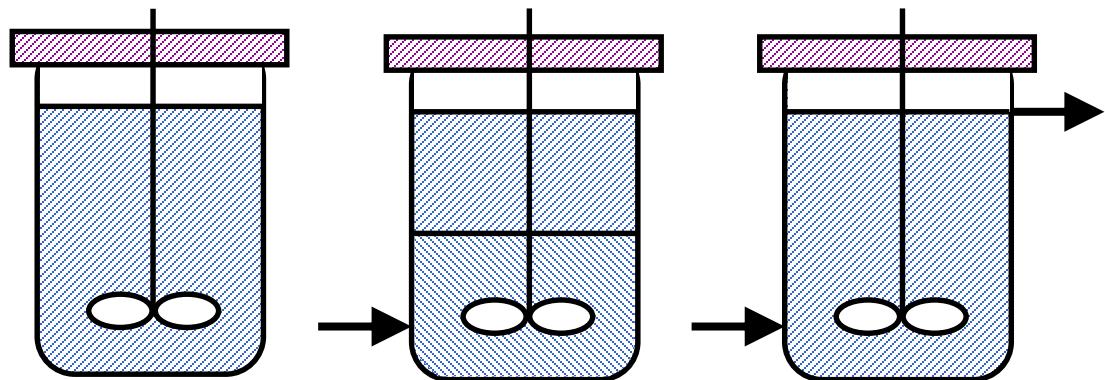


Bioprocesses → Bioreactors

From previous kinetic theory of specific rates q_i :

- q_S (or) μ completely determines the **microbial behavior**
- q_S (or) μ must be controlled at an **optimal value μ_{opt}**

Generic type of process bioreactors:



Batch

2-12 days
Industry

Fed batch

1 – 3 days
Industry

Continuous
(Chemostat)
10 - 100 days
Laboratory

1. Batch $\mu = \mu^{\max}$ and $q_S = q_S^{\max} \rightarrow \mu$ is **not** controlled

2. **Chemostat** μ can be controlled as $\mu = D$ (Dilution rate) at μ^{opt}

3. Fed batch r_S is controlled by (C_S and inflow)

Chemostat process (1)

DEFINITION: Parameters - State variables of Chemostat bioprocess

Parameters			State variables
reactor	operator	micro-organism	
V $\phi_{L,out}$	$\phi_{L,in}$ $C_{S,in}$	q_S^{max} μ^{max} Y_{SX}^{max} m_S, K_S	C_S C_X

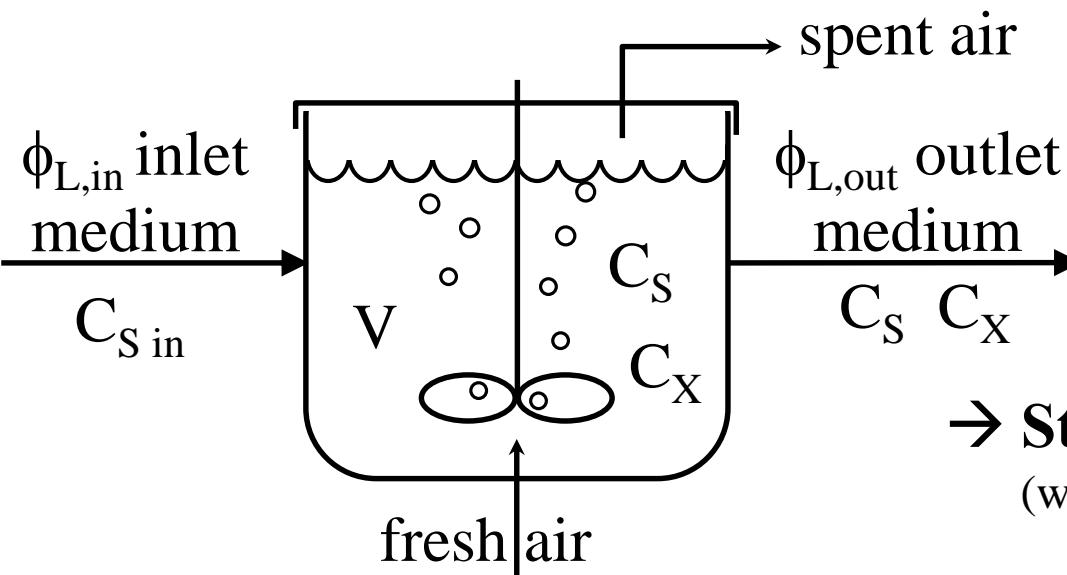
Main properties of chemostat:

- $\mu = D$ **Dilution rate** ($?=1/HRT=1/SRT?$)
- C_S and C_X are **independently manipulated** (by manipulating transport of substrate and biomass to and from the bioreactor)
- It's the (basic) **experimental tool** to study under controlled conditions :
 - Microbial kinetics $q_S(C_S)$, $q_P(\mu)$
 - Stoichiometry of bioprocesses

Complex transient dynamics!

