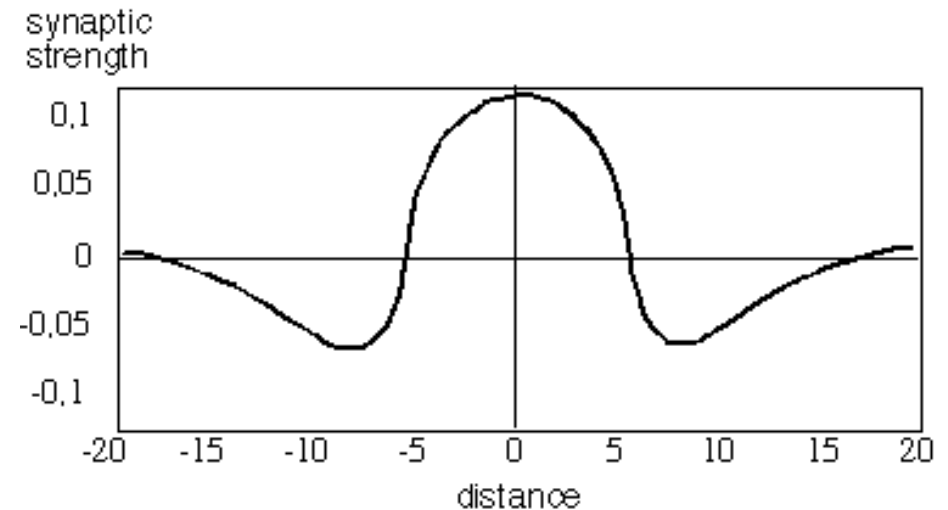
# Lateral cortical connections

Cortical neurons display the following pattern of *projective* connectivity:

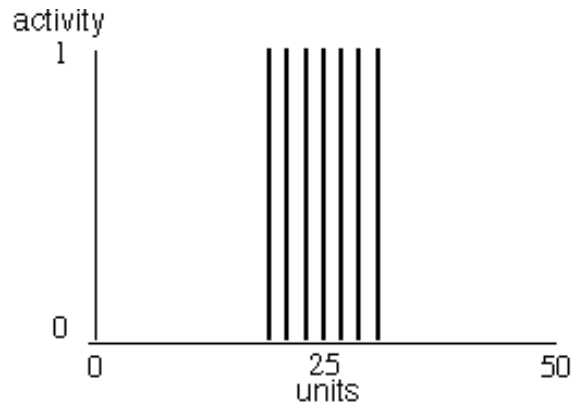
- up to 50-100  $\mu\text{m}$  radius = excitatory
- up to 200-500  $\mu\text{m}$  radius = inhibitory
- up to few cm radius = slightly excitatory

It resembles to a *Mexican Hat*

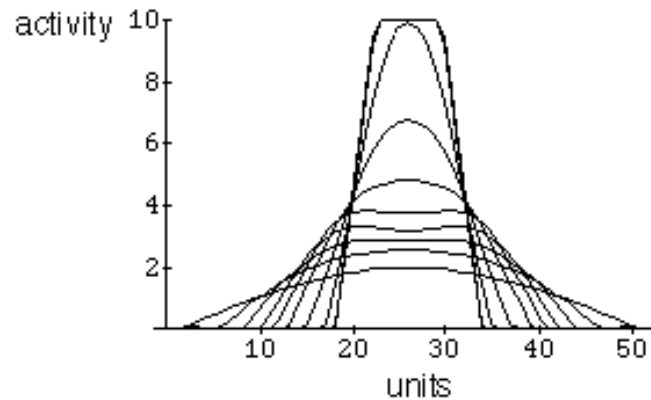
In a neural network, we can approximate the Mexican hat to a bipolar weight distribution.



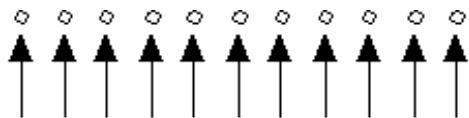
# Neural bubble formation



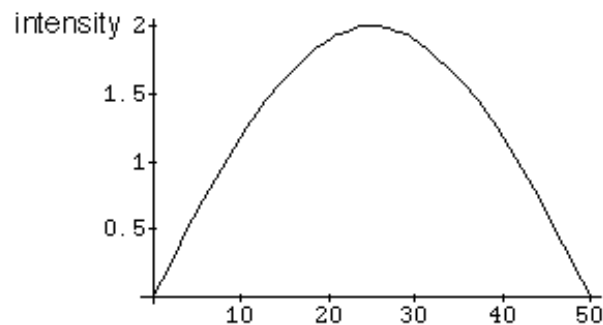
Simplification: directly set output of unit with highest activation and its  $n$  neighbors to 1, and all other units to 0



