Neural Systems Unsupervised and Supervised Learning





Companion slides for the book *Bio-Inspired Artificial Intelligence: Theories, Methods, and Technologies* by Dario Floreano and Claudio Mattiussi, MIT Press

What you will learn today

- Elements of biological nervous systems
- Artificial neuron models
- Neural architectures
- Input encodings
- Unsupervised learning
 - Feature extraction and representations
 - Topological Maps
- Supervised learning
 - From error correction to backpropagation
 - Deep learning with autoencoders
 - Deep Convolutional Neural Networks

Do animals need nervous systems?



Not all animals have nervous systems; some use only chemical reactions Paramecium and sponge move, eat, escape, display habituation





Why Nervous Systems?



- 1) Faster reaction times = competitive advantage
- 2) Selective transmission of signals across distant areas = more complex bodies
- 3) Generation of non-reactive behaviors
- 4) Complex adaptation = survival in changing environments





Central Nervous System with Cortex



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Biological Neurons





Membrane Dynamics



This cycle lasts approximately 3-50 ms, depending on type of ion channels involved (Hodgkin and Huxley, 1952)



Types of Neurons



No. Net

How Do Neurons Communicate?





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How Do Neurons Learn?





- AFF

What Does Make Brains Different?

Components and behavior of individual neurons are very similar across animal species and, presumably, over evolutionary history (Parker, 1919)



Evolution of the brain seems to occur mainly in the **architecture**, that is how neurons are interconnected.

First classification of neurons by Cajal in 1911 was made according to their connectivity patterns



An Artificial Neural Network



A neural network communicates with the environments through input units and output units. All other elements are called internal or hidden units.

Units are linked by uni-directional connections.

A connection is characterized by a weight and a sign that transforms the signal.





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Neuron models





Some output functions







Neurons signal "familiarity"

The output of a neuron is a measure of similarity between its input pattern and its pattern of connection weights.

1. Output of a neuron in linear algebra notation:

$$y = a\left(\sum_{i}^{N} w_{i} x_{i}\right), \qquad a = 1 \longrightarrow y = \mathbf{w} \cdot \mathbf{x}$$

2. Distance between two vectors is:

$$\cos \vartheta = \frac{\mathbf{W} \cdot \mathbf{x}}{\|\mathbf{W}\| \|\mathbf{x}\|}, \qquad 0 \le \vartheta \le \pi$$

where the vector length is:

$$\|\mathbf{x}\| = \sqrt{\mathbf{x} \cdot \mathbf{x}} = \sqrt{x_1^2 + x_2^2 + \dots + x_n^2}$$

3. Output signals vector distance (familiarity) $\mathbf{w} \cdot \mathbf{x} = ||\mathbf{w}|| ||\mathbf{x}|| \cos \vartheta$





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Neural Receptive Fields

The **Receptive Field** indicates the input area subtended by a neuron *and* the input pattern that generates the strongest activation. RF can be visualized by plotting the weight pattern in the input space.





Neurons can act as classifiers

A binary neuron divides the input space in two regions, one where weighted input sum >=0 and one where weighted input sum <0.

The separation line is defined by the synaptic weights:





From Threshold to Bias unit

The threshold can be expressed as an additional weighted input from a special unit, known as bias unit, whose output is always -1.



- Easier to express/program
- Threshold is adaptable like other weights



Architectures



The second

Reservoir Architectures

Exploit rich dynamics in the reservoir of hundreds of randomly interconnected neurons with low connectivity (0.01, e.g)



Liquid State Machines (Maas et al, 2002) Echo State Networks (Jaeger et Haas, 2004)



Local vs Distributed Input Encoding



LOCAL

One neuron stands for one item a.k.a. «Grandmother neurons» Scalability problem

DISTRIBUTED Neurons encode features One neuron may stand for >1 item One item may activate >1 neuron Robust to damage



Normalisation of sensory input





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Filter convolution to capture spatial relationships



