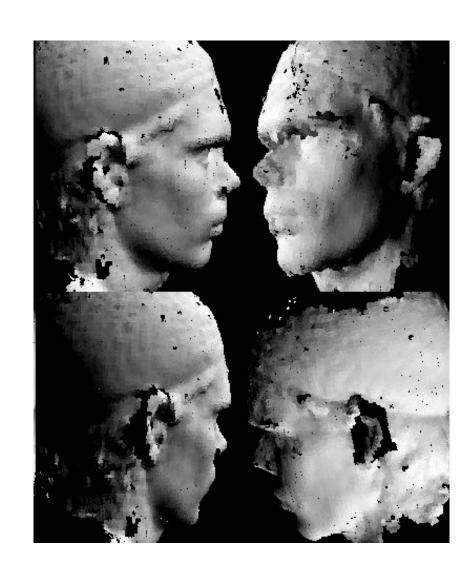
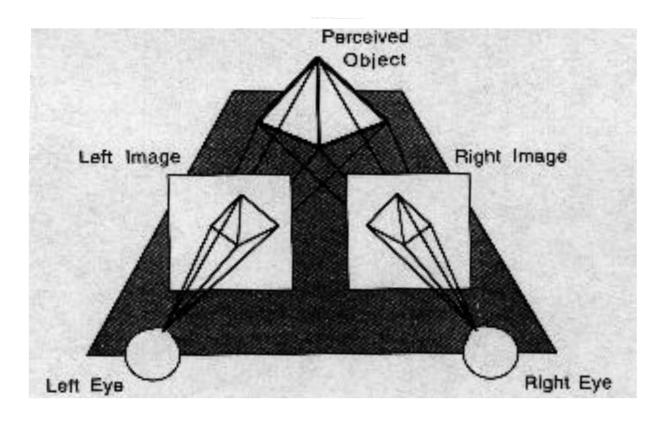
SHAPE FROM X

- One image:
 - Texture
 - Shading
- Two images or more:
 - Stereo
 - Contours
 - Motion



Geometric Stereo

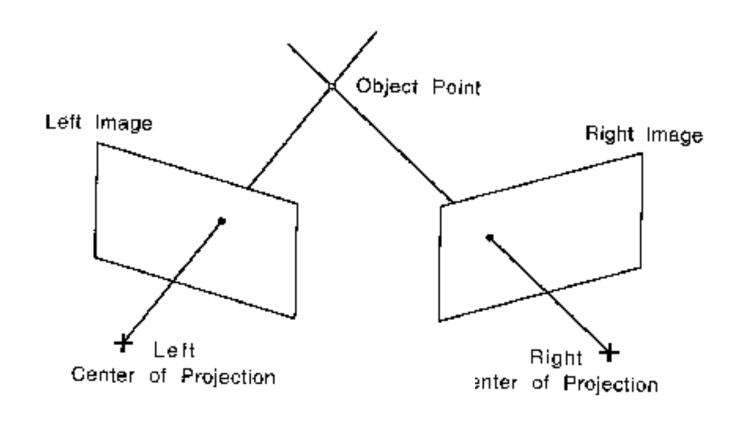


Depth from two or more images:

- Geometry of image pairs
- Establishing correspondences



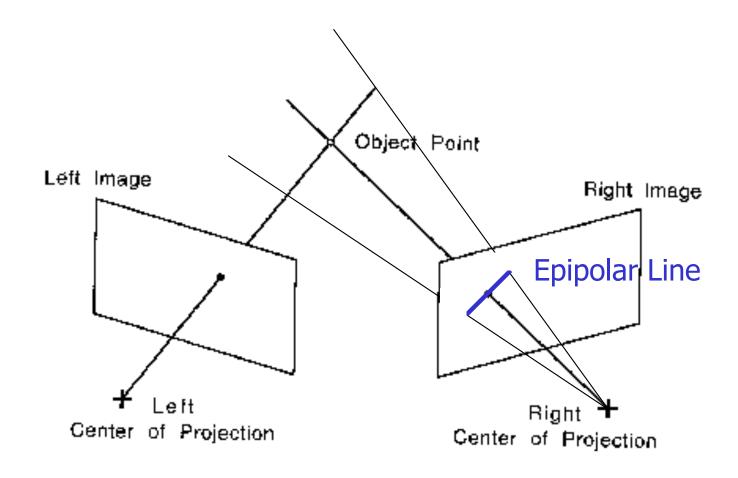
Triangulation



Geometric Stereo: Depth from two images



Epipolar Line



Line on which the corresponding point must lie.

Epipolar Lines



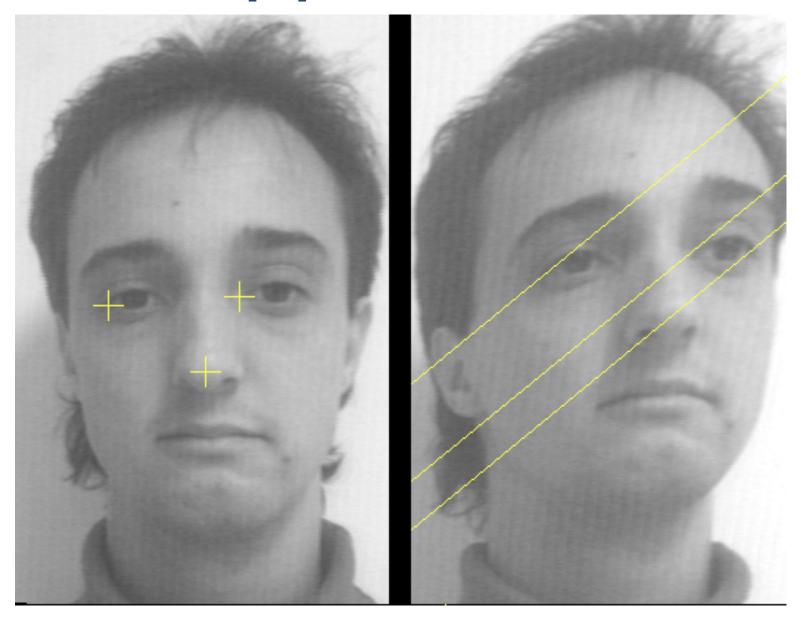


Three points shown as red crosses.

Corresponding epipolar lines.



Epipolar Lines

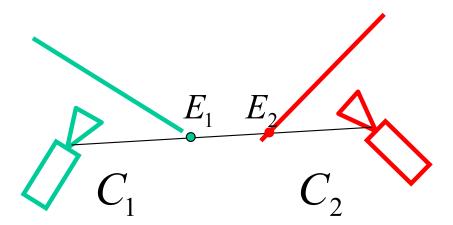


They can have any orientation.



Epipole





Point at which all epipolar lines intersect:

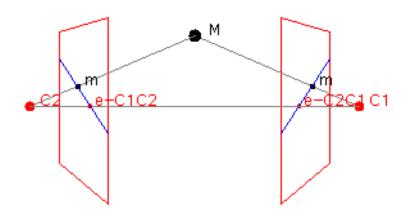
→ Located at the intersection of line joining optical centers and image plane.





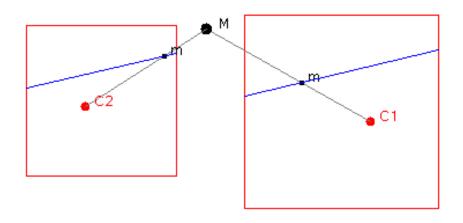
Epipolar Geometry

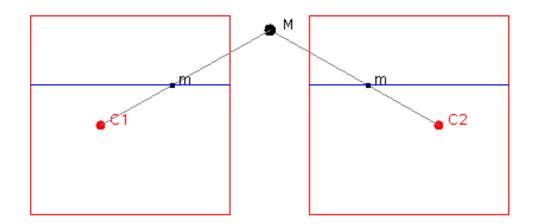
In general:



Parallel image planes

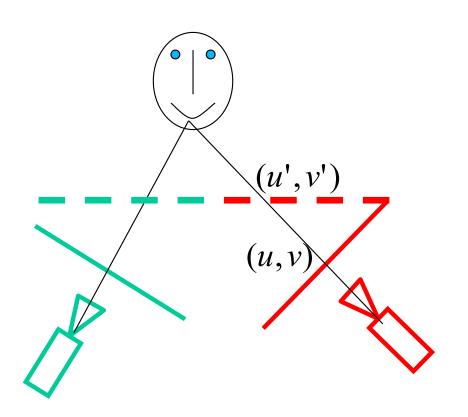
Horizontal baseline







Rectification



$$\begin{bmatrix} U' \\ V' \\ W' \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ 1 \end{bmatrix}$$

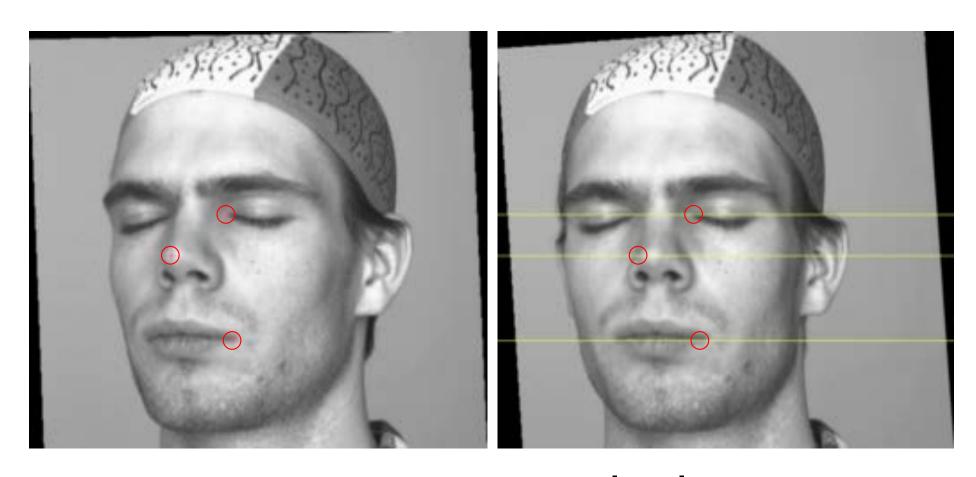
$$u' = \frac{U'}{W'}$$

$$v' = \frac{V'}{W'}$$

Reprojection into parallel virtual image planes:

