

# Bioprocesses → Bioreactors

**The job to be done: Design and operate Bioprocesses towards best efficiency and productivity, at minimal cost!**

For achieve best efficiency or productivity [ $\text{kgP}\cdot\text{m}^{-3}\cdot\text{d}^{-1}$ ]:

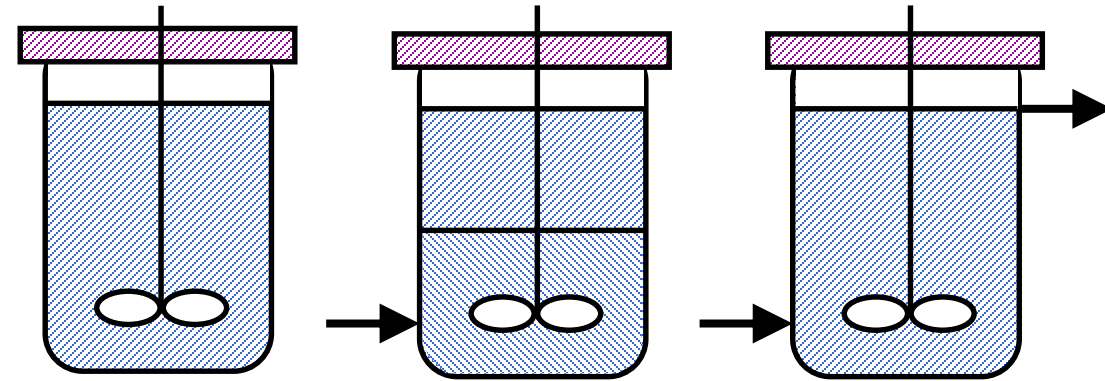
- Optimal Biomass (active one)
- Optimal Operation allowing highest kinetics for growth (production)
- Designing optimal feeding profile
- Optimize required transports of substrates/products (transport processes)
- Scaling up optimization for biggest reactors avoiding transport processes limitation...

Such bioprocesses are operated in bioreactors, which are reactors where microbial growth and product formation occur.

→ What about bioreactors...

# Bioprocesses → Bioreactors

Generic type of process bioreactors:



**Batch**  
2-12 days  
Industry

**Fed batch**  
1 – 3 days  
Industry

**Continuous  
(Chemostat)**  
10 - 100 days  
Laboratory

From previous kinetic theory of specific rates  $q_i$ :  $\mu$

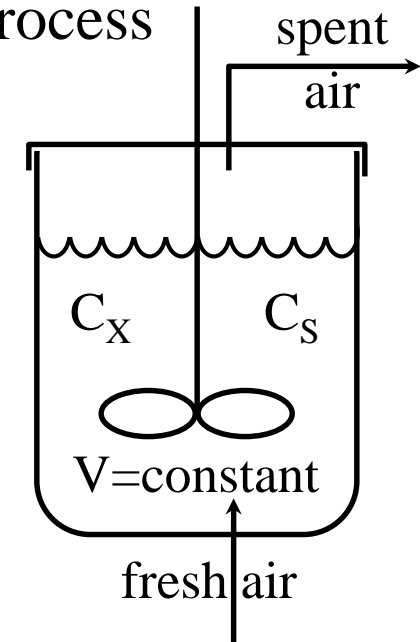
- $q_S$  (or)  $\mu$  completely determines the **microbial behavior**
- $q_S$  (or)  $\mu$  must be controlled at an **optimal value**  $\mu_{opt}$

1. **Batch**       $\mu = \mu^{max}$  and  $q_S = q_S^{max} \rightarrow \mu$  is **not** controlled
2. **Chemostat**       $\mu$  **can be controlled** as  $\mu = D$  (Dilution rate) at  $\mu^{opt}$
3. **Fed batch**       $r_S$  is controlled by ( $C_S$  and inflow)

# Batch process (1)

DEFINITION: Parameters - State variables of Batch bioprocess

Parameters			state Variables
reactor	operator	micro-organism	
$V$	$C_{S0}$ $C_{X0}$	$q_S^{\max}$ $\mu^{\max}$ $Y_{SX}^{\max}$ $m_S, K_S$	$C_S$ $C_X$