Learning

Learning is experience-dependent modification of connection weights



Learning is a gradual process and requires many input-output comparisons



Learning cycle

- 1. Initialize weights (e.g., random values from normal distribution)
- 2. Present randomly selected input pattern to network
- 3. Compute values of output units
- 4. Compute weight modifications
- 5. Update weights

Standard weight update

$$w_{ij}^{t} = w_{ij}^{t-1} + \eta \Delta w_{ij}$$

learning rate [0,1]

6. Repeat from 2. until weights do not change anymore





Learning modalities

Unsupervised learning

Supervised learning

Reinforcement learning (next week)

Evolution (next week)

Evolution and learning (next week)



Unsupervised learning: what for?



Input: x (images, signals, text, etc.)

Categories (labels): none

Goal: learn compact structure (features) that describes input



Unsupervised learning

The weight change depends only on the activity of the pre-synaptic and of the postsynaptic neurons

$$\Delta w_{ij} = x_j y_i$$

Unsupervised learning is used for

- Detecting statistical features of the input distribution
- Data compression and reconstruction
- Detect topological relationships in the input data
- Memorization



Oja's learning rule

Hebb's rule suffers from **self-amplification** (unbounded growth of weights), **but b**iological synapses cannot grow indefinitely

Oja (1982) introduced self-limiting growth factor in Hebb rule



X2

As a result, the weight vector develops along the direction of maximal variance of the input distribution.

Neuron learns **how familar** a new pattern is: input patterns that are closer to this vector elict stronger response than patterns that are far away.



Principal Component Analysis

Oja rule for N output units develops weights that span the sub-space of the N principal components of the input distribution.

Sanger rule for N output units develops weights that correspond to the N principal components of the input distribution.

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Do brains compute PCA?

An Oja network with multiple output units exposed to a large set of natural images develops *receptive fields* similar to those found in the visual cortex of all mammals [Hancock et al., 1992]







Mammals are born with pre-formed hierarchically-organized feature detectors. But they never saw anything in the womb: how can it be?





Multilayer Feature Detection

Linsker (1986)



Topologically restricted connectivity

Linear activation function

Plain Hebbian learning with weight clipping at *w*+ and *w*-

Learn one layer at a time, starting from lower layer



Emerging Receptive Fields

Linsker (1986)







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Neighbouring neurons respond to similar patterns with gradual transitions

The visual cortex is organized in specialized modules. Each module is composed by a series of columns of neurons. Neurons respond to bars at different orientation

 The bar orientation gradually varies along the column.
Neighbouring columns correspond to neighbouring areas of the retina (**retinotopic maps**).

A similar structure exists in the auditory cortex (**tonotopic maps**).






Sensory-Motor Body Map



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Lateral connections to neighbouring neurons

Cortical neurons display the following pattern of *projective* connectivity:

- up to 50-100 μm radius = excitatory
- up tp 200-500 μ m radius = inhibitory
- up to few cm radius = slightly excitatory

Also known as Mexican Hat distribution

In a neural network, we can approximate the Mexican hat with a bipolar weight distribution.



Formation of neural bubbles around strongest input



Self-Organizing Topological Maps

Kohonen (1982)

Let's apply Hebb rule to layer of such laterally connected neurons

$$y_i = \Phi(A_i) = \begin{cases} 1 & \text{if within neighbourhood } \Psi(y) \\ 0 & \text{otherwise} \end{cases}$$

$$\Delta w_{ij} = \eta y_i \left(x_j - \Psi(y_i) w_{ij} \right) \qquad \qquad \Psi(y_i) = \begin{cases} \psi & \text{if } y_i = 1\\ 0 & \text{if } y_i = 0 \end{cases}$$

