## Motion Capture for full-body interaction



## 2. Posture reconstruction

- Minimal marker setup for full-body posture acquisition

- Head, spine and wrist orientations are recovered from multiple position markers (Phasespace LEDs)


## 2. Posture reconstruction (2)

## A two stages process :

- System Calibration
- Install the cameras so that they overlap and cover the whole volume of acquisition
- Register the cameras in a common world coordinate system with a calibration device
- Triangulation : a 3D marker position can be computed when it is
- visible by 2 cameras with 2D sensor (ViCON)
- visible by 3 cameras with 1D sensor (Phasespace)


Output of calibration phase: Known location of camera sensor Coordinate Systems in the World CS


Triangulation :
The known locations of a marker on the 2 sensors allow to build 2 lines that intersect at the marker location in world CS

## 2. Posture reconstruction (3) full body tracking

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INPUT: global location of all makers


World CS

1) CALIBRATION with a SKELETON model In the calibration posture: Determines the location of the body point (called effector) $\circ$ that should coincide with each sensor location
The position of the effector is computed in the LOCAL coordinate system of its associated JOINT.
e.g. a wrist marker determines the (constant) position of the wrist effector in the WRIST coordinate system

2) RUN-TIME : attract each effector towards Its associated marker position by optimizing The state of the JOINT local transformations

## 2. Posture reconstruction (4)

- Input: cloud of 3D marker positions $\left\{x_{i}\right\}$ \& body skeleton model
- Output: Body skeleton posture state expressed as a body global location and a set of joint values $\left\{\theta_{k}\right\}$
- Terminology:
- Forward Kinematics Problem (FK): the position of an effector $x_{i}$ as a function of $\theta_{k}$ is given by a set of highly non-linear equations: $x_{i}=F\left(\theta_{k}\right)$
- Inverse Kinematics Problem (IK): finding a solution to $\theta_{\mathrm{k}}=\mathrm{F}^{-1}\left(\mathrm{x}_{\mathrm{i}}\right)$


$$
\begin{array}{ll}
\text { FK: } & x=f_{1}\left(\theta_{1}, \theta_{2}\right)=L_{1} \cos \theta_{1}+L_{2} \cos \left(\theta_{1}+\theta_{2}\right) \\
& y=f_{2}\left(\theta_{1}, \theta_{2}\right)=L_{1} \sin \theta_{1}+L_{2} \sin \left(\theta_{1}+\theta_{2}\right) \\
\text { IK: } & \theta_{2}=\arccos \left(\frac{x^{2}+y^{2}-L_{1}^{2}-L_{2}^{2}}{2 L_{1} L_{2}}\right) \\
& \theta_{1}=\arctan \left(\frac{y}{x}\right)-\arctan \left(\frac{L_{2} \sin \theta_{2}}{L_{1}+L_{2} \cos \theta_{2}}\right)
\end{array}
$$

### 2.1 Two families of IK methods

- 2.1.1 Analytic IK:
- Possible for simple non-redundant cases, e.g. $\operatorname{dim}(x, y)=\operatorname{dim}\left(\theta_{1}, \theta_{2}\right)$
- The limb case [Korein, Badler, Tolani, Kallmann, Molla, Final-IK]:

- Input: position/orientation of the end effector (e.g. hand) - 3 dof (position) + 3dof (orientation)
- Output: joint state for base/mid/end
-3 dof (base) +2 dof (mid) +2 dof (end)
- One degree of redundancy: swivel angle

- Input: position/orientation of the head (HMD) and the two controllers
- Output: real-time full-body poses including steps to maintain balance

- How to handle the underconstrained problem [D-a-B] ?


The input dimension is $3 \times 6=18$, far smaller than the body pose space
Make pose design decisions based on the observation of human movement (but this may reflect an application-dependent choice):

- The head height impacts the pelvis height
- The pelvis height determines the leg state
- The leg state ensures that the center of mass floor projection lies within the feet or trigger a foot relocation.
- Distribute the head orientation over the spine until the pelvis that is used as a reference frame (its vertical axis remains mostly constant)
- Modulate the spine distribution by taking into account the relative location of hands with respect to the torso
- The hands control the arm including the clavicle, if necessary.


### 2.1 Two families of IK methods

- 2.1.2 Numeric Jacobian-based IK:
- Linearized the FK equations -> build matrix of partial derivatives = Jacobian
- Can handle redundant cases by computing the damped least-square inverse of the Jacobian
- Valid near the current state of the articulated system


Compute a posture variation $\Delta \theta_{\mathrm{k}}$ for a desired variation of the effector $\Delta \mathrm{x}_{\mathrm{i}}$

### 2.1 Two families of IK methods

- 2.1.3 comparison of IK methods on the simplest 1D case $Y_{E}=L_{0} \sin \theta$ The analytic solution is given by : $\theta=\arcsin \left(\right.$ Desired $\left.y_{E} / L_{0}\right)$

Jacobian-based approach: case with $\Delta y_{E}=$ Desired $y_{E}-y_{E}$


The linear approximation is only valid near the current state

### 2.1 Two families of IK methods

- 2.1.3 comparison of IK methods on the simplest 1D case $y_{E}=f(\theta)$

Jacobian-based approach: case with $\Delta y_{E}=$ clamped( Desired $y_{E}-y_{E}$ )


The jacobian-based with clamped $\Delta y_{E}$ has to be iterated until $\Delta y_{E}<\varepsilon$

### 2.1 Two families of IK methods

### 2.1.3 Comparison:

| IK method | Advantages | Drawbacks |
| :--- | :--- | :--- |
| Analytic IK <br> (Final-IK) | Fast | Non-Linear equations request body decomposition <br> into solvable equations, e.g. limbs, etc... |
| Jacobian-based IK | Handle redundancy <br> Minimum norm <br> posture variation <br> Whole-body solution <br> Priority concept | Linearized -> Iterative convergence due to local <br> validity of the solution |
| History-dependent, |  |  |

Other hybrid techniques: CCD (Cyclic Coordinate Descent), FABRIK (Forward And Backward Reaching IK)
Approaches leveraging on ML to map effector locations to a subset of poses

### 2.2 Jacobian-based IK with Priority levels

Redundancy allows to associate priority levels among effectors $A$ and $B$ as long as $\operatorname{Dim}(\theta) \geq \operatorname{Dim}($ effector A$)+\operatorname{Dim}($ effector $B)$

If the effector tasks conflict with each other, we have the guarantee of best possible achievement of the effector task with highest priority.
previous posture


Iterative convergence towards the achievement

High priority Coupled joints (e.g. spine)
Joint limits management with hard inequality constraints

Goal oriented soft constraints
built from marker data and associated with a priority level

Minimizing a cost function expressed in the joint space of the marker constraints

### 2.2 Jacobian-based IK with Priority levels (2)

Demonstrating the concept of priority enforcement [B04]: interactively moving the reach goal


Priority levels :

1. balance
2. feet
3. gaze
4. left hand reach
5. attraction toward rest posture

## [References]

[B04] P. Baerlocher, R. Boulic, «An Inverse Kinematic Architecture Enforcing an Arbitrary Number of Strict Priority Levels », The Visual Computer, Springer Verlag, 20(6), 2004, pp 402-417
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[Final-IK] http://www.root-motion.com/finalikdox/html/index.html
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