Constant $\phi_{L,in}$, $\phi_{L,out}$, C_S , C_X , Vol.

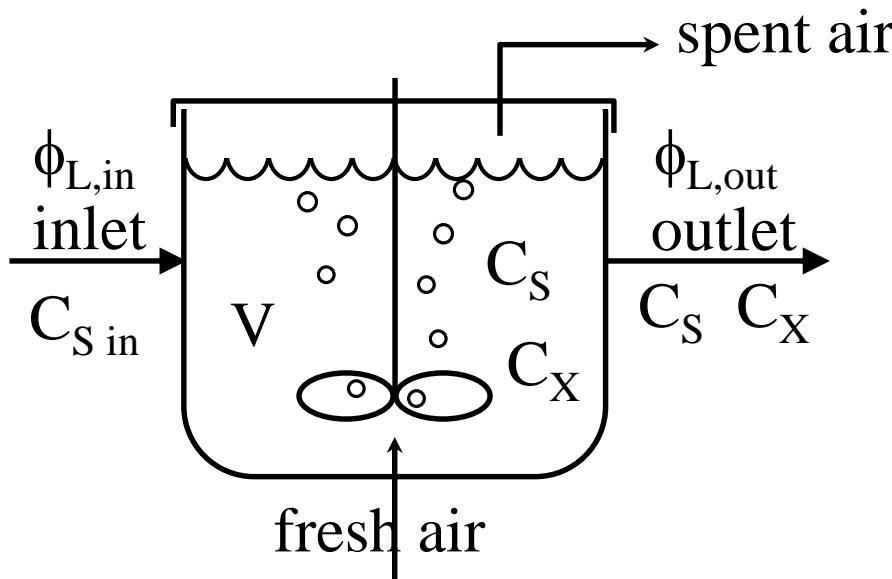
→ **Steady State ≡ Dynamic Equilibrium**
(where all state variables appear stable within time)



Chemostat process (2)

OPERATION of Chemostat bioprocess

1. A **bioreactor CSTR type** (Continuously Stirred Tank Reactor) (sterilized?) is filled with (sterile?) **growth medium** solution containing substrate $C_{S, \text{in}}$, N- and P-source, K^+ , Mg^{2+} , salts, nutrients, vitamins, trace elements and chosen T, pH
2. Provide electron acceptor O_2 , by **starting aeration and mixing**



3. **Inoculate** by adding a small amount of micro-organism (inoculum)
4. **Start feeding** the medium inflow (often $\phi_{L, \text{in}}$ and $\phi_{L, \text{out}}$ are nearly equal, not always)
5. **Wait until a Steady State** \equiv S.S. \equiv Dynamic equilibrium, is achieved

Chemostat process - Steady State ($\mu=D$)

At S.S. mass balance for $C_x \rightarrow \cancel{\frac{d(VC_x)}{dt}} = Q_{L,in} \cancel{C_{x,in}} - Q_{L,out} C_x + r_x V$

At S.S. mass balance for $C_s \rightarrow \cancel{\frac{d(VC_s)}{dt}} = Q_{L,in} C_{s,in} - Q_{L,out} C_s + r_s V$

From mass balances: $r_x = \frac{Q_{L,out} C_x}{V}$ $(-r_s) = \frac{Q_{L,in} C_{s,in} - Q_{L,out} C_s}{V}$

- r_x follows from experimentally measured data and the biomass mass balance
- μ comes from r_x and measured C_x , as $r_x = \mu \cdot C_x$

Thus : $\mu = \frac{r_x}{C_x} = \frac{Q_{L,out}}{V} \stackrel{\text{def}}{=} D : \text{Dilution rate}$

By choosing D, the operator fixes μ . Because $\mu (=D)$ is chosen, **all other q_i -values are chosen** from stoichiometric coupling (see chapter on kinetics).

