

Contents

- 1. What is the problem; congestion collapse
 - 2. Efficiency versus Fairness
 - 3. Definitions of fairness
- 4. Additive Increase Multiplicative Decrease (AIMD)
 - 5. Slow start



1. Congestion Collapse

In October of '86, the Internet had the first of what became a series of 'congestion collapses'. During this period, the data throughput from LBL to UC Berkeley (sites separated by 400 yards and three IMP hops) dropped from 32 Kbps to 40 bps. Mike Karels¹ and I were fascinated by this sudden factor-of-thousand drop

Jacobson, Van. "Congestion avoidance and control." *ACM SIGCOMM computer communication review*. Vol. 18. No. 4. ACM, 1988.

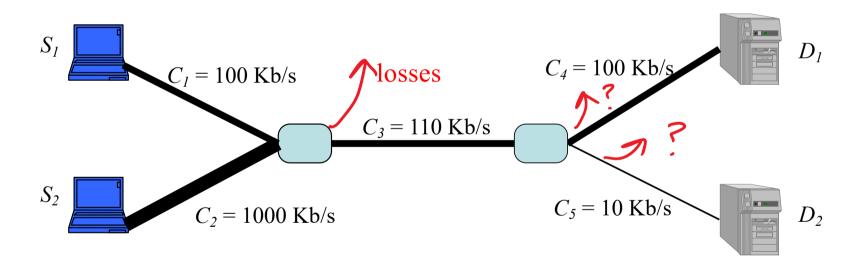


How much will S_1 send to D_1 ? S_2 to D_2 ?

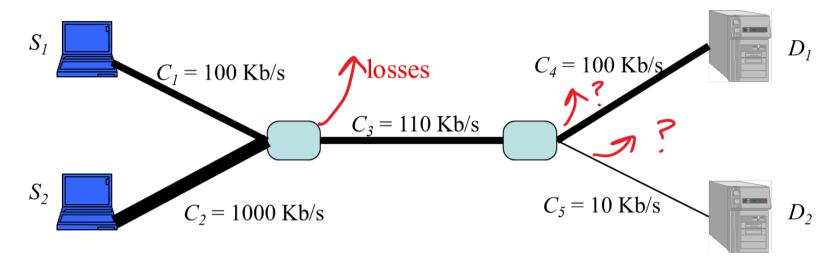
Network may lose some packets;

Assume greedy sources (i.e. send as much as they want)

Assume loss is proportional to submitted traffic and links can be fully utilized



S_1 to D_1 rate is ...



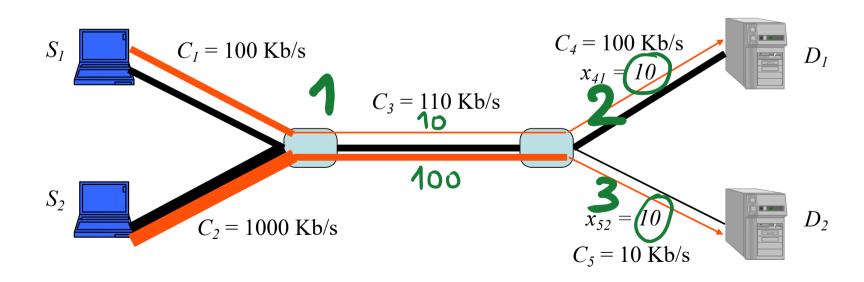
- A. 10 kb/s
- B. 50 kb/s
- C. 100 kb/s
- D. I don't know

Answer A: Ratio of accepted traffic at 1 is $\frac{110}{100+1000} = 10\%$

Ratio of accepted traffic at 2 is 100%

Ratio of accepted traffic at 3 is $\frac{10}{100} = 10\%$

Both sources send at 10 kb/s!