- Linear operation in projective coordinates
- Real-time implementation possible

Rectification



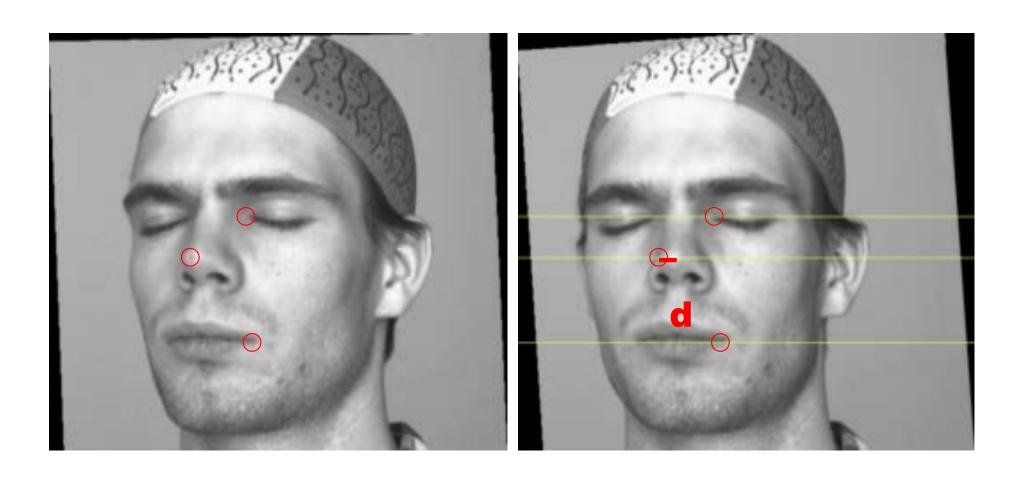
From intersecting epipolar lines ...

... to parallel ones.





Disparity



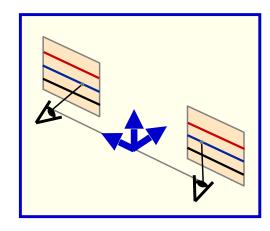
The horizontal shift along an epipolar line, inversely proportional to distance.





Disparity vs Depth





$$u_{l} = \frac{f(X - b/2)}{Z}, v_{l} = \frac{fY}{Z}$$
$$u_{r} = \frac{f(X + b/2)}{Z}, v_{l} = \frac{fY}{Z}$$

$$d = f \frac{b}{Z}$$

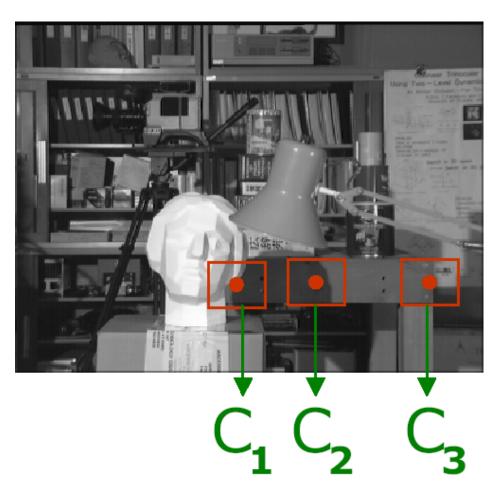
→ Disparity is inversely proportional to depth.





Window Based Approach to Establishing Correspondences



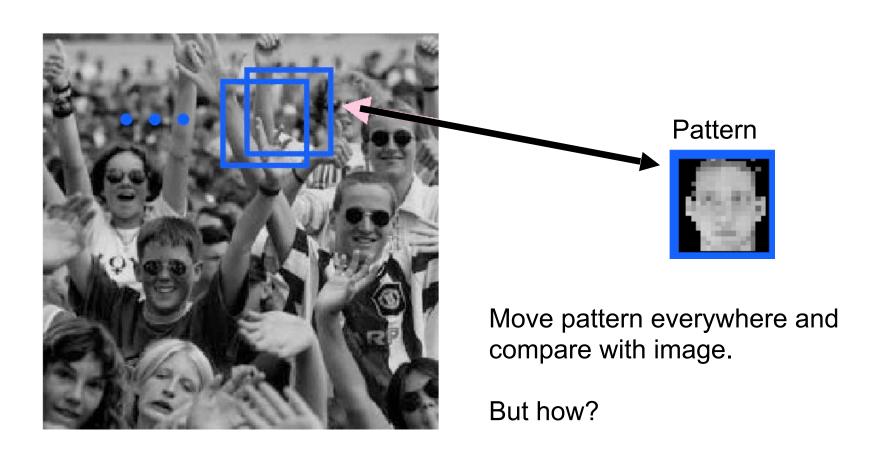


- Compute a cost for each C_n location.
- Pick the lowest cost one.



Finding a Pattern in an Image

Straightforward approach:





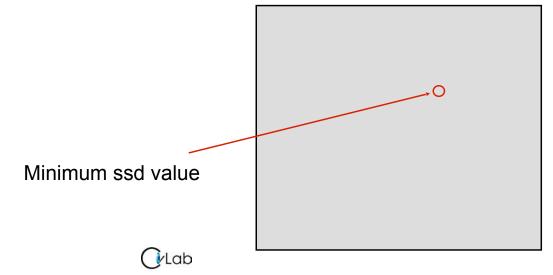
Sum of Square Differences

 Subtract pattern and image pixel by pixel and add squares:

$$ssd(u,v) = \sum_{(x,y)\in N} [I(u+x,v+y) - P(x,y)]^2$$

• If identical ssd=0, otherwise ssd >0

→Look for minimum of ssd with respect to u and v.



Correlation

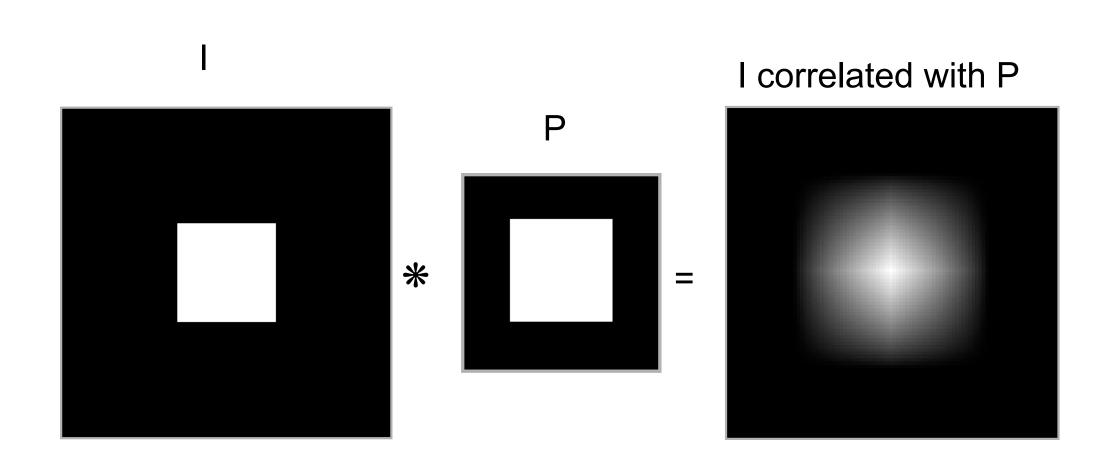
$$ssd(u,v) = \sum_{(x,y)\in N} \left[I(u+x,v+y) - P(x,y) \right]^2$$

$$= \sum_{(x,y)\in N} I(u+x,v+y)^2 + \sum_{(x,y)\in N} P(x,y)^2 - 2 \sum_{(x,y)\in N} I(u+x,v+y) P(x,y)$$
Sum of squares of the window the pattern (slow varying) (constant)

ssd(u,v) is smallest when correlation is largest

→ Correlation measures similarity

Synthetic Example





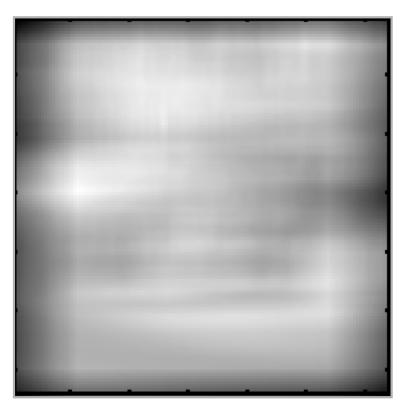


Rea World Example

Image Correlation







- The correlation value depends on the local gray levels of the pattern and image window.
- Need to normalize.