Chemostat process - Steady State (C_S)

Using C_X mass balance \rightarrow Calculate C_S residual substrate in bioreactor
(only limited by substrate)

From kinetic expression for q_S [Herbert-Pirt Eq. and q_S hyperbolic kinetic]
 C_S and μ are linked, with Y_{SX}^{\max} , m_S , q_S^{\max} , K_S :

Thus μ can be expressed as $\mu = f(C_S)$
and $C_S = f(\mu) \dots$

$$q_S^{\max} \cdot \frac{C_S}{K_S + C_S} = -q_S = \frac{1}{Y_{SX}^{\max}} \mu + m_S$$

$$q_S^{\max} Y_{SX}^{\max} C_S = (\mu + m_S Y_{SX}^{\max}) \cdot (K_S + C_S)$$

$$\mu = \frac{C_S (q_S^{\max} Y_{SX}^{\max} - m_S Y_{SX}^{\max}) - m_S Y_{SX}^{\max} K_S}{(K_S + C_S)} \text{ with } q_S^{\max} = \frac{1}{Y_{SX}^{\max}} \mu^{\max} + m_S$$

$$\mu = \frac{C_S \mu^{\max} - m_S Y_{SX}^{\max} K_S}{(K_S + C_S)} \text{ with } C_S^{\min} = \frac{m_S Y_{SX}^{\max} K_S}{\mu^{\max}}$$

$$q_S^{\max} Y_{SX}^{\max} C_S = (\mu + m_S Y_{SX}^{\max}) \cdot (K_S + C_S)$$

$$C_S = \frac{(\mu + m_S Y_{SX}^{\max}) \cdot K_S}{(q_S^{\max} Y_{SX}^{\max} - (\mu + m_S Y_{SX}^{\max}))} \text{ with } \mu^{\max} = q_S^{\max} Y_{SX}^{\max} - m_S Y_{SX}^{\max} \text{ and } \mu = D$$

$$C_S = \frac{m_S Y_{SX}^{\max} K_S + D K_S}{(\mu^{\max} - D)} \text{ with } C_S^{\min} = \frac{m_S Y_{SX}^{\max} K_S}{\mu^{\max}}$$

$$\mu = \mu^{\max} \frac{C_S - C_S^{\min}}{C_S + K_S} ; C_S^{\min} = m_S K_S Y_{SX}^{\max} / \mu^{\max}$$

$$C_S = \frac{C_S^{\min} + K_S \frac{D}{\mu^{\max}}}{1 - \frac{D}{\mu^{\max}}}$$

Chemostat process - Steady State (C_S)

Thus, C_S residual substrate :

$$C_S = \frac{C_S^{\min} + K_S \frac{D}{\mu^{\max}}}{1 - \frac{D}{\mu^{\max}}}$$

- Is independent of $C_{S,in}$!!!
 - Depends only on:
 - Microbial characteristics
 - D dilution rate
- ??? How ???

$$\mu = \mu^{\max} \frac{C_S - C_S^{\min}}{C_S + K_S} ; C_S^{\min} = m_s K_s Y_{sx}^{\max} / \mu^{\max}$$

$$\mu = \frac{r_x}{C_x} = \frac{Q_{L,out}}{V} \stackrel{\text{def}}{=} D : \text{Dilution rate}$$

Specific growth rate depends only on C_S . During exponential batch growth, or very high C_S residual substrate, C_S^{\min} becomes negligible, according “Monod” growth.

Chemostat process - Steady State (C_X)

Using $C_S \rightarrow$ Calculate C_X

Calculate r_s from measurements using C_S mass balance $(-r_s) = \frac{Q_{L,in}C_{S,in} - Q_{L,out}C_S}{V}$

Thus:

$$(-r_s) = (\alpha \cdot C_{S,in} - C_S) \cdot D \quad \text{with} \quad \alpha = \frac{Q_{L,in}}{Q_{L,out}}, D = \frac{Q_{L,out}}{V}$$

$$\text{As } r_s = q_s \cdot C_x \rightarrow C_x = \frac{(\alpha \cdot C_{S,in} - C_S) \cdot D}{(-q_s)} \text{ as } Y_{SX} = \frac{\mu}{q_s}$$

Thus C_X expression depends on $C_{S,in}$:

As $C_S = f(D)$, $Y_{SX} = f(\mu) = f(D)$

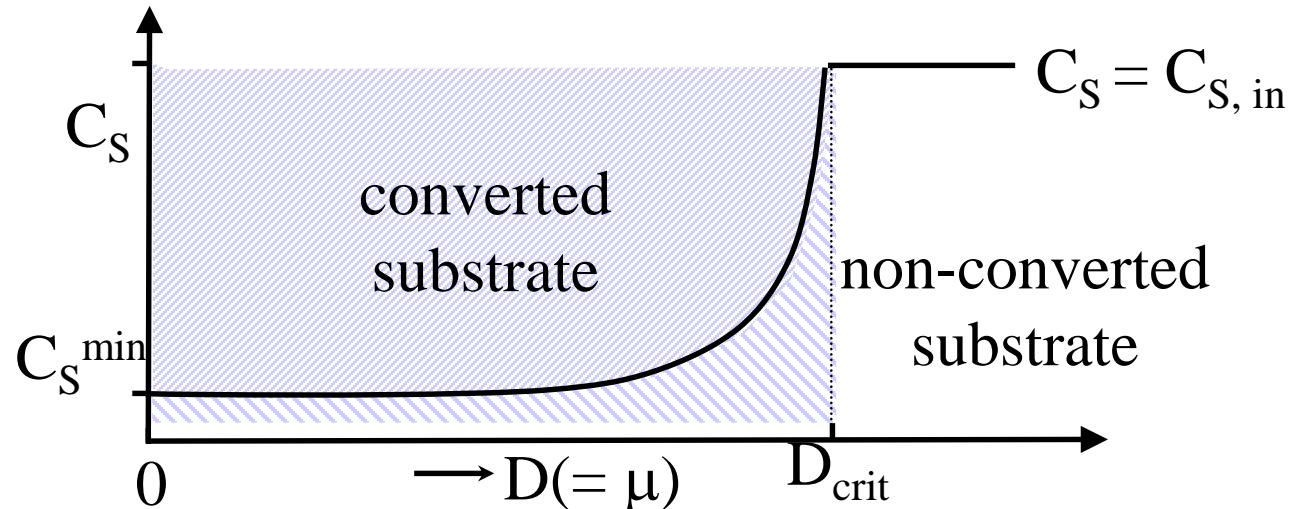
$$C_X = Y_{SX} (\alpha \cdot C_{S,in} - C_S)$$

$$\text{as } Y_{SX} = \frac{\mu}{(-q_s)} \quad C_S = \frac{C_S^{min} + K_S \frac{D}{\mu^{max}}}{1 - \frac{D}{\mu^{max}}}$$

Mostly $C_S \approx 0$ for $D \ll \mu^{max}$
 (Again, ONLY for exclusively substrate limited condition)

Chemostat process - Steady State (D_{crit})

$$C_S = \frac{C_S^{\min} + K_S \frac{D}{\mu^{\max}}}{1 - \frac{D}{\mu^{\max}}}$$



With:

$C_{S,\text{in}}$ order of 10000; C_S^{\min} order 1; K_S order of 10 [mgCOD.L⁻¹]

D_{crit} is the maximal dilution rate D (i.e. μ), achievable in the chemostat. It occurs when the maximal C_S is achieved: $C_S = C_{S,\text{in}}$.

$$D_{\text{crit}} = \mu^{\max} \cdot \frac{(C_{S,\text{in}} - C_S^{\min})}{K_S + C_{S,\text{in}}} \approx \mu^{\max}$$