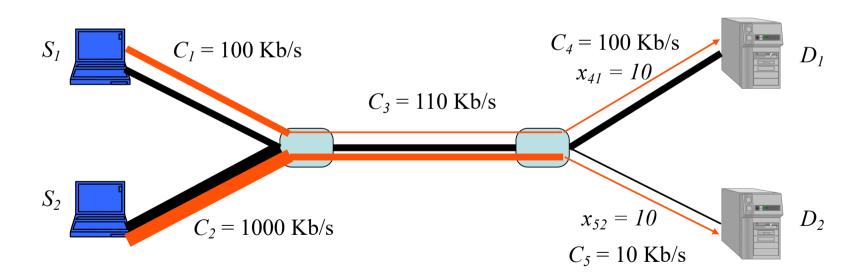
Take home message Greedy Sources May Be Inefficient

A better allocation is:

 S_1 : 100 kb/s

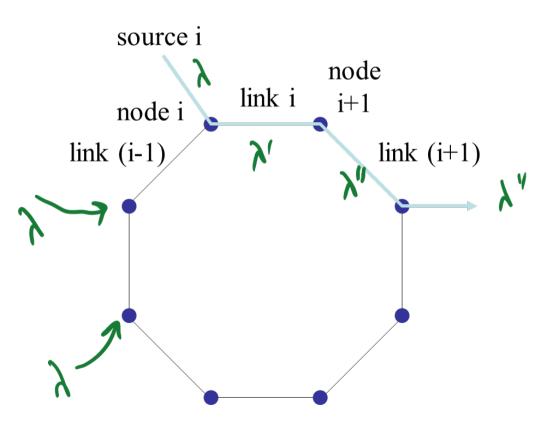
 S_2 : 10 kb/s

The problem was that S₂ sent too much (but did not know)



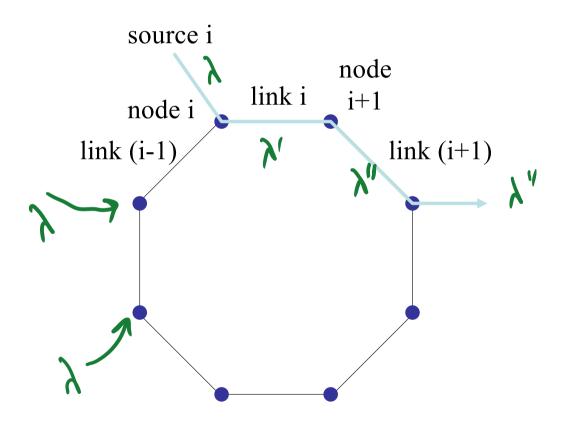
How much can node *i* send to its destination ?

Source i uses two links, all of same capacity c At every node there is a source – all sources at same rate



How much can node *i* send to its destination ?

If $\lambda < \frac{c}{2}$ there is no loss (in this simple model) and $\lambda'' = \lambda$



How much can node *i* send to its destination?

If $\lambda > \frac{c}{2}$ there is some loss (in this simple model)

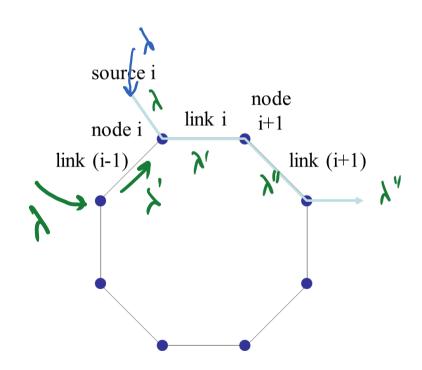
Ratio of accepted traffic at one node is $\frac{c}{\lambda + \lambda'}$

Therefore

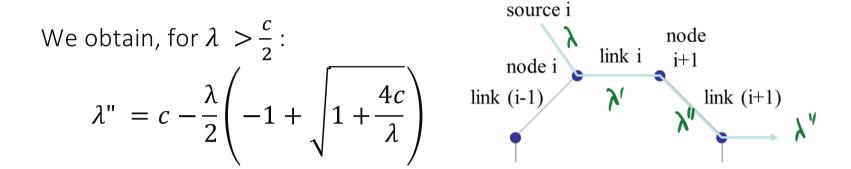
$$\lambda' = \frac{c}{\lambda + \lambda'} \lambda \quad (1)$$
$$\lambda'' = \frac{c}{\lambda + \lambda'} \lambda' \quad (2)$$