Normalized Cross Correlation

$$ncc(u,v) = \frac{\sum_{(x,y)\in N} [I(u+x,v+y)-\overline{I}][P(x,y)-\overline{P}]}{\sqrt{\sum_{(x,y)\in N} [I(u+x,v+y)-\overline{I}]^2 \sum_{(x,y)\in N} [P(x,y)-\overline{P}]^2}}$$

- Between -1 and 1
- Invariant to linear transforms
- Independent of the average gray levels of the pattern and the image window

Normalized Example

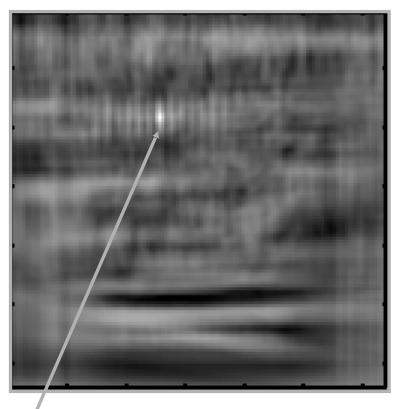
Image



Pattern



Normalized Correlation

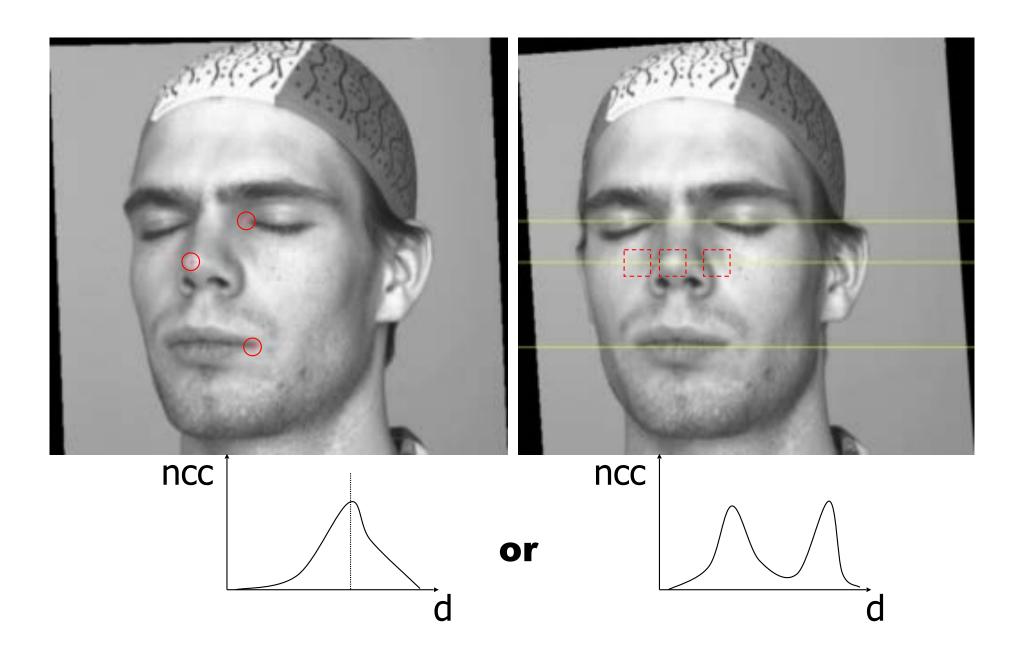


Point of maximum correlation





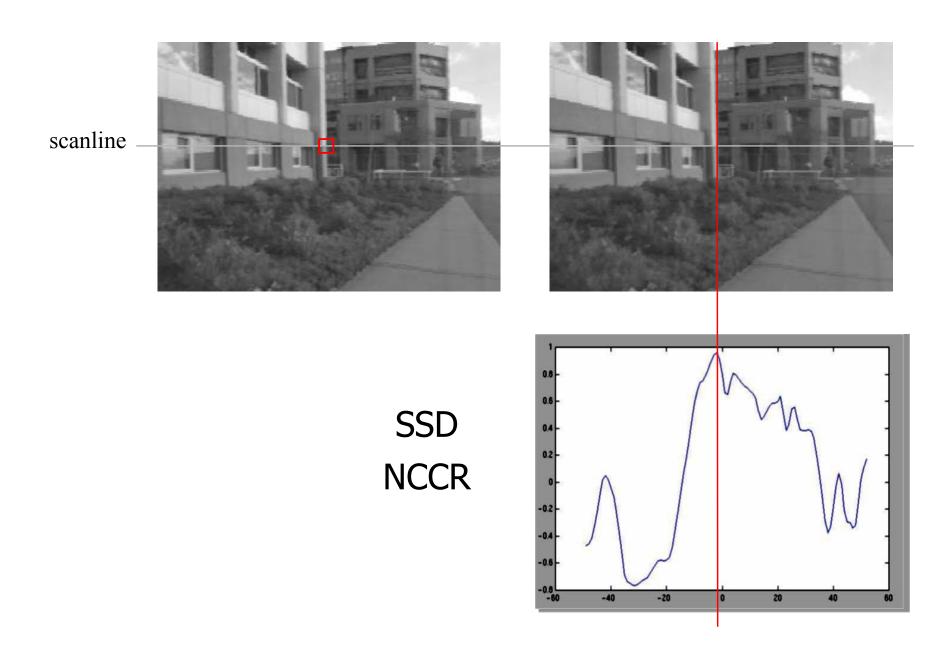
Searching along Epipolar Lines







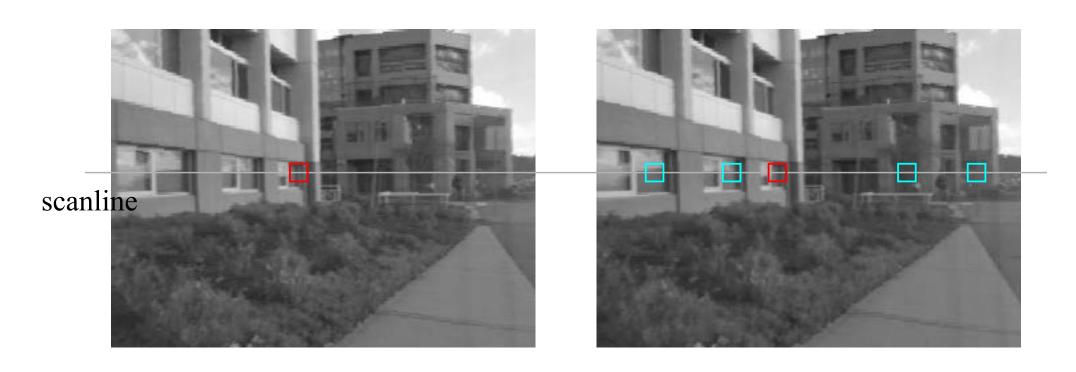
Outdoor Scene







Ambiguities



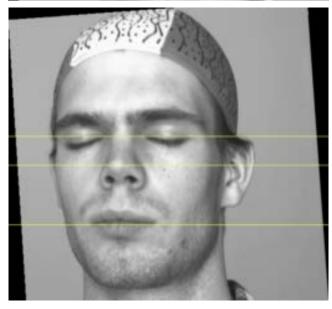
—> Repetitive patterns, textureless areas, and occlusions can cause problems.

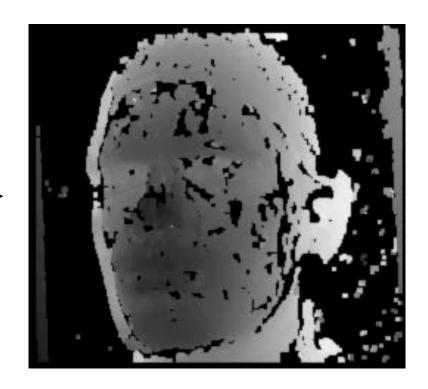




Disparity Map



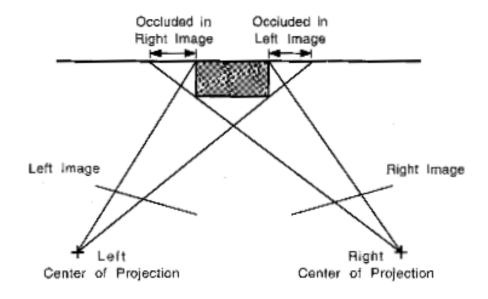




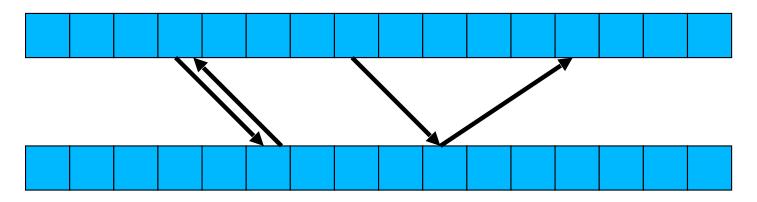
Black pixels: No disparity.

Occlusions

Some pixels have no corresponding pixel in the other image:



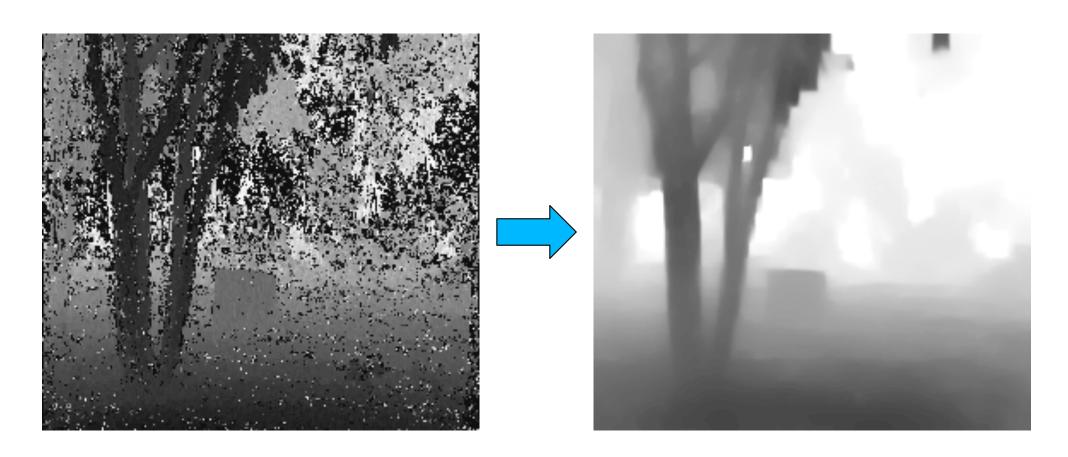
Left right consistency test:







Combining Disparity Maps



- Merging several disparity maps.
- Smoothing the resulting map.