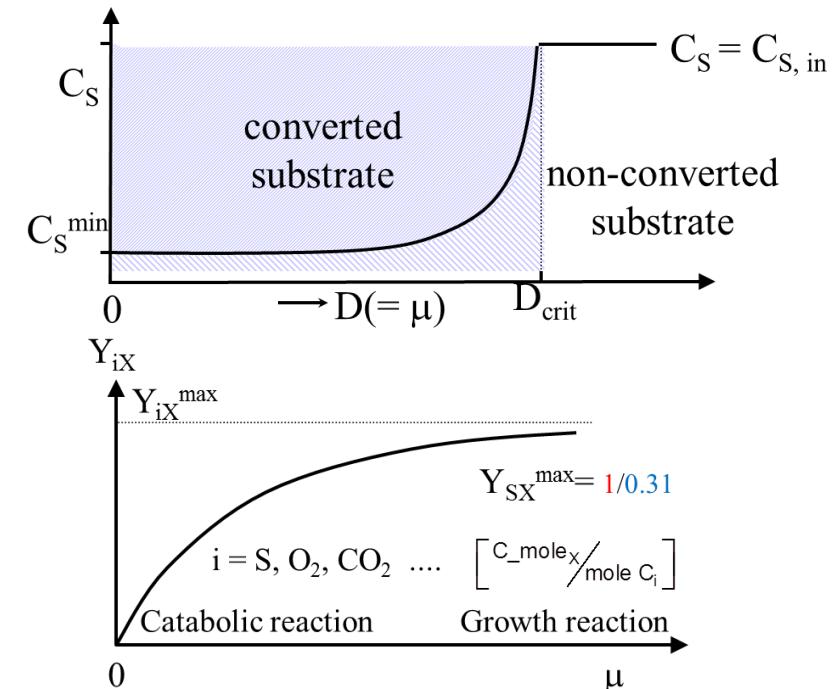
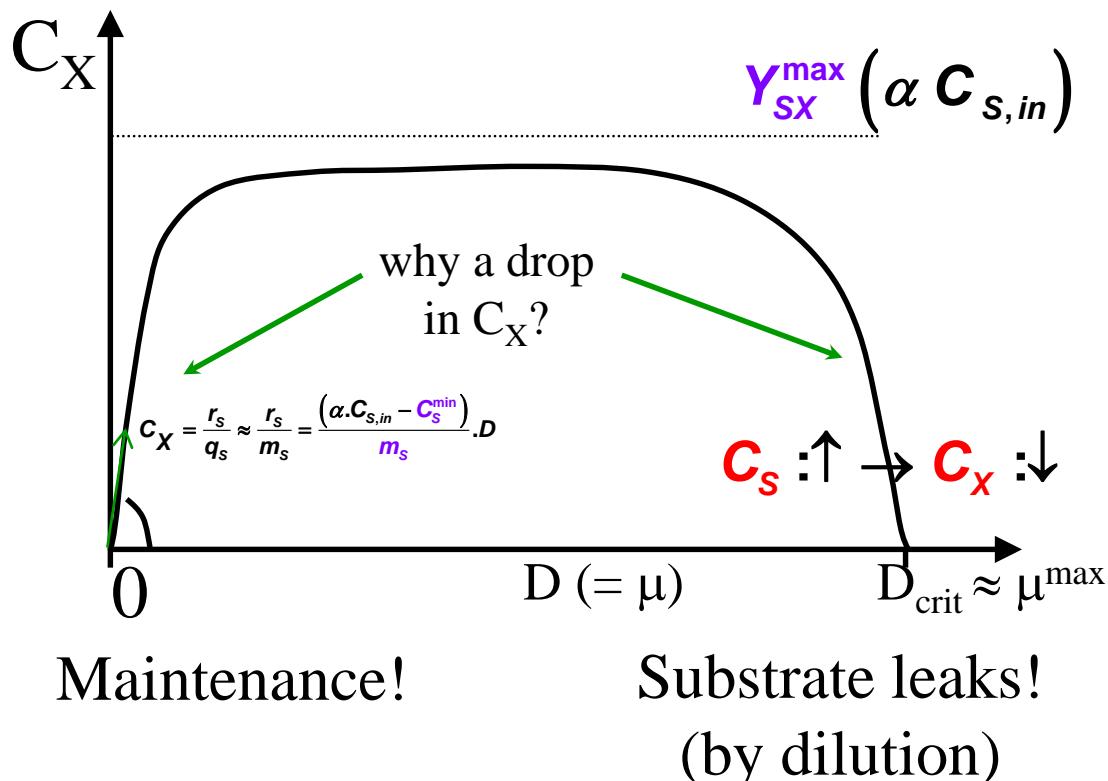
Washing out of the bioreactor occurs when the applied dilution rate exceeds the maximum specific growth for a given $C_{S,\text{in}}$. This happens when $D = D_{\text{crit}}$.