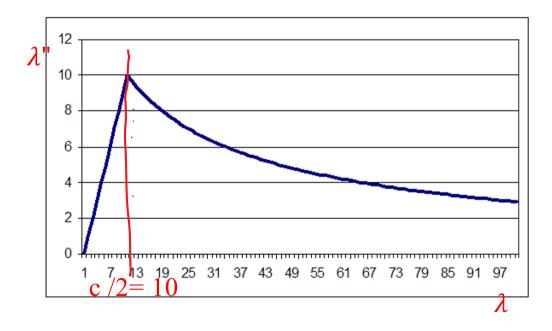
$$\lambda'' = \frac{c}{\lambda + \lambda'} \lambda' \quad (2)$$

Solve for λ', λ'' from (1),(2)



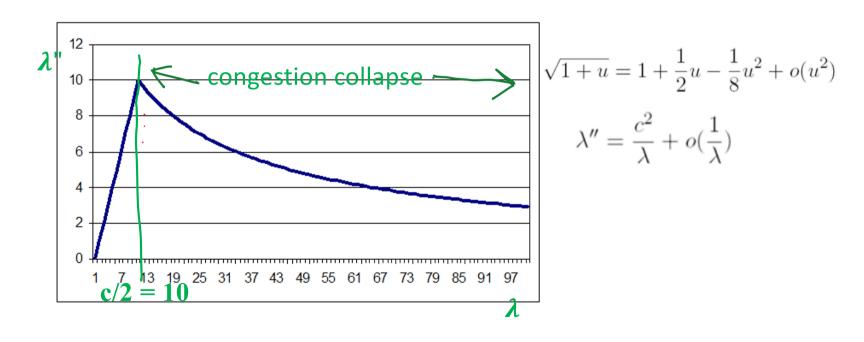
How much can node i send to its destination?





For large offered traffic λ , the limit of useful work is 0

We obtain, for
$$\lambda > \frac{c}{2}$$
:
$$\lambda = c - \frac{\lambda}{2} \left(-1 + \sqrt{1 + \frac{4c}{\lambda}} \right)$$
source i
node i
link i
link (i-1)
link (i+1)
link (i+1)

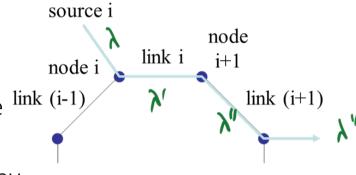


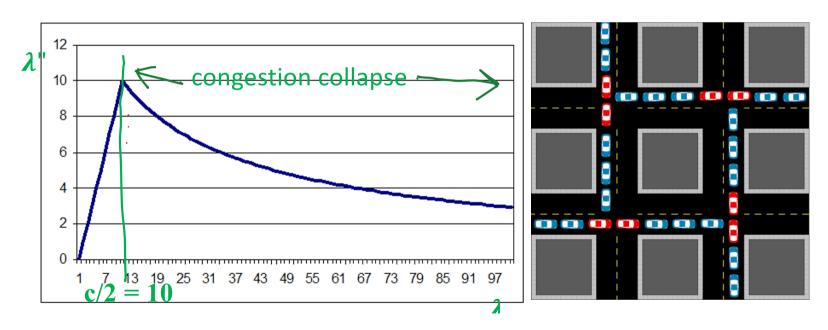
Take-Home Message 2

This *is* congestion collapse, i.e. : as the offered load increases, the total throughput decreases