Variational Approach

$$\mathcal{C} = \int s(w - w_0)^2 + \lambda_x (\frac{\partial w}{\partial x})^2 + \lambda_y (\frac{\partial w}{\partial y})^2$$



= Correlation score if w_0 has been measured, 0 otherwise.

$$\lambda_x = c_x f(\frac{\partial I}{\partial x})$$

$$\lambda_x = c_x f(\frac{\partial I}{\partial x})$$

$$\lambda_y = c_y f(\frac{\partial I}{\partial y})$$

$$f(x) = \begin{cases} 1 & \text{if } x < x_0 \\ \frac{x_1 - x}{x_1 - x_0} & \text{if } x_0 < x < x_1 \\ 0 & \text{if } x_1 < x \end{cases}$$

Solving the Variational Problem

Discretize the integral and solve a linear problem:

$$C = \sum_{ij} s_{ij} (w_{ij} - w_{0ij})^2 + \lambda_x \sum_{ij} (w_{i+1,j} - w_{i,j})^2 + \lambda_y \sum_{ij} (w_{i,j+1} - w_{i,j})^2$$

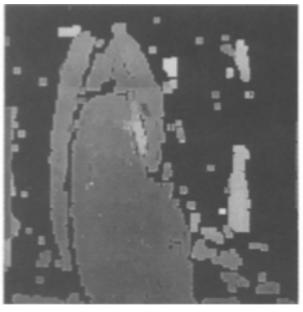
$$= (W - W_0)^t S(W - W_0) + W^t KW$$

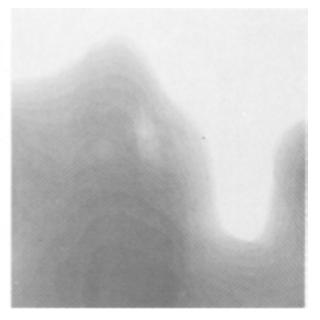
$$\Rightarrow \frac{\partial \mathcal{C}}{\partial W} = 0$$

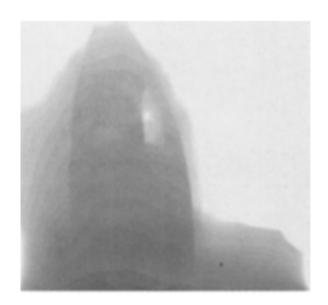
$$\Rightarrow (K+S)W = SW_0$$

Preserving Discontinuities









$$\lambda_x = f(\frac{\partial I}{\partial x})f(\frac{\partial w}{\partial x})^2$$

$$\lambda_x = f(\frac{\partial I}{\partial x}) f(\frac{\partial w}{\partial x})^2$$

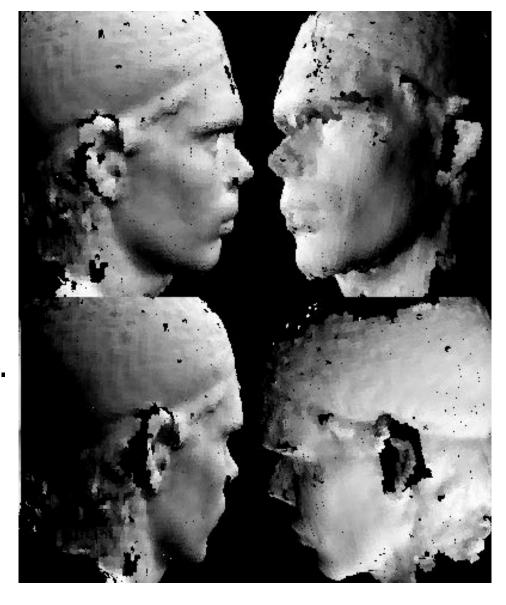
$$\lambda_y = f(\frac{\partial I}{\partial y}) f(\frac{\partial w}{\partial y})^2$$

Shape From Video



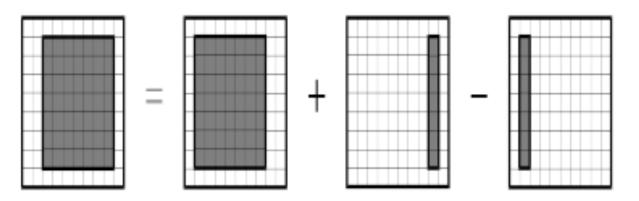
Treat consecutive images as stereo pairs.

- 1. Compute disparity maps.
- 2. Merge 3-D point clouds.
- 3. Represent as small patches.





Real-Time Implementation



$$C(x,y,d) \propto \frac{\sum_{i,j} I_1(x+i,y+j) \times I_2(x+d+i,y+j)}{\sqrt{\sum_{i,j} I_2(x+d+i,y+j)^2}}$$

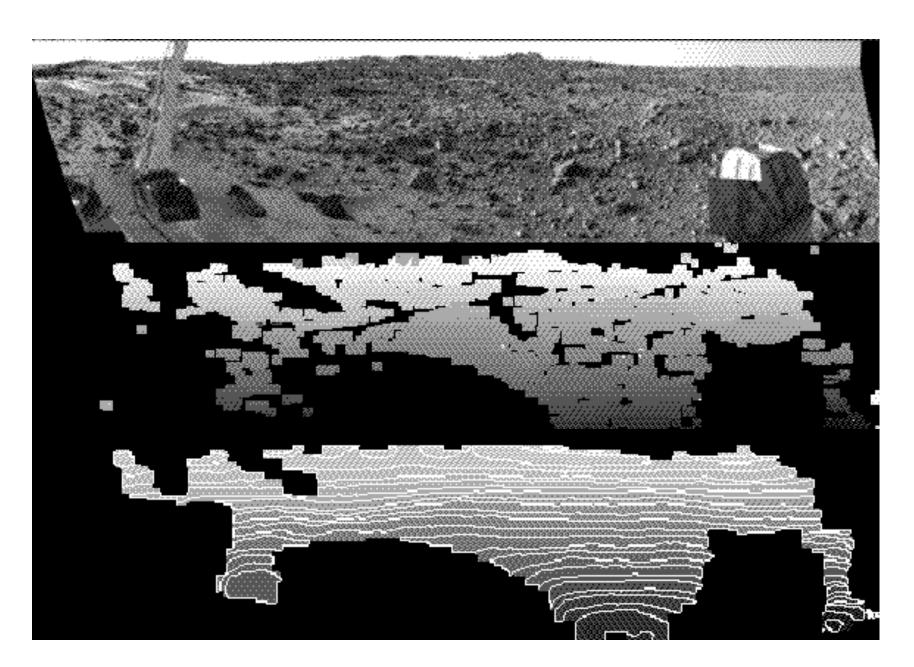
$$C(x+1,y,d) \propto \frac{\sum_{i,j} I_1(x+1+i,y+j) \times I_2(x+1+d+i,y+j)}{\sqrt{\sum_{i,j} I_2(x+1+d+i,y+j)^2}}$$

$$\propto \frac{\sum_{i',j} I_1(x+i',y+j) \times I_2(x+d+i',y+j)}{\sqrt{\sum_{i,j} I_2(x+d+i',y+j)^2}}$$

- Many duplicated computations.
- Can be implemented so that it is fast.
- Speed is independent from window size.



Then



1993: 256x256, 60 disps, 7 fps.

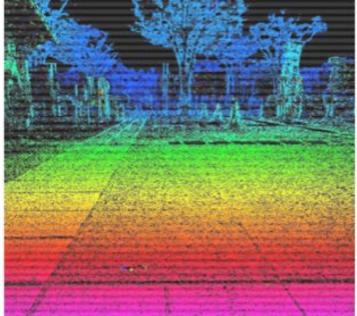




... And More Recently







Subaru's EyeSight System

http://www.gizmag.com/subaru-new-eyesight-stereoscopic-vision-system/14879/

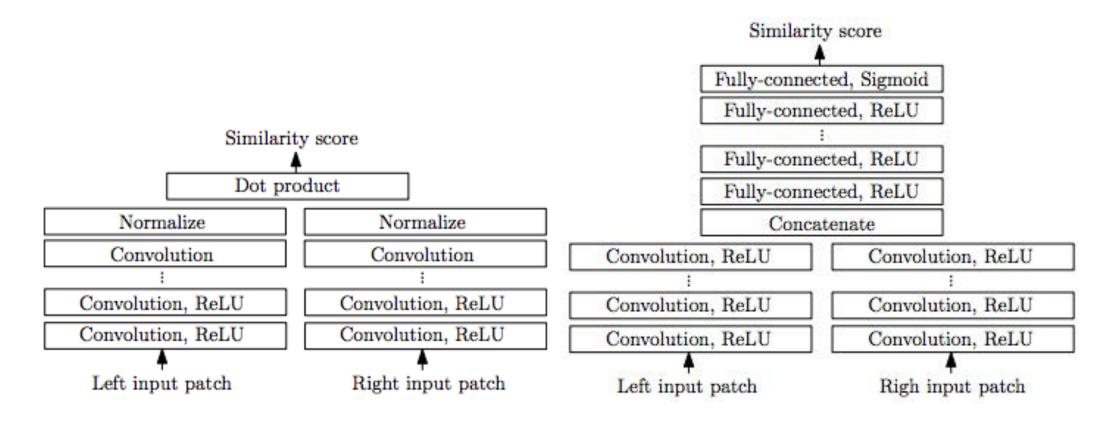
2011: 1312x688, 176 disps, 160 fps.