Gradual emergence of bubble centered around unit with strongest activation



Laterally connected neurons



Input pattern

# Self-Organizing Maps

Kohonen (1982)

Let's apply Hebb rule to layer of such laterally connected neurons

$$y_i = \Phi(A_i) = \begin{cases} 1 & \text{if within neighbourhood } \Psi(y) \\ 0 & \text{otherwise} \end{cases}$$

$$\Delta w_{ij} = \eta y_i (x_j - \Psi(y_i) w_{ij}) \qquad \Psi(y_i) = \begin{cases} \psi & \text{if } y_i = 1 \\ 0 & \text{if } y_i = 0 \end{cases}$$

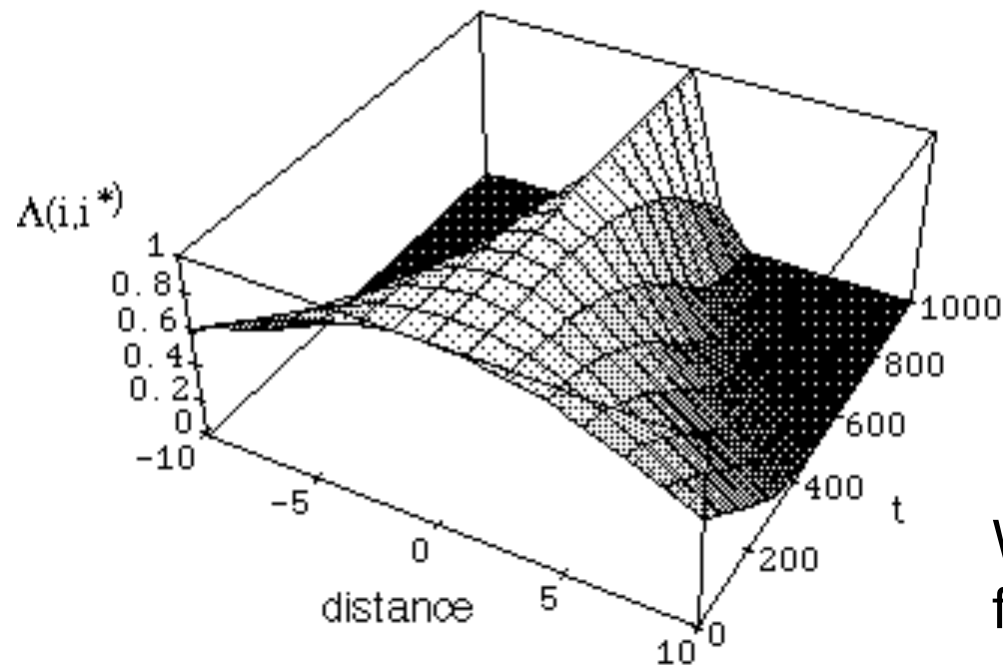
If we set  $\Psi(y_i)$  equal to the learning rate  $\eta$ , then the learning rule becomes:

$$\Delta w_{ij} = \begin{cases} \eta(x_j - w_{ij}) & \text{if } y_i = 1 \\ 0 & \text{if } y_i = 0 \end{cases} \quad \text{and} \quad \mathbf{w}_i^{t+1} = \begin{cases} \mathbf{w}_i^t + \eta(\mathbf{x} - \mathbf{w}_i^t) & \text{if } y_i = 1 \\ \mathbf{w}_i^t & \text{if } y_i = 0 \end{cases}$$

1. The weights are changed only for the neurons that are geographically near the neuron with the highest activity,
2. The change moves the weight vector towards the input pattern.

# Neighborhood function

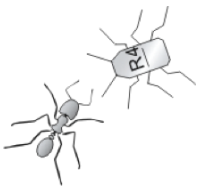
The neighbourhood size  $\Psi(y)$  is a critical aspect of map self-organization. It should be large at the beginning of training to give a chance to all neurons to change weights and gradually shrink