OPERATION:

1. Add growth medium solution (sterilized?): Substrate with initial concentration  $C_{S0}$ , N- and P-source,  $K^+$ ,  $Mg^{2+}$ , salts, nutrients, vitamins, trace elements and chosen T, pH
2. Add electron acceptor ( $O_2$ ,  $NO_3^-$ , etc).
3. Add (inoculum) micro-organism,  $C_{X0}$   
 $\rightarrow t = 0$  ; Biomass =  $C_{X0}$  and Substrate =  $C_{S0}$

# Batch process (2)

DYNAMIC of the state variables.

How will  $C_S$  and  $C_X$  change with time?

Using of mass balances...

For Biomass  $C_X$ :

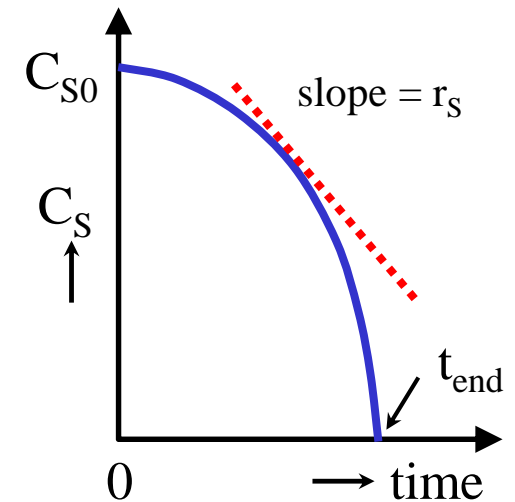
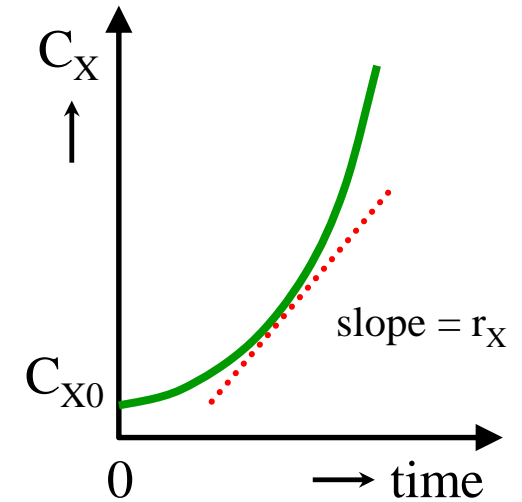
$$\frac{d(C_X V)}{dt} = \text{transport of biomass} + r_X V$$

$$V = \text{cst} \rightarrow r_X = \frac{dC_X}{dt} = \text{slope}$$

For Substrate  $C_S$ :

$$\frac{d(C_S V)}{dt} = \text{transport of biomass} + r_S V$$

$$V = \text{cst} \rightarrow r_S = \frac{dC_S}{dt} = \text{slope}$$



# Batch process (State variables)

DYNAMIC of the state variables from mass balances  
 As  $\mu \approx \mu^{\max} = \text{cst}$ , and  $q_s \approx q_s^{\max} = \text{cst}$ , as  $C_s$  is high.  
 At  $t = 0$ , biomass =  $C_{X0}$ , substrate =  $C_{S0}$ .

For Biomass  $C_X$ :  $r_x = \mu C_X \rightarrow \frac{dC_X}{dt} = \mu^{\max} \cdot C_X$