... and even More Recently

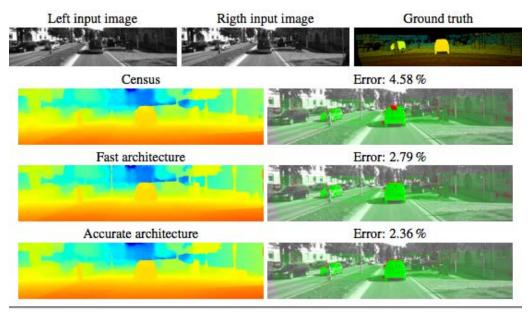
Replace Normalized Cross Correlation by Siamese nets designed to return a similarity score for potentially matching patches.

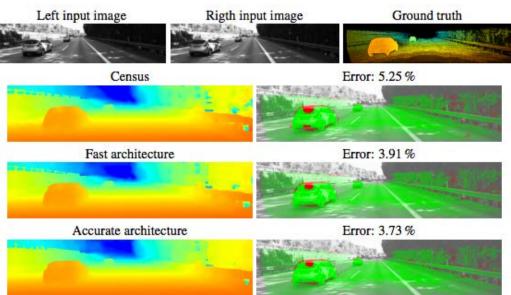






Comparative Results





Improved performance on test data but

- How well will it generalize to unseen images?
- Is it worth the much heavier computational load?

Time will tell.



Tesla's non LiDar Approach



https://www.therobotreport.com/researchers-back-teslas-non-lidar-approach-to-self-driving-cars/





Window Size

Small windows:

- Good precision
- Sensitive to noise

Large windows:

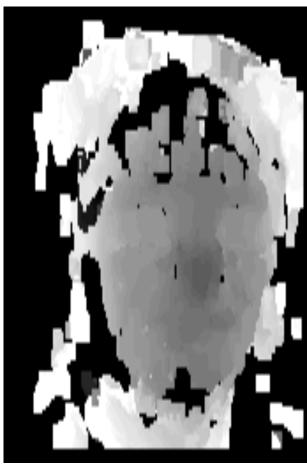
- Diminished precision
- Increased robustness to noise
- → Same kind of trade-off as for edge-detection.





Window Size







15x15

7x**7**





Scale-Space Revisited







Gaussian pyramid







Difference of Gaussians

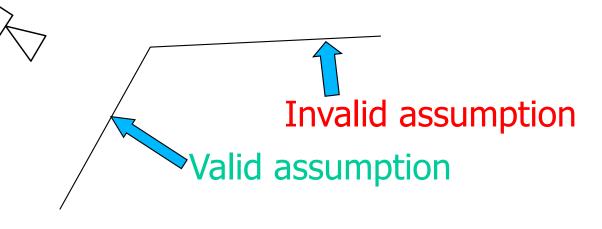
- Using a small window on a reduced image is equivalent to using a large one on the original image.
- Using difference of Gaussian images is an effective way of achieving normalization.
- →It becomes natural to use results obtained using low resolution images to guide the search at higher resolution.





Fronto-Parallel Assumption

 The disparity is assumed to be the same over the entire correlation window, which is equivalent to assuming constant depth.



→ Ok when the surface faces the camera but breaks down otherwise.

Multi-View Stereo



Multi-view reconstruction setup

—> Adjust correlation window shapes to handle orientation.

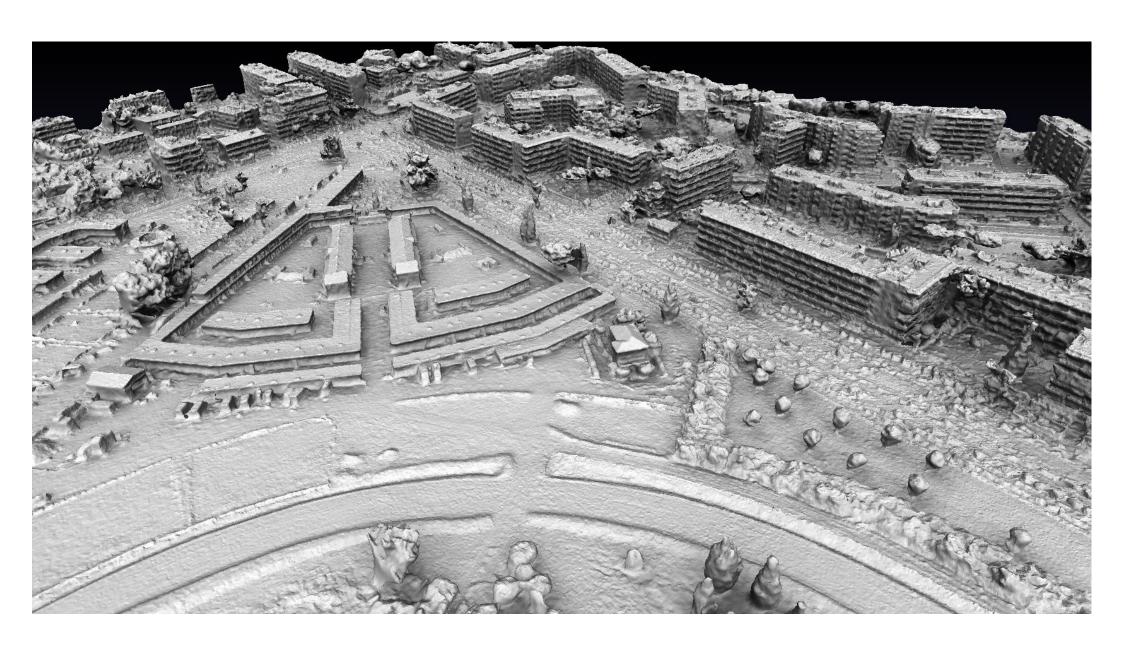


Text Silva Utalppood M Dd Model





MULTI-VIEW STEREO







Small Drones





SenseFly: www.sensefly.com

Gatewing: www.gatewing.com





Matterhorn



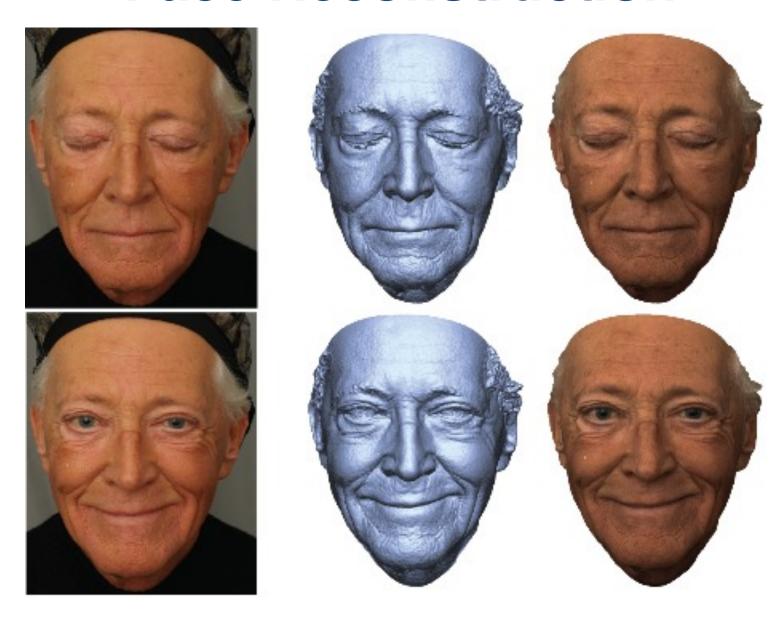
Drone: www.sensefly.com

Mapping: www.pix4d.com





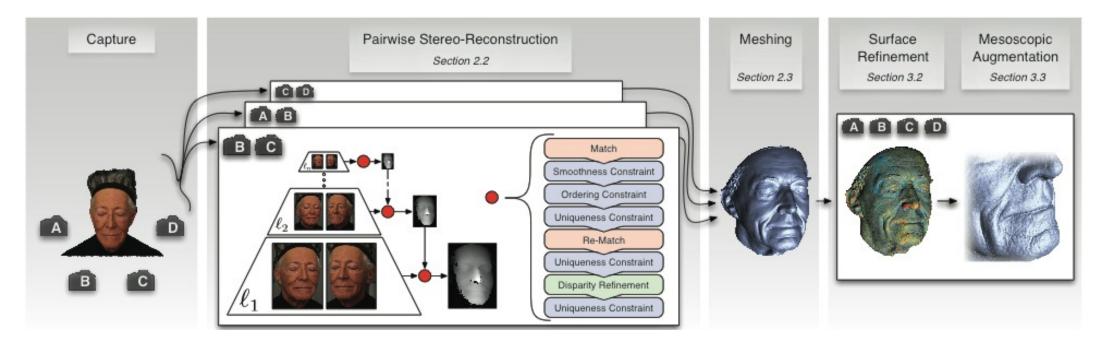
Face Reconstruction





Face Reconstruction









Dynamic Shape

Lightweight Binocular Facial Performance Capture under Uncontrolled Lighting

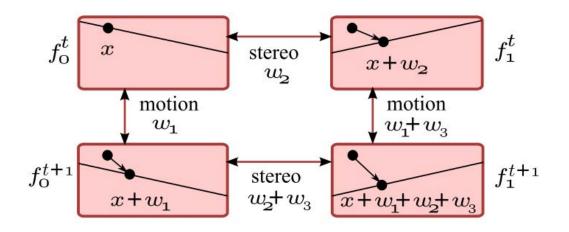
Levi Valgaerts ¹ Chenglei Wu ^{1,2} Andrés Bruhn ³ Hans-Peter Seidel ¹ Christian Theobalt ¹