If we set $\Psi(y)$ equal to the learning rate η , then the learning rule becomes:

$$\Delta w_{ij} = \begin{cases} \eta (x_j - w_{ij}) & \text{if } y_i = 1\\ 0 & \text{if } y_i = 0 \end{cases} \quad \text{and} \quad \mathbf{w}_i^{t+1} = \begin{cases} \mathbf{w}_i^t + \eta (\mathbf{x} - \mathbf{w}_i^t) & \text{if } y_i = 1\\ \mathbf{w}_i^t & \text{if } y_i = 0 \end{cases}$$

1. The weights are changed only for the neurons that are geographically near the neuron with the highest activity,

2. The change moves the weight vector towards the input pattern.

Neighborhood function

The neighbourhood size $\Psi(y)$ is a critical aspect of map self-organization. It should be large at the beginning of training to give a chance to all neurons to change weights and gradually shrink



Example of self-organizing map





Self-organization phases



Supervised learning: what for



Input: x (images, signals, text, etc.)

Category (label): y (eat, wear, wear, eat, wear, eat)

Goal: learn mapping between input data and labels



Supervised Learning

• Teacher provides desired responses for a set of training patterns

• Synaptic weights are modified in order to reduce the **error** between the output *y* and its desired output *t* (a.k.a. teaching input)

Widrow-Hoff defined the error with the symbol delta: $\delta_i = t_i - y_i$ (a.k.a. delta rule)





Error (loss) function

The delta rule modifies the weights to descend the gradient of the error function





Linear Separability

Perceptrons can solve only problems whose input/output space is **linearly separable**.

Several real world problems are not linearly separable.





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Multi-layer Perceptron (MLP)

Multi-layer neural networks can solve problems that are not linearly separable
Hidden units re-map input space into a space which can be linearly separated by output units.



Output units "look" at regions (in/out)



Output Function in MLP

• Multi-layer networks should not use linear output functions because a linear transformation of a linear transformation remains a linear transformation.

• Therefore, such a network would be equivalent to a network with a single layer





Back-propagation of Error

In a simple perceptron, it is easy to change the weights to minimize the error between output of the network and desired output.



$$\begin{split} \delta_{i} &= t_{i} - y_{i} & \Delta w_{ij} = \eta \delta_{i} x_{j} \\ \delta_{i} &= (t_{i} - y_{i}) \dot{\Phi}(A_{i}) & \text{in the case of non-linear} \\ \text{output functions, add derivative of output} \end{split}$$

In a multilayer network, what is the error of the hidden units? This information is needed to change the weights between input units and hidden units.

The idea suggested by Rumelhart et al. in 1986 is to propagate the error of the output units backward to the hidden units through the connection weights:

$$\delta_{j} = \dot{\Phi}(A_{j}) \sum_{i} w_{ij} \delta_{i}$$

Once we have the error for the hidden units, we can change the lower layer of connection weights with the same formula used for the upper layer.



Algorithm





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Using Back-Propagation

Error space can be complex in multilayer networks: local minima and flat areas $$_{\rm Ew_{A}}$$



1. Large learning rate: take large steps in the direction of the gradient descent

2. Momentum: add direction component from last update $\Delta w_{ii}^{t} = \eta \delta_{i} + \alpha \Delta w_{ii}^{t-1}$

3. Additive constant: keep moving when no gradient $\delta_i^{\mu} = (\dot{\Phi} + k)(t_i^{\mu} - y_i^{\mu})$



Over-fitting





The second

Time Series

Extraction of time-dependent features is necessary for time-series analysis





NETtalk

A neural network that learns to read aloud written text: •7 x 29 input units encode characters within a 7-position window(TDNN) •26 output units encode english phonemes •approx. 80 hidden units

Training on 1000-word text, reads any text with 95% accuracy

Learns like humans: segmentation, bla-bla, short words, long words



[Sejnowski & Rosenberg, 1987]



Chemical sensors of volatile molecules

The human brain recognizes millions of smell types by combining responses of only 10,000 receptors. Smell detection is a multi-billion industry (food, cosmetics, medicine, environment monitoring...). Human detection: costly, fatigue, history, aging, subjective.