→ Exponential  
Growth

$$C_X = C_{X0} \exp(\mu^{\max} t)$$

$P\left(\frac{1}{X}\right) = [\ln(x)]_{x_0}^x$

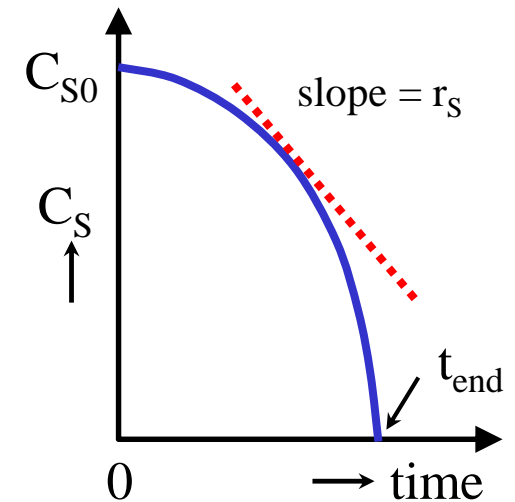
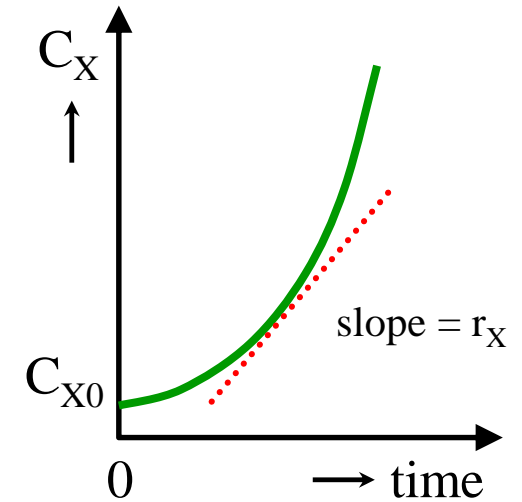
For Substrate  $C_S$ :  $r_s = q_s C_X \rightarrow \frac{dC_S}{dt} = -q_s^{\max} C_X$

