

# Environmental Bioprocess Engineering

## Assignment #2 (A.2.1 & A.2.2)

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Don't remain alone and stuck if you don't understand a step and if you have difficulties with the problem.

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**This assignment is the study of the biodegradation of organic pollution by heterotrophic biomass under aerobic conditions. The following aspects will be studied**

- **Microbial growth kinetics and yields with kinetics parameters (A.2.1)**
- **Analytical determination of the bioprocess (chemostat) behavior (Steady state study) (A.2.2)**
- **Dynamic simulation of the bioprocess, modeling (Simplified ASM approach) and simulation (Aqasim) (A.2.3)**

For A.2.1 and A.2.2., you will provide an Excel file and its PDF version.

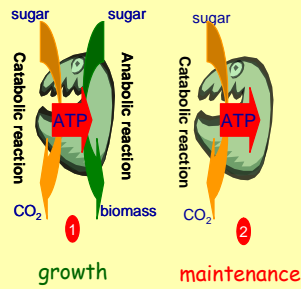
### A.2.1. Stoichiometry and kinetics of microbial growth study (in 1 Excel sheet)

One considers the study of the microbial aerobic heterotrophic growth of biomass on acetate with  $\text{NH}_4^+$  as N-Source at atmospheric pressure and  $25^\circ\text{C}$ .

Available acetate stock is in the form sodium acetate  $\text{CH}_3\text{COONa}$  with an  $\Delta_f^{01}$  of  $-369.41 \text{ kJ}\cdot\text{mol}^{-1}$  ( $\equiv$  Acetate)

- a. (4) Using the required Gibbs Energy of heterotrophic growth  $Y_{\text{GX}}^{\text{max}}$  correlation, compute and provide the global growth reaction. Then provide all  $Y_{\text{IX}}^{\text{max}}$  stoichiometric coefficients of global growth reaction...  
You will see that the growth will produce protons and bicarbonate ions ( $\text{H}^+$  and  $\text{HCO}_3^-$ ). According the stoichiometry of the growth reaction, is the bioprocess alkalizing or acidifying?
- b. (2) Establish the catabolic reaction, which gives the  $\Delta G_{\text{cat}}$  of the catabolic reaction.
- c. (2) Establish the anabolic reaction.
- d. (3) Check that the global reaction is the sum of the anabolic and the catabolic respiration of the growth (using  $1/Y_{\text{OX}}$  stoichiometric yield) of global growth reaction)
- e. (3) Using the Gibbs Energy correlations:
  - compute the maximal specific growth rate  $\mu^{\text{max}}$
  - and from Gibbs Energy  $m_G$  correlation, provide the rates  $m_i$  required for the maintenance
- f. (4) Express all specific rates  $q_i$  (biomass, Acetate,  $\text{O}_2$ ,  $\text{NH}_4^+$ ,  $\text{H}^+$ ...) and yields  $Y_{\text{IX}}$  as function of growth rate  $\mu$   
Provide a double Y scatter plot of the  $q_i$  rates and the yields  $Y_{\text{IX}}$  vs  $\mu$  [ $0 - 1.2 \mu^{\text{max}}$ ]

### A.2.1.



$$-\frac{1}{Y_{Gx}^{\max}} \text{elec donor} - (\dots) N_{\text{source}} - \frac{1}{Y_{Ax}^{\max}} \text{elec acceptor} + 1 \text{Cmol biomass} + (\dots) H_2O + (\dots) HCO_3^- + (\dots) H^+ + \frac{1}{Y_{Gx}^{\max}} \text{heat} + \frac{1}{Y_{Gx}^{\max}} \text{Gibbs energy}$$

$$-q_s = \frac{1}{Y_{SX}^{\max}} \mu + m_s \quad -q_s = q_s^{\max} \frac{C_s}{K_s + C_s}$$