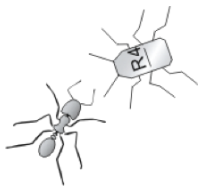
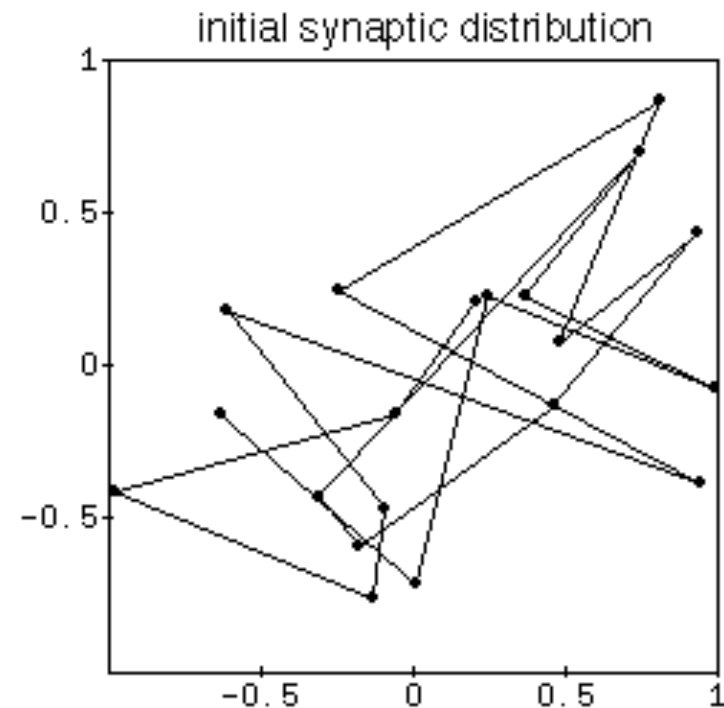
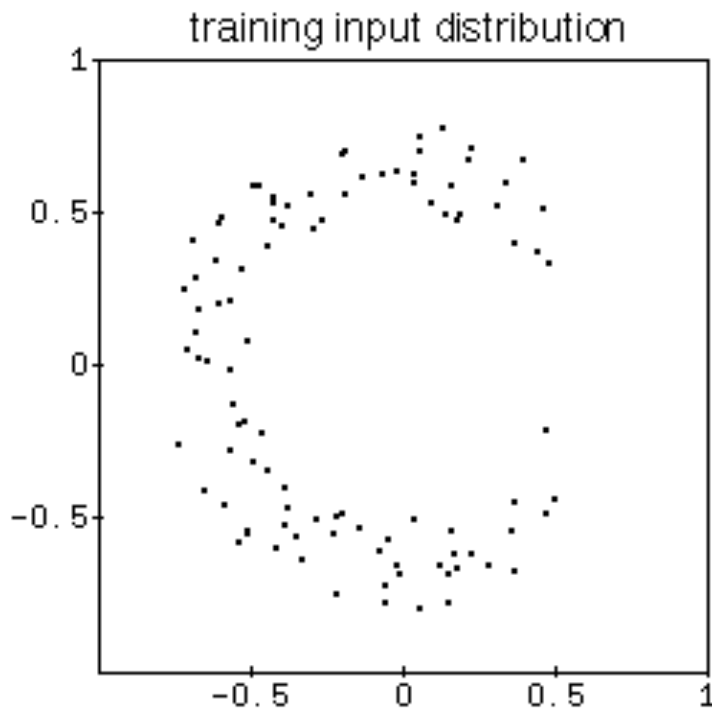
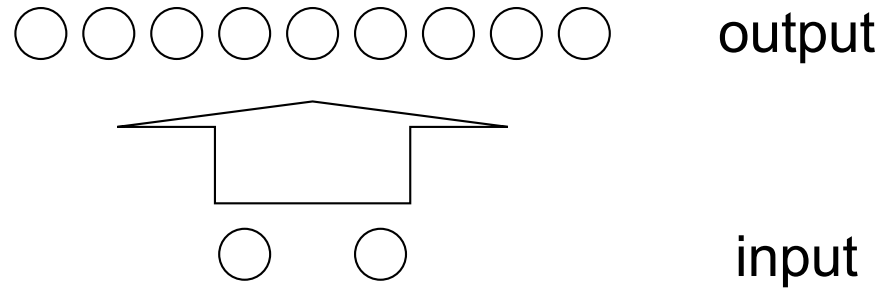
$$\Lambda(i, i^*) = \begin{cases} 1 & \text{if } \|\mathbf{c}_i - \mathbf{c}_{i^*}\| \leq r \\ 0 & \text{otherwise} \end{cases}$$

