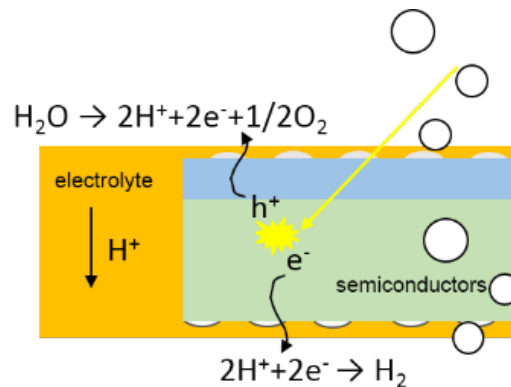


## Renewable Energy: Exercise 11 (Solar fuels)

This exercise deals with assessment of solar fuels generation. In the first part, the production of hydrogen by photoelectrochemical water-splitting is investigated. In the second part, you use solar thermochemical route for the production of synthesis gas used in a fuel cell.

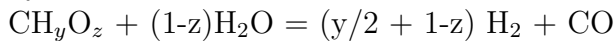
- The schematic of a photoelectrochemical cell is shown in figure 1.



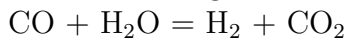
**Figure 1:** Schematic of the photoelectrochemical water splitting device

- The photoabsorber is a dual absorber made of Si (band gap 1.1 eV) and GaAs (band gap 1.4 eV). Which of the two cells (Si or GaAs) will you put on top of your device?
- Calculate the fraction of incident light which is ideally absorbed in both cells.
- Assume that the resulting cell performance can be calculated by
 
$$i = i_0 - i_1 \cdot \left( e^{\frac{qV}{nk_B T}} - 1 \right)$$
 with  $i_0 = 115 \text{ A/m}^2$ ,  $i_1 = 3 \cdot 10^{-33} \text{ A/m}^2$ ,  $n = 1$   
 Determine the short circuit current and open circuit voltage. What is the fill factor of this dual absorber cell?
- Assume that the load curve of the integrated electrochemical cell can be calculated by
 
$$V = V_0 + i\rho l_p + a_1 \log\left(\frac{i}{i_{0a}}\right) + a_2 \log\left(\frac{i}{i_{0c}}\right)$$
 with  $V_0 = 1.23 \text{ V}$ ,  $\rho = 0.05 \text{ } \Omega\text{m}$ ,  $l_p = 8 \text{ mm}$ ,  $a_1 = 0.035 \text{ V/dec}$ ,  $i_{0a} = 0.00001 \text{ A/m}^2$ ,  $a_2 = 0.03 \text{ V/dec}$ ,  $i_{0c} = 1 \text{ A/m}^2$ ,  $T = 300 \text{ K}$   
 Describe the meaning of the four terms on the right hand side and calculate the overpotentials at a current density  $i = 200 \text{ A/m}^2$ .
- Plot the two curves (i.e. for both PV and electrochemical cell) in a V-i-plot (x-axis: V, y-axis: i) and read the operating potential and current density. Is it operating at the maximum power point? How could we operate more close to the maximum power point?

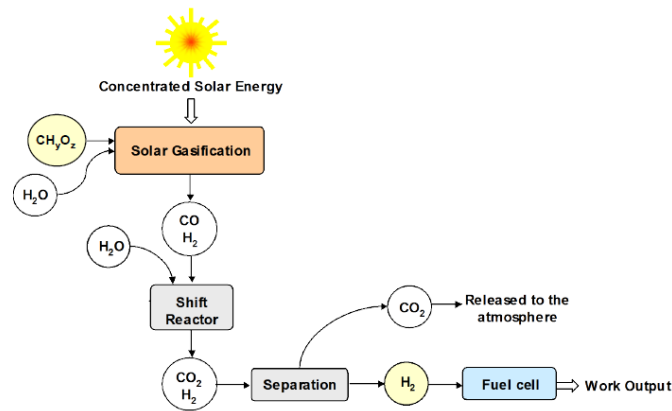
- (f) What is the efficiency of the cell, assuming an irradiation of  $1000 \text{ W/m}^2$ ?
- (g) Calculate how much hydrogen is produced per year and area assuming a continuous operation at the operating point for 1900 hours (high heating value of  $\text{H}_2 = 141 \text{ MJ/kg}$ ).
2. The solar steam-gasification of carbonaceous material for syngas production is represented by the net stoichiometric reaction:



Each mole of CO in the syngas is further water gas-shifted to generate an additional mole of  $\text{H}_2$  according to:



The  $\text{H}_2/\text{CO}_2$  mixture undergoes separation to  $\text{H}_2$  and  $\text{CO}_2$ .  $\text{H}_2$  produced is fed to a  $\text{H}_2/\text{O}_2$  fuel cell, while  $\text{CO}_2$  produced is released to the atmosphere. The process is schematically depicted in Fig. 2. The selected carbonaceous feedstock is wood, of elemental composition: 49 wt% C, 6 wt% H, and 45 wt% O.



**Figure 2:** Schematic representation of the solar gasification process for  $\text{H}_2$  generation

Assumptions:

- Solar reactor is a perfectly insulated blackbody cavity-receiver; only radiation losses are considered.
- Reactor operating temperature,  $T_{reactor} = 1200 \text{ K}$ .
- Mean solar flux concentration ratio,  $C = 1800 \text{ suns}$ .
- Normal beam insolation,  $I = 1 \text{ kW/m}^2$ .
- Mass flow rate of  $\text{CH}_y\text{O}_z$ ,  $\dot{n}_{\text{CH}_y\text{O}_z} = 1 \text{ mol/s}$ .

- The net power absorbed by the solar reactor matches the enthalpy change per unit time of the reaction  $\dot{Q}_{Reactor,net} = \dot{n}_{CH_yO_z} \cdot \Delta H = 210 \text{ kW}$ .
  - The water-gas shift reaction is carried out in an auto-thermal reactor.
  - The  $H_2/CO_2$  separation unit is based on the pressure swing adsorption technique (PSA) at 94% recovery rate.
  - The  $H_2/O_2$  fuel cell operates with a conversion efficiency of 62% of the high heating value of  $H_2$ .
  - Heating value of carbonaceous feedstock,  $HV_{CH_yO_z} = 570 \text{ kJ/mol}$ .
  - High heating value of  $H_2$ ,  $HV_{H_2} = 285 \text{ kJ/mol}$ .
- (a) Calculate  $y$  and  $z$  using the elemental composition of the carbonaceous feedstock. Calculate the number of moles of  $H_2$  and  $CO_2$  ideally produced for a mole of  $CH_yO_z$  gasified.
- Hint:  $\gamma_i = \frac{\nu_i/M_i}{\sum_n \nu_n/M_n}$ , with  $\gamma$  molar fraction,  $\nu$  weight fraction, and  $M$  molar mass of species  $i$ .
- (b) Calculate the absorption efficiency of the solar reactor,  $\eta_{absorption}$ .
- (c) Calculate solar power input,  $\dot{Q}_{solar}$ .
- (d) Calculate the electric power output of the  $H_2/O_2$  fuel cell,  $\dot{W}_{out}$ .
- (e) Calculate the Energy Gain Factor (EGF), defined as the ratio of the electric output of the solar process to that obtained when using the same amount of  $C$  as a combustion fuel in a 40% efficient Rankine cycle.
- (f) Calculate the specific  $CO_2$  emissions, in units of  $kg \text{ CO}_2/kWh_e$ , for the solar process and for the 40% efficient Rankine cycle.