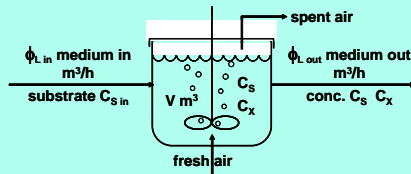
$$\frac{1}{Y_{Gx}^{\max}} = 200 + 18 \cdot (6 - C)^{1.8} + \exp\left[\frac{(3.8 - \gamma)^2}{(3.6 + 0.4C)}\right]$$

$$\mu^{\max} = \left(\frac{3 \cdot (-\Delta G_{\text{cat}})}{Y_D} - 4.5\right) \cdot Y_{Gx}^{\max} \exp\left(\frac{-20000}{R} \left(\frac{1}{T} - \frac{1}{298}\right)\right)$$

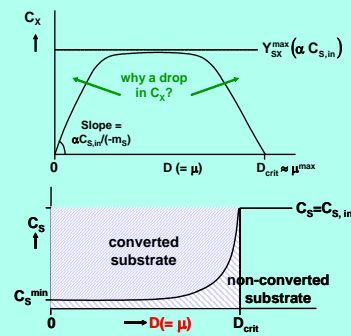
All specific rate  $q_i$  and yield  $Y_{ij}$  with  $Y_{SX}^{\max}$ ,  $m_s$ ,  $\mu^{\max}$ ,  $K_s$  4 models parameters

### A.2.2.

#### Chemostat (steady state) mass balance

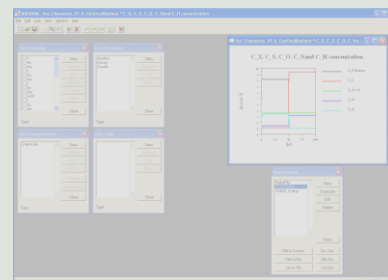


$$\frac{d(V C_X)}{dt} = Q_{L,in} C_{X,in} - Q_{L,out} C_X + r_X V$$



### A.2.3.

		Continuity				
Component	$i$	1	2	3	Process Rate, $r_i$ [ML <sup>-3</sup> T <sup>-1</sup> ]	
$j$ Process	↓	$X_a$	$S_b$	$S_c$		
1 Growth	1		$-\frac{1}{Y}$	$-\frac{1-Y}{Y}$	$\frac{\mu S_b}{K_s + S_b} X_a$	
2 Decay	-1			-1	$\delta X_a$	
Observed Conversion Rates	ML <sup>-3</sup> T <sup>-1</sup>	$r_i = \sum r_{ij} = \sum r_{ji} \theta_j$			Kinetic Parameters:	
Stoichiometric Parameters:					Maximum specific growth rate: $\mu$	
True growth yield: $Y$		Biomass [M(COD) L <sup>-3</sup> ]	Substrate [M(COD) L <sup>-3</sup> ]	Oxygen (negative COD) [M(COD) L <sup>-3</sup> ]	Half-velocity constant: $K_s$	
					Specific decay rate: $\delta$	



### A.2.2. Reactor study (Steady state) (in 1 Excel Sheet)

According this previous A.2.1, one wants to do an experiment to study this growth biosystem to determine its biological kinetic parameters. For this purpose, a 1.5 L of CSTR chemostat bioreactor will be used. Assume an inlet organic loading concentration of  $C_{S,in}$  1500 mg COD/L. Suppose  $K_s$  the affinity constant of the biomass for this substrate is 20 mg COD/L

- (1) As A.2.1. Stoichiometry and kinetics of microbial growth study is developed and expressed in C-mole of biomass and mole of sodium acetate, convert units of  $C_{S,in}$  and  $K_s$ .
- (5) Provide the expression of putative concentrations of Biomass  $C_X$ , Substrate  $C_S$  as function of dilution rate  $D$  (use Chemostat lecture notes)

- Build mass balance for Biomass  $C_X$ , Substrate  $C_S$  state variables, provide volumetric rates

- From two known expressions of  $q_s$  (Herbert-Pirt and hyperbolic link  $q_s$  to  $\mu$  and  $C_s$  provide.

- expression for  $C_s = f(D)$  which doesn't depend on  $C_{s,in}$  inlet concentration
- expression for  $C_x = f(C_s)$
- expression  $\mu = f(C_s)$  using minimal substrate concentration (for maintenance)  $C_{s,min}$  which occurs when  $\mu=0$ , but when residual  $C_s$  allows biomass maintenance (see lecture on Chemostat).