Chemostat process - Steady State (D)

From:

$$C_X = Y_{SX} (\alpha \cdot C_{S,in} - C_S)$$

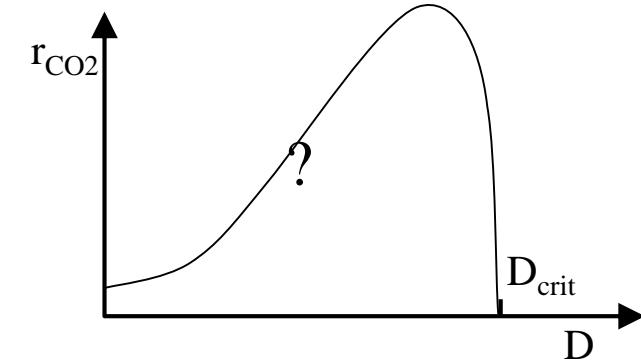
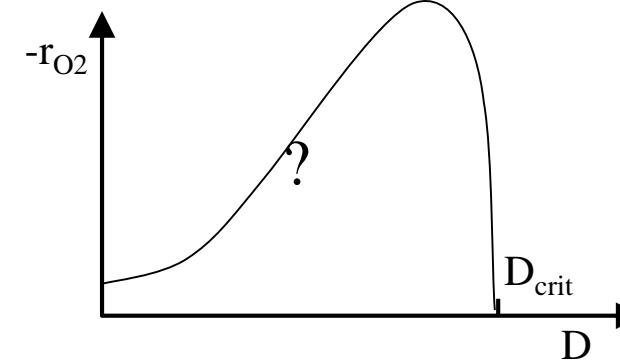
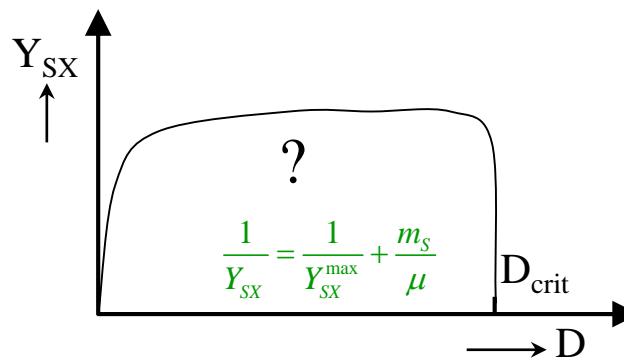
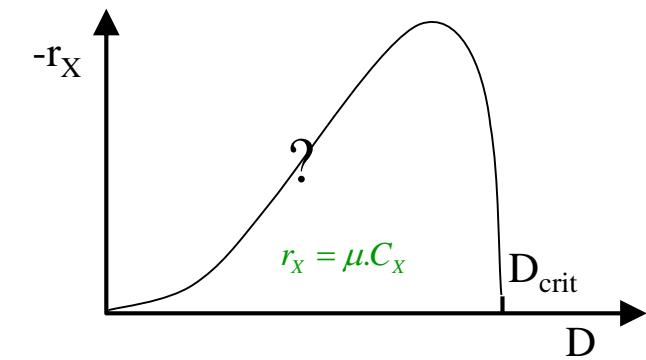