Substance recognition from chemical sensors



[Keller et al., 1994]

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Deep vs. shallow neural networks

Compact distributed encoding (smallest possible number of computing elements) = better generalization

Compared to compact network of k layers, a network of k-1 layers requires exponentially larger number of computing elements to achieve same learning error, and therefore has worse generalisation



Backpropagation in deep networks

Backpropagation yields poor results when applied to networks of many layers (k>3)

The problem lies in poor gradient estimation in the lower layers of the neural network, leading to smaller gradients and thus small weight modifications



Not all connections are shown



Features



What do they have in common?

 $\sim - 0$



"Deep learning", one layer at a time

Unsupervised training of low layers to generate structure of increasingly complex representations + Supervised training of top layer





Unsupervised learning with autoencoders

PCA are not good for unsupervised learning in deep networks because PCA is a linear transformation

Autoencoders are supervised networks (e.g., Back-prop) that learn to reproduce the input pattern on the output layer. Usually, they have smaller set of hidden units (*encoding units*) to generate a compressed representation, which spans the same space of PCA representation, but can use non-linear units.



Not all connections are shown



Denoising Autoencoders (dropout)

Identity coding problem arises *w*hen encoding units are equal or larger than input units



To prevent identity encoding, use *denoising autoencoders* (Vincent et al. 2008): corrupt input by randomly switching off 50% of units while keeping teaching output equal to uncorrupted input



Not all connections are shown

Deep training

input OOO ... O































Supervised training of top layer


Supervised fine tuning of entire network



Convolutional Neural Networks

Instead of training weights from all input units to each detector (filter), as autoencoders do, train only weights from few neighboring input units to each detector and convolve image to generate activations of the next layer



Filter convolution for 2D images



6 x 6 image

Each filter is a local detector



Filter 1



6 x 6 image

1	-1	-1	
-1	1	-1	
-1	-1	1	

Filter 1

If stride=2

1	0	0	0	0	1
0	1	0	0	1	0
0	0	1	1	0	0
1	0	0	0	1	0
0	1	0	0	1	0
0	0	1	0	1	0

3 -3

6 x 6 image



Filter 1





6 x 6 image



-1	1	-1	
-1	1	-1	Filter 2
-1	1	-1	





6 x 6 image

Repeat this for each filter





Add non-linearity to each value in the block, e.g. ReLU function (Rectified Linear Unit)



Subsampling by pooling



Typical Convolutional Neural Network

Filters are learned to minimize the error (loss) function of the output



https://en.wikipedia.org/wiki/Convolutional_neural_network Image by Aphex34 - Own work, CC BY-SA 4.0, https://commons.wikimedia.org/w/index.php?curid=45679374

Learning object classification and positions



S. Ren, K. He, R. Girshick and J. Sun (2017), *IEEE Transactions on Pattern Analysis and Machine Intelligence*, doi: 10.1109/TPAMI.2016.2577031.

Bird detection and deterrence on buildings



SwissTech building, EPF Lausanne

- City pigeon excrements damage buildings and facades
- Cleaning and repair cost up to 1.1 billion USD per year in USA (Pimentel et al, 2000)
- Pigeon droppings are reservoirs of dangerous zoonotic pathogens (Haag-Wackernagel, 2004)

Current solutions



- Require human operator, or
- Are too loud for operation in urban environment, or
- Are dangerous for animals, or
- Are ineffective





F. Schiano, D. Natter, D. Zambrano and D. Floreano (2022) Autonomous Detection and Deterrence of Pigeons on Buildings by Drones, *IEEE Access*, 10, 1745-1755, doi: 10.1109/ACCESS.2021.3137031.



The system in action

Ground camera view

Drone onboard camera view

Without drone system, pigeon flock stay on roof up to 3 hours With drone system, pigeon flock stays up to 4 minutes