- c. (2) From  $\mu = f(C_s)$  expression, give and compute the maximum critical dilution rate and determine  $D_{crit}$ , which occurs when  $C_s=C_{s,in}$ ...

Compute  $C_{s,min}$  of minimal residual substrate concentration for maintenance

- d. (4) Then, from  $C_s$  mass balance  $r_s=q_s.C_x$ , using observed  $Y_{sx}$  yield ( $q_x/q_s$  rate ratio) or using one of the  $q_s$  expression, give 3 expression of
- $C_x = f(C_s, Y_{sx}, D)$
  - $C_x = f(D, C_s)$  Herbert Pirt  $q_s$
  - $C_x = f(D, C_s)$  Hyperbolic  $q_s$

Then with expressions of  $C_x = f(\mu) = f(D)$  and  $C_s = f(\mu) = f(D)$  from [0 to  $D_{crit}$ ] in 30 steps compute  $C_s$  and  $C_x$  (also all  $q_i$  for all global growth components)

Check same calculated for  $C_s$  by the 3 expressions

Plot them on one graph, the two 2 state variables  $C_x$  &  $C_s$  as function of  $D$  ( $D_{crit}$ )

- e. (6) From mass balances, express all other state variables as function of  $D$  ( $NH_4^+$ , dissolved  $O_2$ , dissolved  $CO_2$  and  $H^+$ ) using:
- $C_{N,in} = Y_{SN} * C_{S,in} * 120\%$ ,  $Y_{SN}$  obtained from  $Y_{SX}$  and  $Y_{NX}$  of global growth equation
  - $C_{O,in}=0 \text{ mole.m}^3$ ,  $K_{la} = 90 \text{ hr}^{-1}$ ,  $C_{O2,sat} 25^\circ\text{C} = 0.258 \text{ mole.m}^{-3}$ . We consider that there is no limitation, and there no  $O_2$  switch function. [same recommendations that will be used in A.2.3 (below)]

Once all  $C_i$  states variables can be expressed from their respective mass balance, compute and plot on one graph, all these  $C_i$  component concentrations of global growth equation using same dilution rates of d.)

Do the same for all  $r_i$  volumetric rates.

- f. (2) Check  $K_s$  affinity constant effect on chemostat behavior, by modifying  $k_s$ .  
Note:  $C_x$ ,  $C_s$  and  $D_{critical}$  depend on to  $\mu^{max}$  or  $q_s^{max}$  and  $K_s$ . Compute  $C_x$  and  $C_s$  as function  $f(K_s, \mu) = f(K_s, D)$ , for Half  $K_s$ ,  $K_s$  and 2 times  $K_s$ . Then plot  $C_s$  and  $C_x$  vs dilution rate  $D$ . Comment!

- g. (4) The aim of this chemostat study will be to use an experimental chemostat for the estimation of the 4 biological kinetic parameters ( $\mu^{max}$ ,  $Y_{sx}^{max}$ ,  $k_s$ , and  $m_s$ ) of heterotrophic biomass growing aerobically on sodium acetate.  
According estimation tools (See Chemostat lecture: Lineweaver-Burk and Hanes-Woolf linearization), the quality of the estimation depends on the covered range of  $C_s$  substrate residual concentration, which is fixed by the dilution rate  $D$  chosen, for each chemostat Steady State.

Using the  $C_S=f(D)$  expression (provide 10 dilution rate values, providing 10  $C_S$  values which cover the range from  $0.1 \times C_{S_{in}}$  to  $C_{S_{in}}$ , in an equal distributed manner...

- h. (3) During Practical Labs Chemostat experiment, even if  $C_{S_{in}}$  and  $D$  are supposed to be chosen and fixed, pumping reality of inlet medium, real outlet flow, bioreactor volume as well as inlet substrate concentration make observed/measured  $C_{S_{in}}$  and  $D$  quite different from what has been supposed to be chosen. As residual substrate and biomass concentration depends mainly on these 2 applied operating parameters  $C_{S_{in}}$  and  $D$ , provide an easy calculation of  $C_S$  and  $C_X$  using applied observed  $C_{S_{in}}$  and  $D$  dilution rate. Use  $C_S$  and  $C_X$  expressions above.