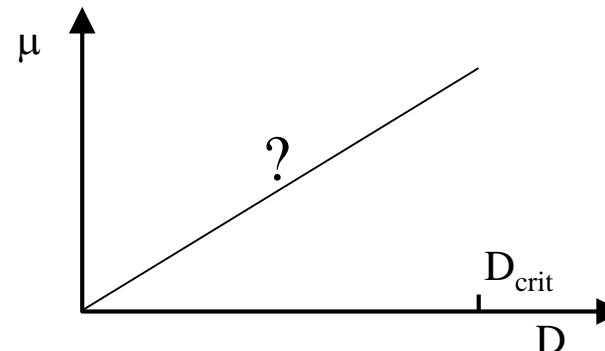
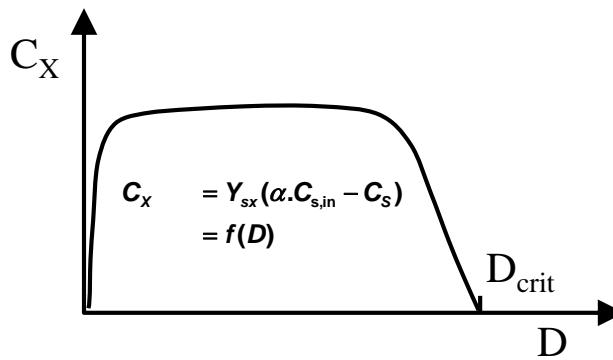
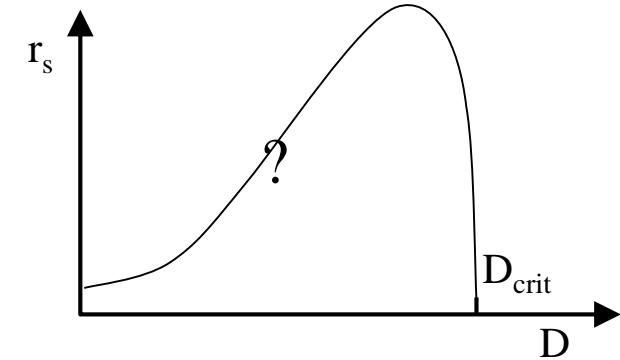
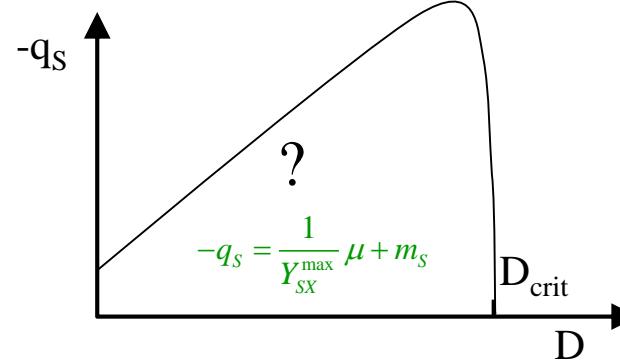
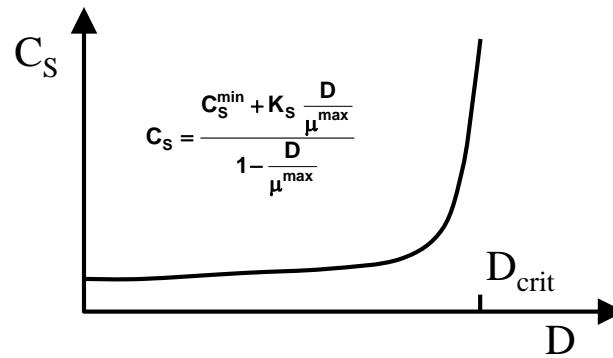
As Y_{SX} and C_S depends on D $\rightarrow C_X = f(D)$