Sources should limit their rates to adapt it to the link (i-1) network condition

Otherwise inefficiency or congestion collapse may occur



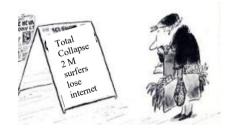


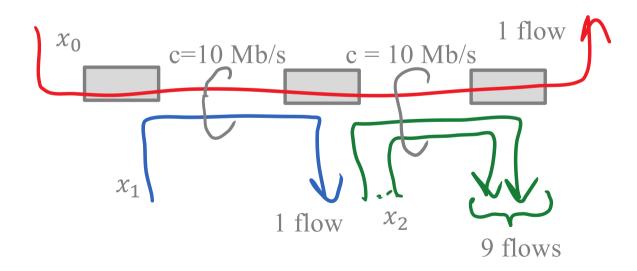
2. Efficiency vs Fairness

A network should be organized so as to avoid inefficiency

However, being maximally efficient may be a problem

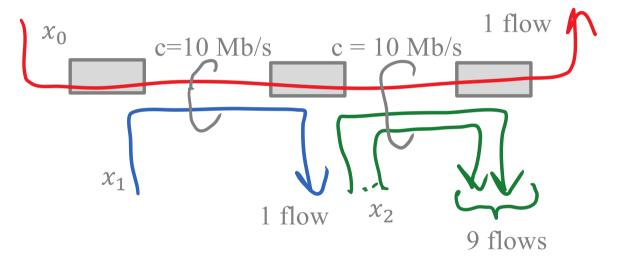
Example: what is the maximum total throughput in this network?





The maximum throughput is ...

- A. 5 Mb/s
- B. 10 Mb/s
- C. 20 Mb/s
- D. None of the above
- E. I don't know

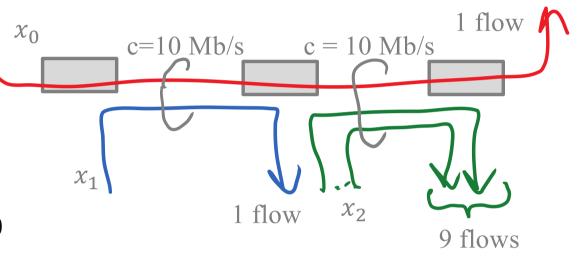


Answer C

Total throughput $\theta = x_0 + x_1 + 9x_2$ Maximize $\theta = x_0 + x_1 + 9x_2$

subject to $x_0 + x_1 \le 10$, $x_0 + 9x_2 \le 10$

 $\text{over } x_0 \geq 0, x_1 \geq 0 \ x_2 \geq 0$



The max can be obtained by linear programming, or directly here by inspection:

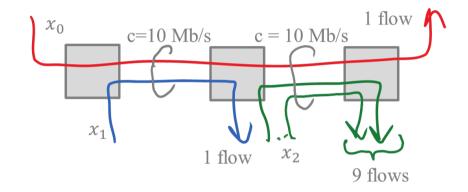
 $\theta \leq 20$ because $x_0 + x_1 \leq 10$ and $9 x_2 \leq 10$

 $\theta=20$ is achieved with $x_1=10$ and $x_2=\frac{10}{9}$

therefore the max is 20 Mb/s

The value of x_0 when the maximum throughput is attained is ...

- A. 1 Mb/s
- B. $\frac{10}{9}$ Mb/s
- C. 2 Mb/s
- D. None of the above
- E. I don't know



Answer D

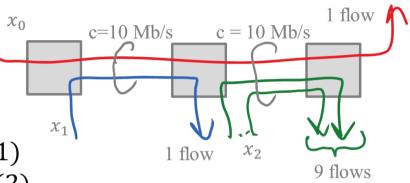
Find all $x_0 \ge 0$ $x_1 \ge 0$ $x_2 \ge 0$ subject to

$$x_0 + x_1 \le 10$$
 (1)
 $x_0 + 9x_2 \le 10$ (2)
 $x_0 + x_1 + 9x_2 = 20$ (3)

By (1) and (3): $9x_2 \ge 10$

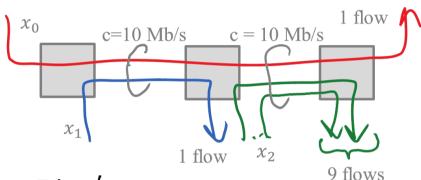
Compare to (2): $9x_2 = 10$

Thus $x_0 = 0$ (and $x_1 = 10$, $x_2 = 10/9$)



Pareto Efficiency

A feasible allocation of rates \vec{x} is called Pareto-efficient (synonym: Pareto-optimal) iff increasing one source must be at the expense of decreasing some other source i.e. \vec{x} is Pareto-efficient iff:



for any other feasible \vec{x}' , $\exists i: x_i' > x_i \Rightarrow \exists j: x_i' < x_j$

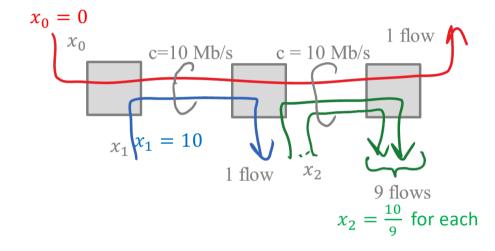
 \Leftrightarrow every source has a bottleneck link (i.e. for every source i there exists a link, used by i, which is saturated, i.e. the constraint of which is satisfied with equality).