$$\frac{dC_S}{dt} = -q_s^{\max} C_{X0} \exp(\mu^{\max} t)$$

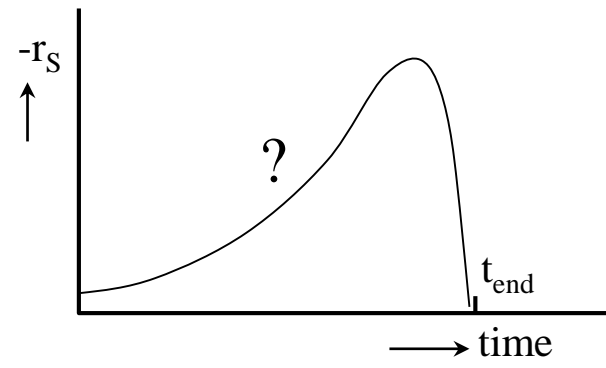
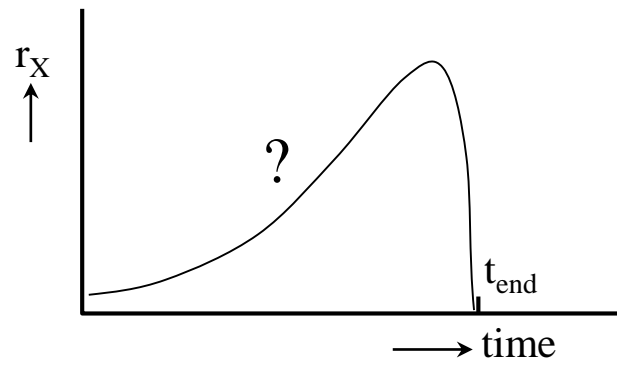
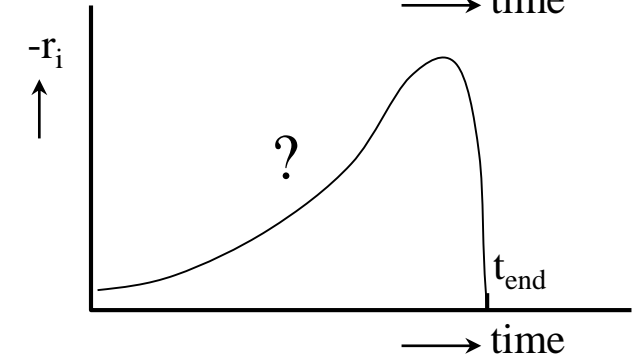
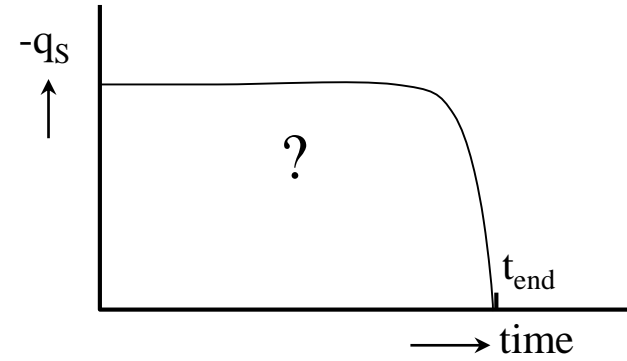
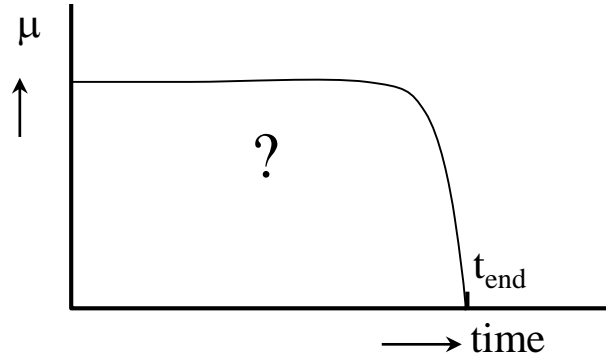
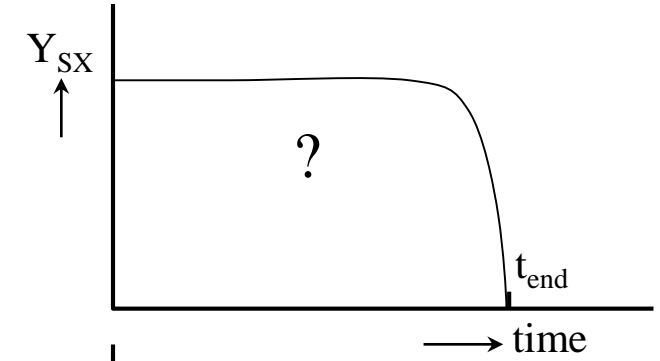
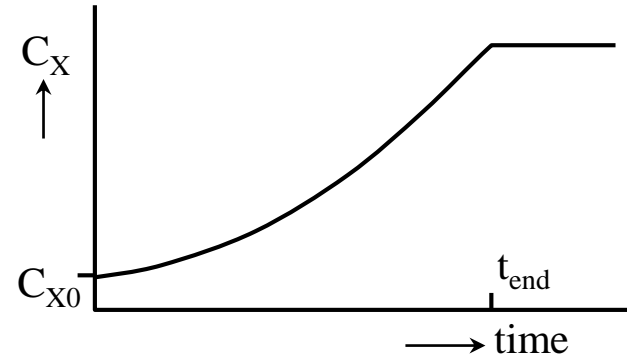
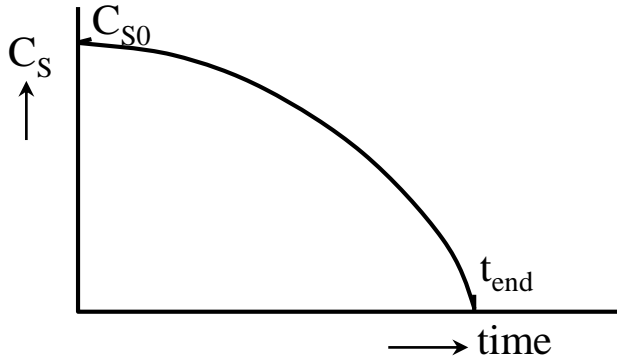
$$C_{S0} - C_S = \frac{q_s^{\max}}{\mu^{\max}} C_{X0} \left[ \exp(\mu^{\max} t) - 1 \right]$$

$P\left(\frac{1}{a}\right) = \left[ \frac{e^{ax}}{a} \right]_{x_0}^x$

→  $t_{\text{end}}$  can be determined with  $C_S = 0$ !



# Batch process (Results)



# Batch process (Comments)

Batch bioprocess, under non limiting conditions (substrate),  $\mu$ ,  $Y_{SX}$  and  $q_S$  are constant  $\rightarrow \mu^{\max}$ ,  $Y_{SX}^{\max}$ ,  $q_S^{\max}$ . This occur during Exponential Growth phase (and only during this phase!!!)