MPI for Informatics
 Intel Visual Computing Institute
 University of Stuttgart

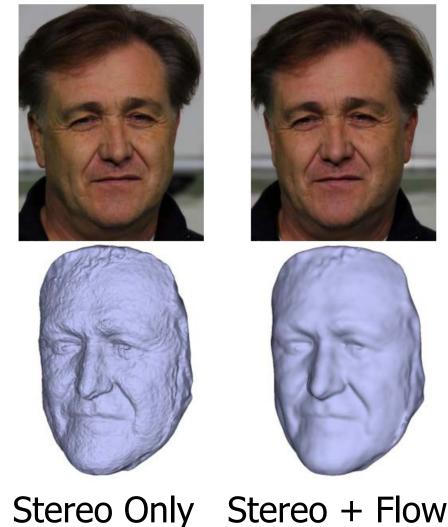




Scene Flow



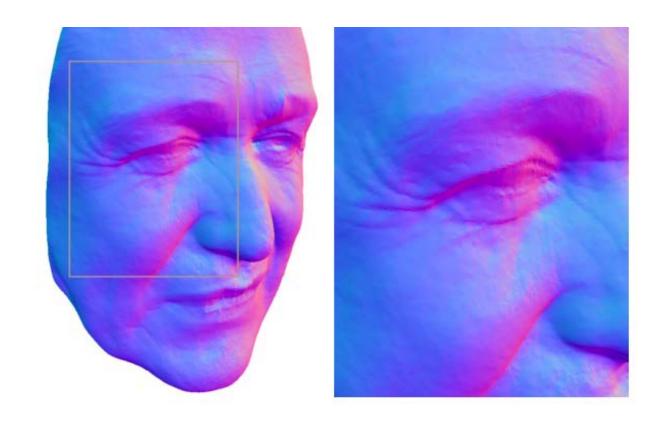
Correspondences across cameras and across time







Refining using Shape From Shading



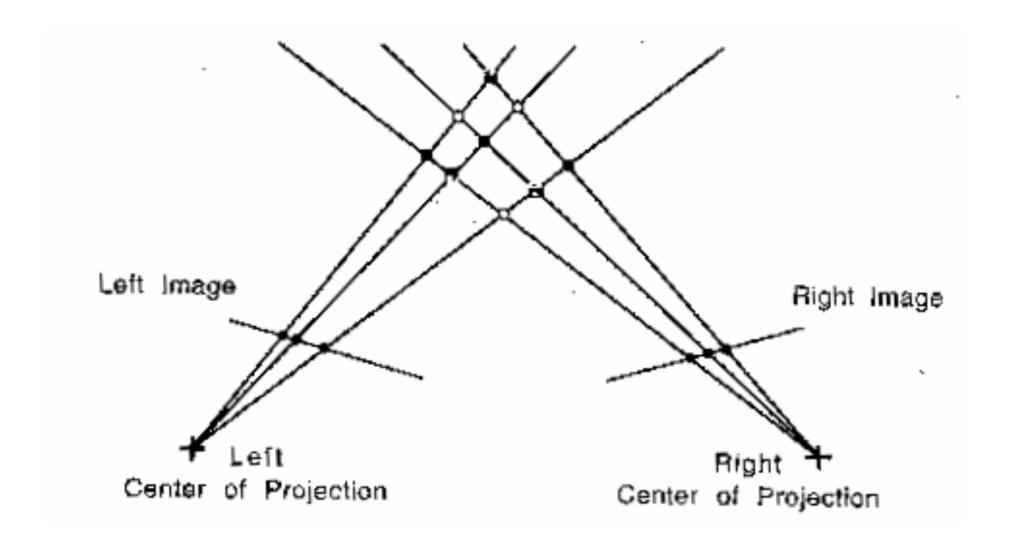
Shape-from-shading can be used to refine the shape and provide high-frequency details.







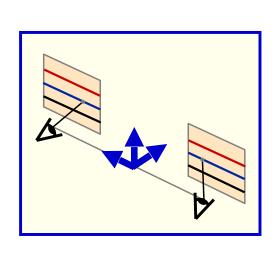
Uncertainty







Precision vs Baseline



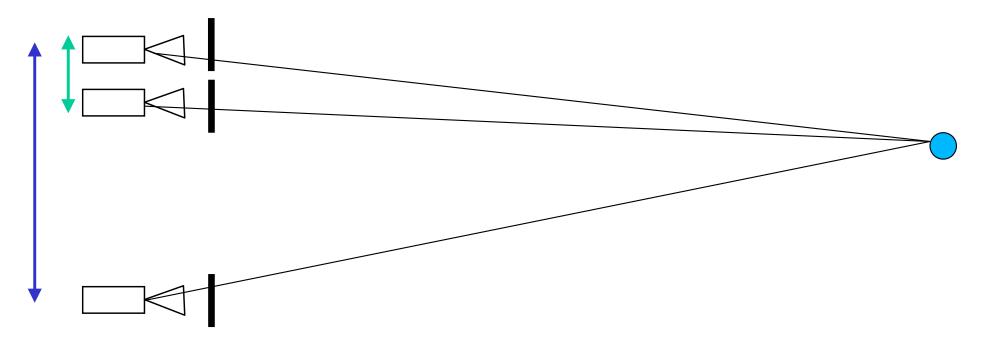
$$d = f\frac{b}{Z}$$

$$\Rightarrow Z = f\frac{b}{d}$$

$$\Rightarrow \frac{\delta Z}{\delta d} = -f\frac{b}{d^2} = -\frac{Z^2}{fb}$$

- Beyond a certain depth stereo stops being useful.
- Precision is inversely proportional to baseline length.

Short vs Long Baseline



Short baseline:

- Good matches
- Few occlusions
- Poor precision

Long baseline:

- Harder to match
- More occlusions
- Better precision





Mars Rover



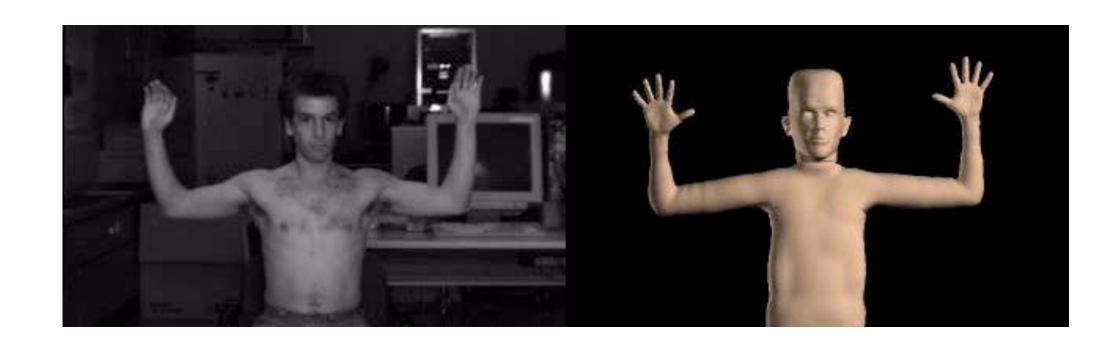


There are four cameras!





Video-Based Motion Capture

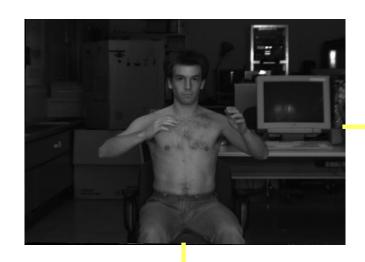


Fitting an articulated body model to stereo data.





Trinocular Stereo











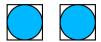


Multi-Camera Configurations





3 cameras give both robustness and precision







4 cameras give additional redundancy







3 cameras in a T arrangement allow the system to see vertical lines.

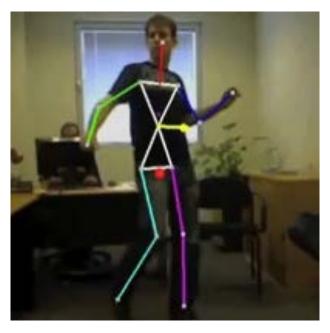






Kinect: Structured Light





- The Kinect camera projects a IR pattern and measures depth from its distortion.
- Same principle but the second camera is replaced by the projector.