An allocation \vec{x} is not Pareto-efficient iff it can be improved unilaterally, i.e. there exists a feasible allocation \vec{x}' such that $x_i' > x_i$ for some i and $x_i' \ge x_j$ for all j.

Example

Is the allocation $x_0 = 0, x_1 = 10, x_2 = 10/9$ Pareto-efficient?

Link 1 is bottleneck for sources 0 and 1
Link 2 is bottleneck for source 0 and all sources 2



Every source has a bottleneck and cannot be increased unilaterally: The allocation is Pareto-efficient.

Observe that the throughput-maximizing allocation is always Pareto-efficient.

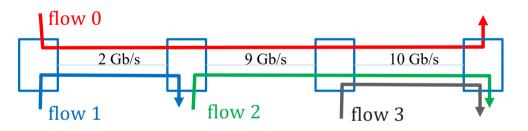
Which allocations are Pareto-Efficient?

A.
$$x_0 = 1, x_1 = 0.5, x_2 = 8, x_3 = 1$$

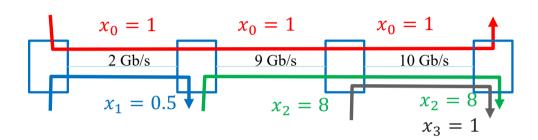
B.
$$x_0 = 1, x_1 = 1, x_2 = 8, x_3 = 1$$

C.
$$x_0 = 1, x_1 = 1, x_2 = 2, x_3 = 7$$

- D. A and B
- E. A and C
- F. B and C
- G. All
- H. None
- I. I don't know



Answer F (B and C)



Allocation A: Source 1 does not have a bottleneck. Its rate can be increased unilaterally. For example, we can increase x_1 to $x'_1 = 0.6$ while leaving the other rates unchanged and obtain a feasible allocation. Allocation A is not Pareto-efficient

Allocation B:

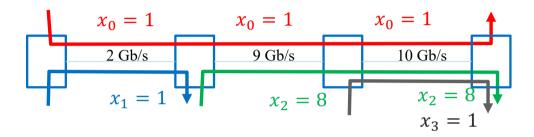
Link 1 is bottleneck for sources 0 and 1

Link 2 is bottleneck for sources 0 and 2

Link 3 is bottleneck for sources 0, 2 and 3

Every source has a bottleneck. None can be increased unilaterally.

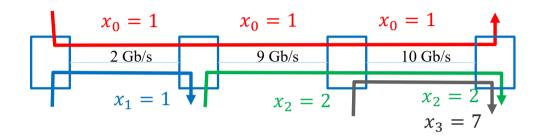
Allocation B is Pareto-efficient.



Allocation C:

Link 1 is bottleneck for sources 0 and 2

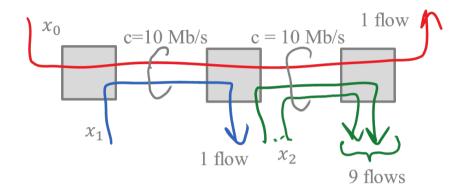
Link 3 is bottleneck for sources 0, 2 and 3



Every source has a bottleneck. None can be increased unilaterally. Allocation C is Pareto-efficient.

Observe that link 2 is not saturated in this Pareto-efficient allocation.

Take Home Message



Maximal efficiency means Pareto efficiency.

Maximizing total throughput is Pareto efficient, but means shutting down flow 0; this is at the expense of fairness.

Are there Pareto efficient allocations that are fair? What is fairness?

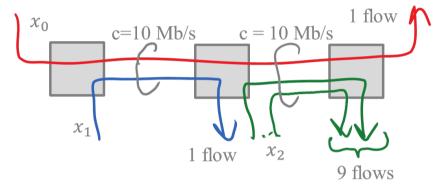
3. Let us try a first definition (Egalitarianism): allocate as much as possible but same to all. In this example, what is the allocation according to this definition?