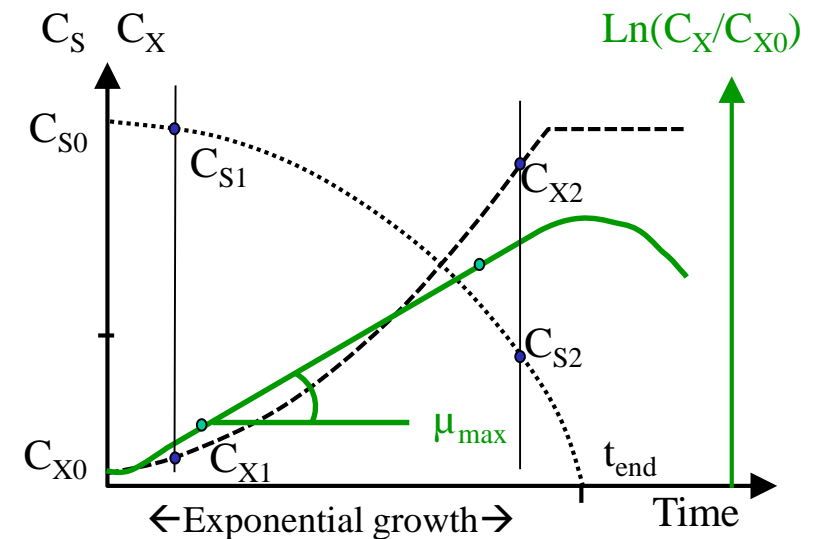
Microbiological biokinetic model parameters are easily determined by combining the exponential equation with  $C_S$  and  $C_X$  data versus time

$$C_X = C_{X0} \exp(\mu^{\max} t)$$

During Exponential Growth phase (only!)

$$\mu^{\max} = \text{slope} \ln\left(\frac{C_X}{C_{X0}}\right)$$

$$Y_{SX} \approx Y_{SX}^{\max} = \frac{C_{X2} - C_{X1}}{C_{S1} - C_{S2}}$$



$\rightarrow$  But  $\mu$ , the most important rate (Herbert-Pirt Eq.) can not be controlled in batch bioprocess!

# Bio-sample stability ?

Sampling of a bioprocess to access  $C_S$  and  $C_X$ . Once sampled, what behavior?

- $C_X$  does not significantly change within minutes
- But  $C_S$  may strongly drop within minutes according  $q_S$

**$C_{SR}$  is the Residual Substrate of the bioprocess to be measured.** The sample tube can be considered as a batch bioreactor ( $V = \text{cst}$ , No transport). From substrate mass balance:

With  $t = 0 ; C_S = C_{SR} ; q_S^{\text{max}} = \text{cst} ; C_X = \text{cst}$

$$\frac{dC_S}{dt} = q_S \cdot C_X = -q_S^{\text{max}} \cdot \frac{C_S}{K_S + C_S} \cdot C_X$$

$$\frac{K_S + C_S}{C_S} \cdot dC_S = -q_S^{\text{max}} \cdot C_X \cdot dt$$

$$K_S \ln\left(\frac{C_S}{C_{SR}}\right) + C_{SR} \left(\frac{C_S}{C_{SR}} - 1\right) = -(q_S^{\text{max}} C_X) t$$

$$F\left(\frac{ax+b}{cx+d}\right) = \frac{ax+b}{c} - \frac{ad-bc}{c^2} \cdot \ln|cx+d|$$

Assuming		t(s)	$C_S/C_{SR}$
$K_S$	= 20 $10^{-3}$ [gS.L <sup>-1</sup> ]	1	0.91
$q_S^{\text{max}}$	= $1 \cdot 10^{-3}$ [gS.gX <sup>-1</sup> .s <sup>-1</sup> ]	5	0.61
$C_X$	= 3.5 [gX.L <sup>-1</sup> ]	10	0.33
$C_{SR}$	= 20. $10^{-3}$ [gS.L <sup>-1</sup> ]	<b>25</b>	<b>0.03</b>

→ How to prevent this ?