Faces from Low-Resolution Videos



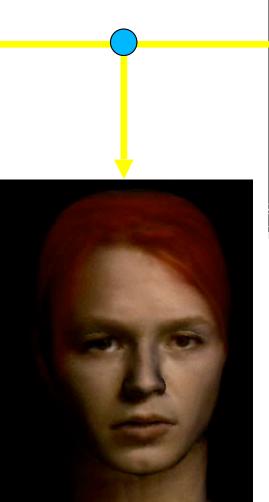
- No calibration data
- Relatively little texture
- Difficult lighting

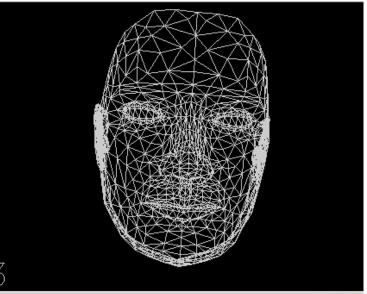




Simple Face Model

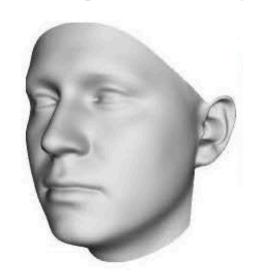


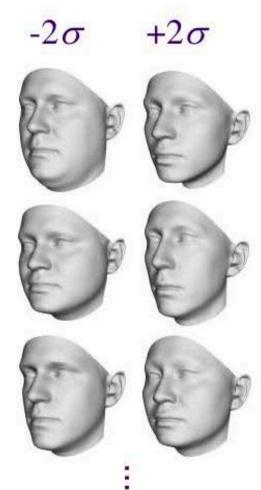






PCA Face Model





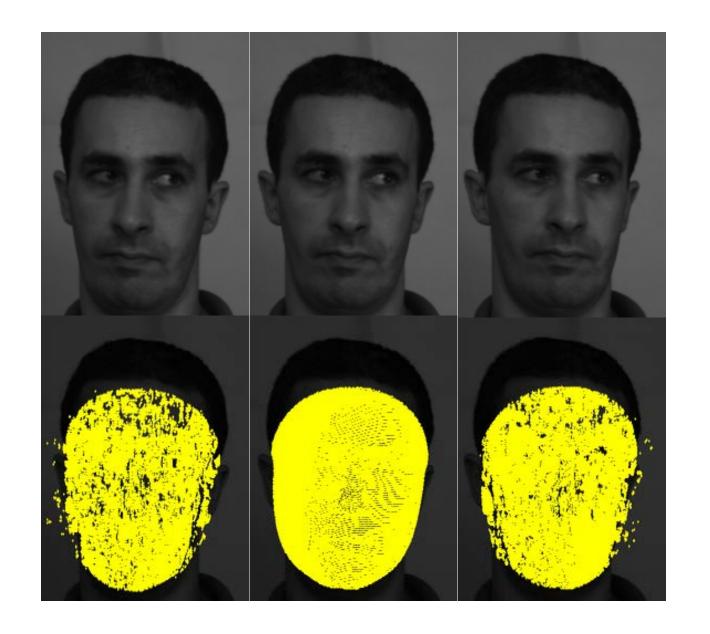
$$S = \bar{S} + \sum_{i=1}^{99} \alpha_i S_j$$
 Shape vector $\alpha_i : Shape coefficients$

 \overline{s} : Average shape

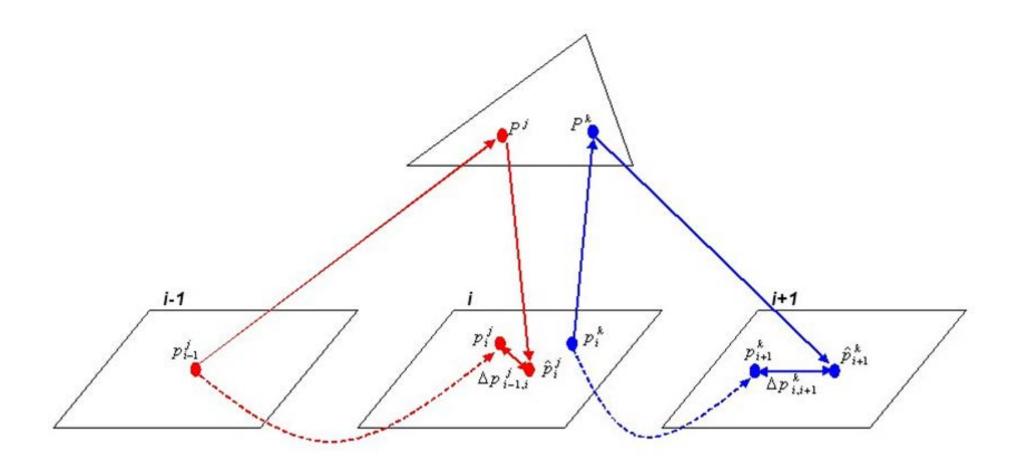
 α_i : Shape coefficients



Correspondences

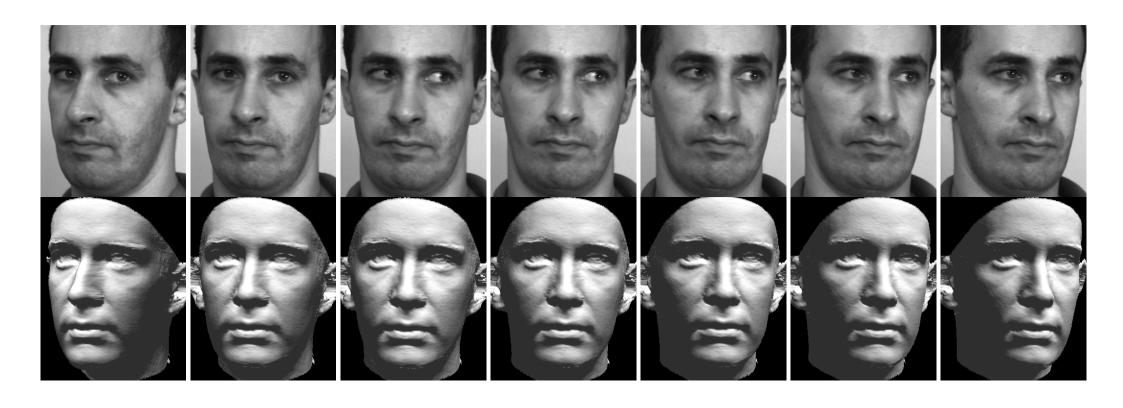


Transfer Function



$$F_3(A, C_{i-1}, C_i, C_{i+1}) = \sum_{j \in Q_{i-1}} \left\| \Delta p_{i-1,i}^j \right\|^2 + \sum_{k \in Q_i} \left\| \Delta p_{i,i+1}^k \right\|^2$$

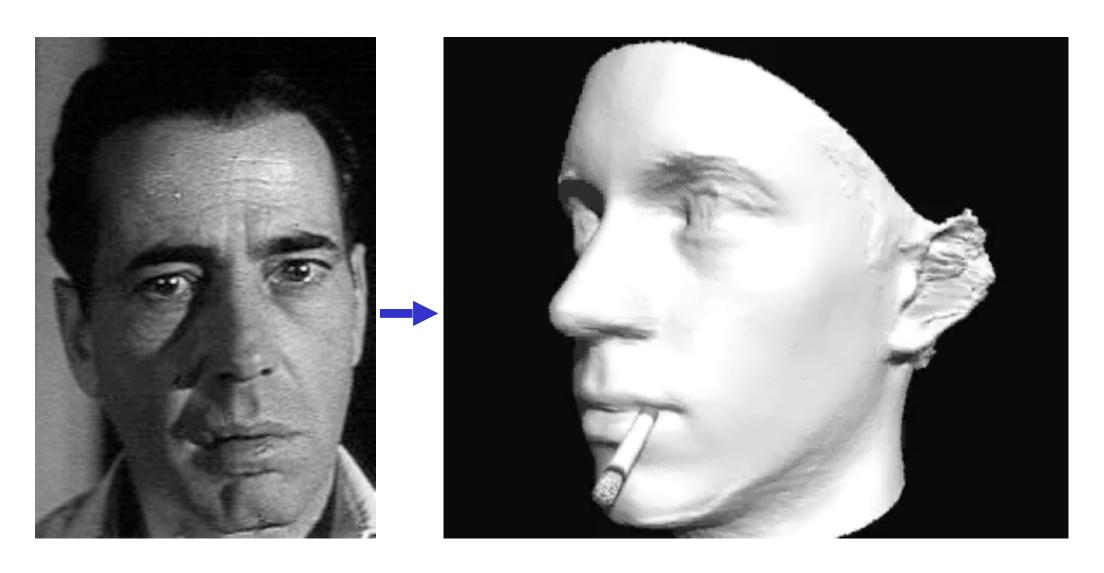
Model Based Bundle Adjustment



Adjusting the PCA coefficients to minimize the objective function yields an accurate face reconstruction from low-resolution images.



Model from Old Movie



Adjusting the PCA coefficients to minimize the objective function yields an accurate face reconstruction from low-resolution images.