We can incorporate the neighborhood function in the SOM learning rule

$$\Delta w_{ij} = \eta \Lambda(i, i^*) (x_j - w_{ij})$$



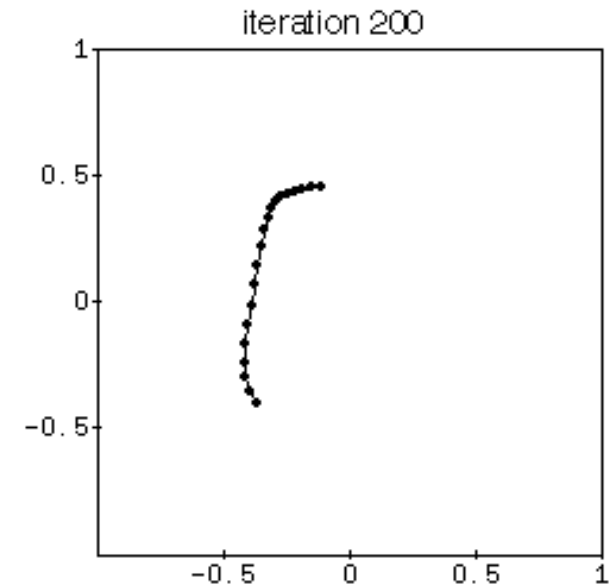
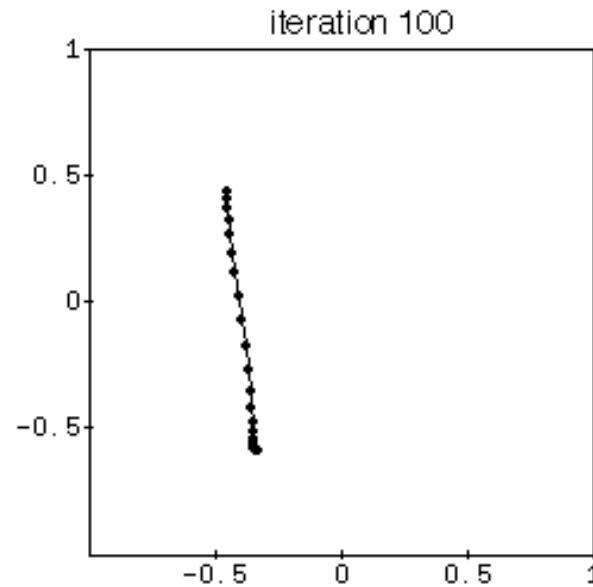
# Example of self-organizing map



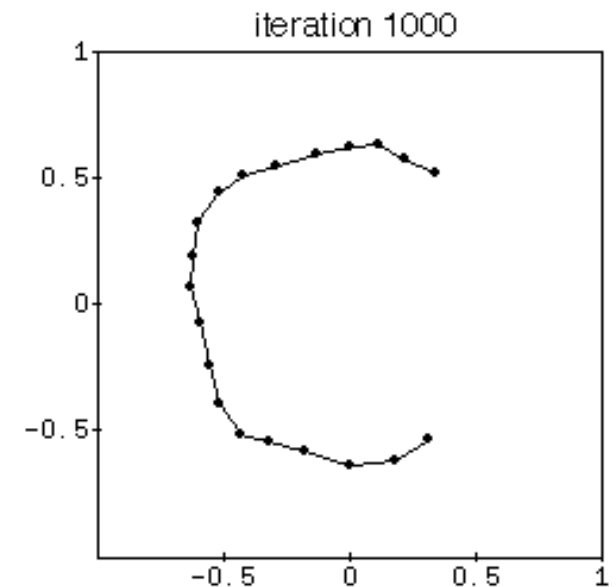
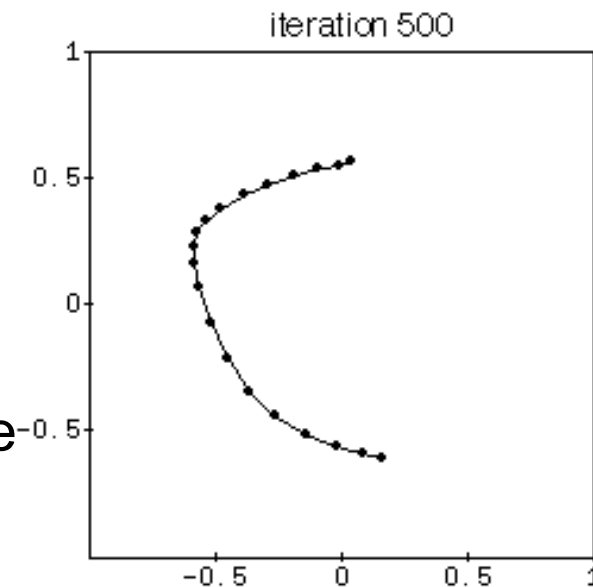


# Self-organization phases

Ordering phase:  
Fast  
Neighborhood change



Convergence phase:  
Slow  
No neighborhood change



# *The phonetic typewriter*

The phonetic typewriter transform a spoken text into written text.  
Output layer provides a compact representation of speech.  
Topological representations helps discrimination of similar phonemes.  
It requires manual labeling and articulation rules