As biomass C_X depends on the overall C_S consumption :

- At low D, low μ , low C_S , maintenance drives C_S consumption instead of growth...
- When $D \approx D_{crit}$, the growth cannot consume all the available substrate, which leaks impair C_X growth...

Chemostat - Behavior



Chemostat - Applications

1. Kinetic studies

By choosing different $D (= \mu)$ values, and waiting for Steady State, as $C_S = f(D)$, one obtains Y_{SX}^{\max} , m_S , q_S^{\max} , K_S by linear or non linear fitting

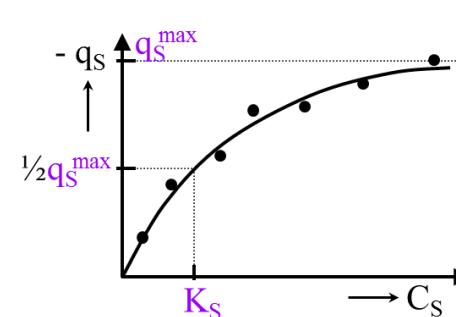
Lineweaver-Burk linearisation

$$\frac{1}{q_S} = \frac{k_s}{q_S^{\max}} \frac{1}{C_S} + \frac{1}{q_S^{\max}}$$

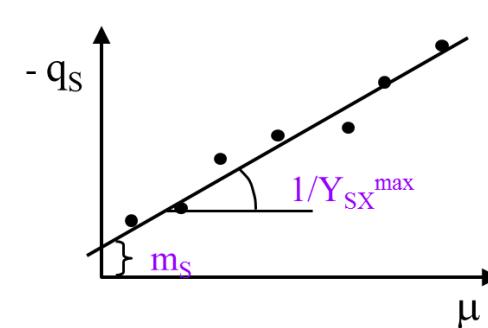
Hanes-Woolf linearisation

$$\frac{C_S}{q_S} = \frac{1}{q_S^{\max}} \cdot C_S + \frac{k_s}{q_S^{\max}}$$

Hyperbolic equation $q_S = f(C_S)$



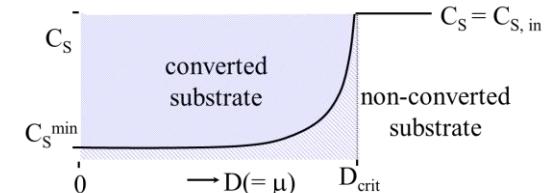
Herbert-Pirt equation $q_S = f(\mu)$



2. Physiological studies of microorganisms by change in substrate, electron acceptor, N-source or type of limitation ...

3. Waste water treatment purification $(+)/(-) ???$

4. Industrial fermentation (not widely applied : low C_X , low C_P , biomass loss in outflow, microbial selection for non-producing mutants)



Chemostat – Optimisation (D_{opt})

What D-value = D_{opt} where r_S and r_X are maximal?

(which may be combined with economic parameters)

$$r_S = \text{kg S}_{\text{converted}} \cdot \text{m}^{-3} \cdot \text{h}^{-1}$$

From substrate mass balance and assuming $\alpha = 1 : r_S = D \cdot (C_{S,in} - C_S)$

According, $C_S = f(D)$ graph, r_S has a maximum at higher D, therefore assuming m_S negligible $\rightarrow C_S^{\min} \approx 0$

$$\text{Thus } C_S = \frac{K_s / \mu^{max}}{\frac{D}{\mu^{max}} - 1}; r_S = DC_{S,in} - DK_s \times \frac{D}{\mu^{max} - D}$$

D_{opt} follows from differentiation where $\frac{dr_S}{dD} = 0$

Using MathCAD

$$\text{Find}(D) \rightarrow \left[\frac{1}{2 \cdot (C_{S,in} + 1)} \cdot \left[2 \cdot C_{S,in} + 2 + 2 \cdot (C_{S,in} + 1)^{\frac{1}{2}} \right] \cdot \mu_{max} \right] \cdot \left[\frac{1}{2 \cdot (C_{S,in} + 1)} \cdot \left[2 \cdot C_{S,in} + 2 - 2 \cdot (C_{S,in} + 1)^{\frac{1}{2}} \right] \cdot \mu_{max} \right]$$

Chemostat – Wash-out dynamics

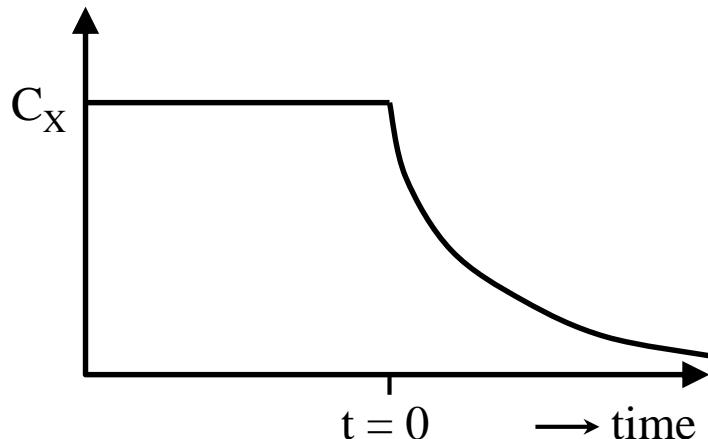
Assume that D is close to D_{crit} , and μ close to μ^{max} under Steady State conditions

→ What happens if D is increased to D' above μ^{max} ?
The biomass C_x will be washed out of the bioreactor.

From biomass mass balance

$$\frac{dC_x}{dt} = \mu C_x - D' C_x$$

with $\mu \gg \mu^{max}$; $\mu^{max} - D' < 0$ and cst



$$C_x(t) = C_{x(t=0)} * \exp^{-(D' - \mu^{max})t}$$

$$\text{or } \ln \frac{C_x}{C_{x(t=0)}} = -(D' - \mu^{max}) t$$

→ Washout curve can give $\mu^{max}!!!$
(Only under non limited growth C_s , C_{O_2} , etc...)

Very useful for short $\mu^{max} = 1/\text{HRT} = D$)

One Steady State is normally more than 3-5 HRT! If $1/\mu^{max}$ is about 3 weeks (methanogen), 3 months are required for 1 S.S.!