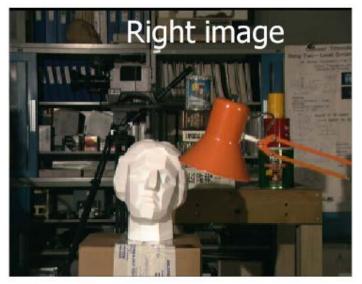


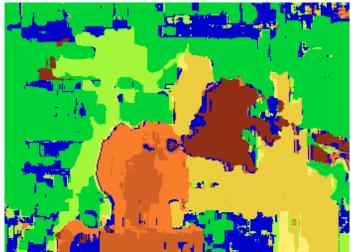
Limitations Of Window Based Methods





Ground truth



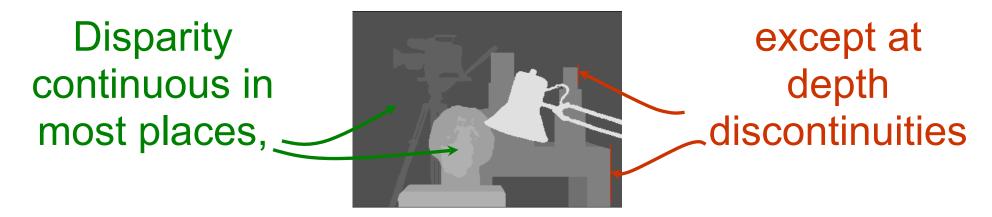


Correlation result





Energy Minimization

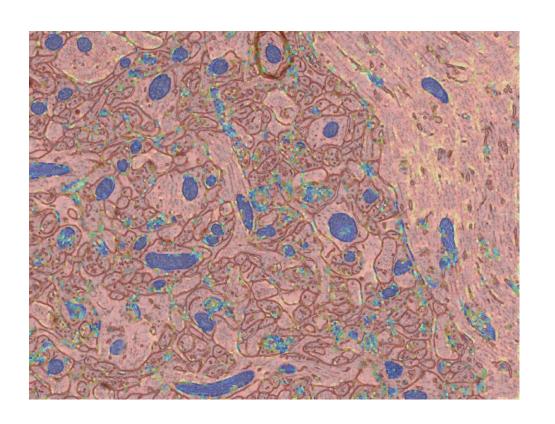


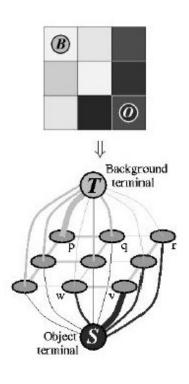
- 1. Matching pixels should have similar intensities.
- 2. Most nearby pixels should have similar disparities
- Minimize

$$\sum [I_2(x+D(x,y),y)-I_1(x,y)]^2 + \lambda \sum [D(x+1,y)-D(x,y)]^2 + \mu \sum [D(x,y+1)-D(x,y)]^2$$



Reminder: Graph-Based Segmentation





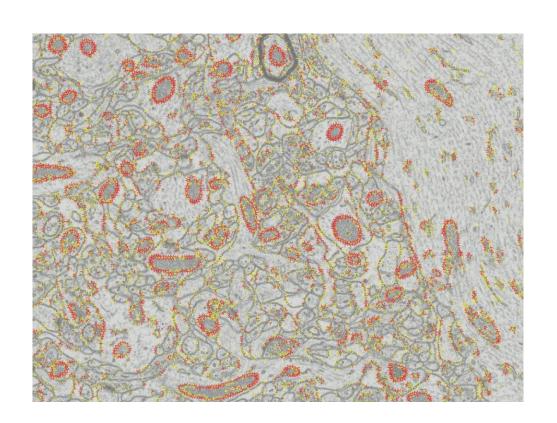
- A high probability of being a mitochondria can be represented by a strong edge connecting a supervoxel to the source and a weak one to the sink.
- And conversely for a low probability.

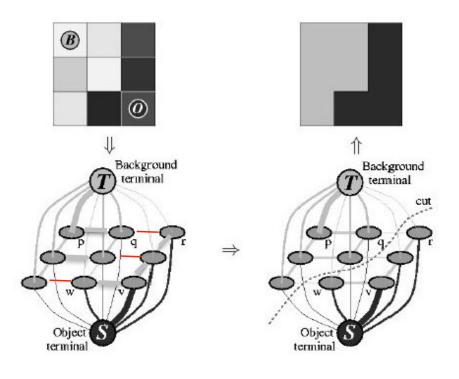






Reminder: Graph-Based Segmentation



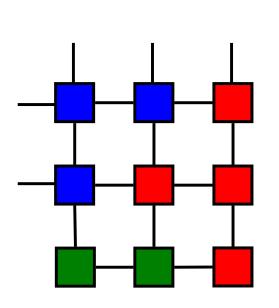


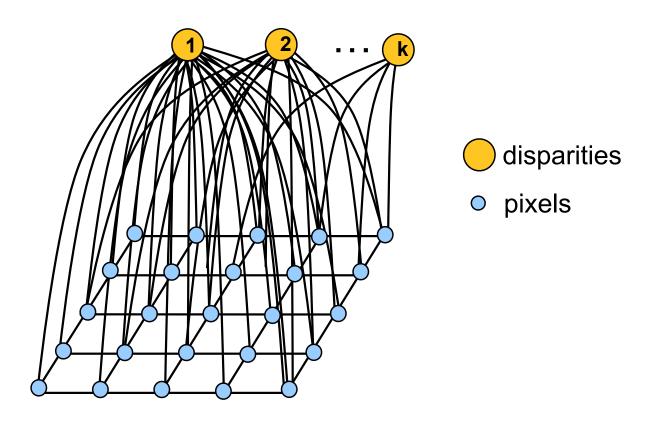
- Another classifier can be trained to assign a high-weight to edges connecting supervoxels belonging to the same class and a low one to others.
- Graph-cut can then be used to partition the pixels into separate regions.





Graph Cut for Stereo





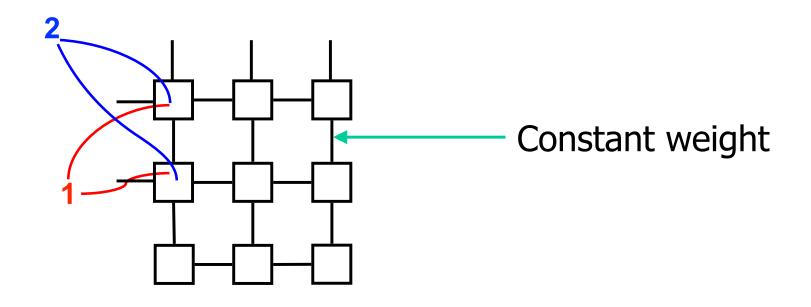
- 1. Stereo is a labeling problem. —> Use graph cut.
- 2. Connect each pixel to each possible disparity value.

(VLab





Assigning Edge Weights



Assign a weight that is inversely proportional to |I2(x+1,y)-I1(x,y)|Assign a weight that is inversely proportional to |I2(x+2,y)-I1(x,y)|.....





Minimizing the Objective Function

Minimize:

$$\sum [I_2(x+D(x,y),y)-I_1(x,y)]^2 + \lambda \sum [D(x+1,y)-D(x,y)]^2 + \mu \sum [D(x,y+1)-D(x,y)]^2$$

Graph cut algorithm:

- Guarantees an absolute minimum only when there are only two possible disparities.
- Effective heuristics (α -expansion, α - β swap) otherwise.





NCC vs Graph-Cut



Normalized correlation

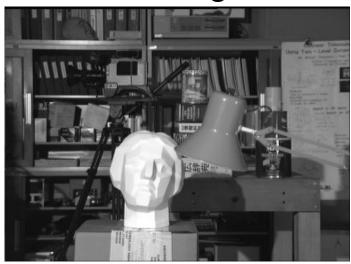
Graph Cut



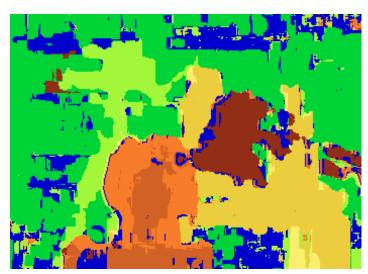


NCC vs Graph Cut

left image



Normalized correlation



true disparities



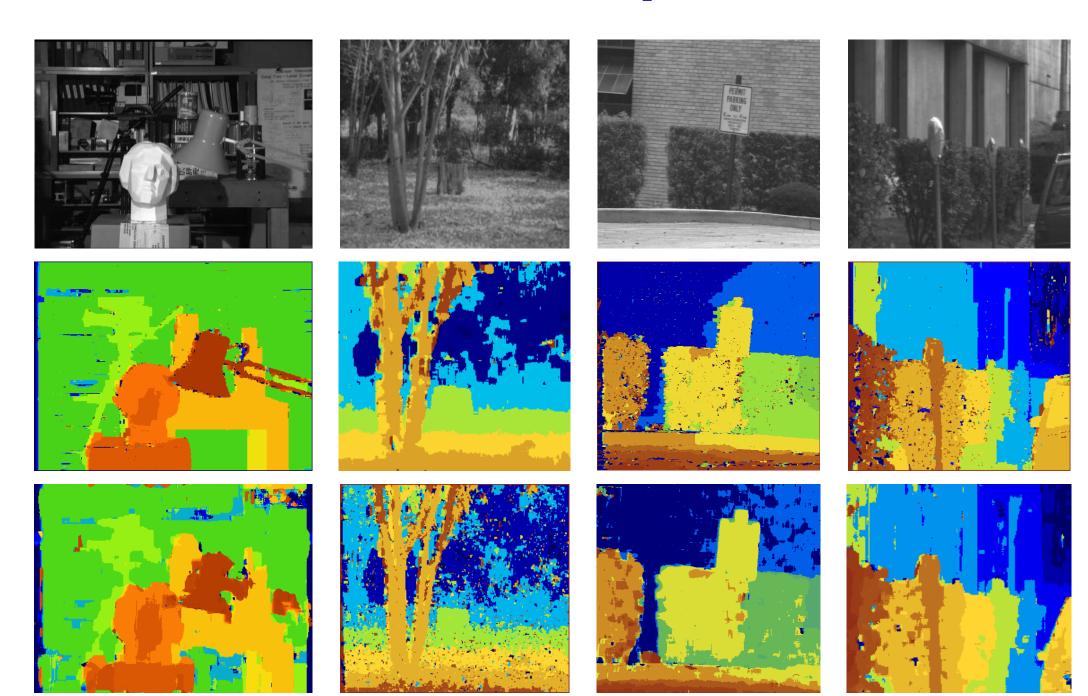
Graph Cuts







NCC vs Graph Cut



Strengths and Limitations

Strengths:

- Practical method for depth recovery.
- Runs in real-time on ordinary hardware.

Limitations:

- Requires multiple views.
- Only applicable to reasonably textured objects.