A.
$$x_0 = x_1 = x_2 = 0.5 Mb/s$$

B.
$$x_0 = x_1 = x_2 = 1 Mb/s$$

C.
$$x_0 = x_1 = x_2 = \frac{10}{9} Mb/s$$

- D. None of the above
- E. I don't know



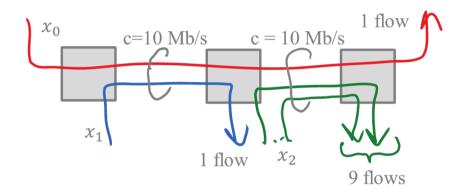
Maximize
$$x=x_0=x_1=x_2$$
 subject to
$$2\,x \le 10$$

$$10\,x \le 10$$

with $x \ge 0$

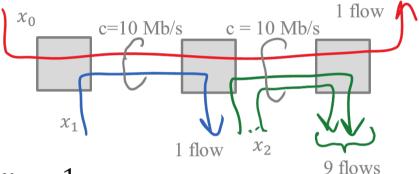
The solution is x = 1 Mb/s

Answer B



Egalitarianism is not Pareto- efficient

Egalitarianism gives $x=1\,$ Mb/s to all this is stupid, we could give more to x_1 without hurting anyone



A better allocation is:

$$x_0 = 1, \qquad x_1 = 9,$$

 $x_2 = 1$

It is Pareto-efficient (every resource has a bottleneck) and is "fair", since it gives to every one at least as much as egalitarianism.

This is the max-min fair allocation for this example.

Max-Min fairness

We say that a feasible allocation \vec{x} is max-min fair iff for any other feasible \vec{x}' , $(\exists i: x_i' > x_i \Rightarrow \exists j: x_i' < x_j \text{ and } x_j \leq x_i)$

i.e. For every source i, increasing its rate must force the rate of some other (not richer) source j to decrease

Which allocations are max-min fair?

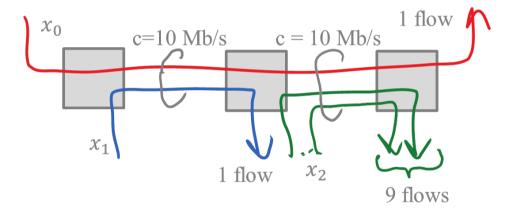
$x_0 = 0 \text{ Mb/s} \quad || x_0 = 1 \text{ Mb/s} ||$ $x_1 = 10 \text{ Mb/s} || x_1 = 9 \text{ Mb/s}$ $x_2 = \frac{10}{9} \text{ Mb/s}$ $x_2 = 1 \text{ Mb/s}$

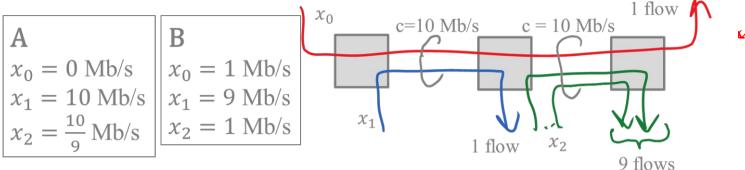
$$x_0 = 1 \text{ Mb/s}$$

$$x_1 = 9 \text{ Mb/s}$$

$$x_2 = 1 \text{ Mb/s}$$

- A. A
- B. B
- C. A and B
- D. None
- I don't know





Allocation A

I can increase x_0 (e.g. $x_0 \leftarrow 1$) and decrease x_1 ($x_1 \leftarrow 9$) and x_2 ($x_2 \leftarrow 1$); this does not contradict fairness because x_1 and x_2 are larger than x_0 . There exists one increase that does not contradict fairness

A is not max-min fair

Allocation B

If I increase x_0 I must decrease $x_2 \Rightarrow$ contradicts fairness

If I increase x_1 I must decrease $x_0 \Rightarrow$ contradicts fairness

If I increase x_2 I must decrease $x_0 \Rightarrow$ contradicts fairness

Any increase contradicts fairness

B is max-min fair

The Maths of Max-Min Fairness

Given a set of constraints for the rates

If it exists, the max-min fair allocation is unique

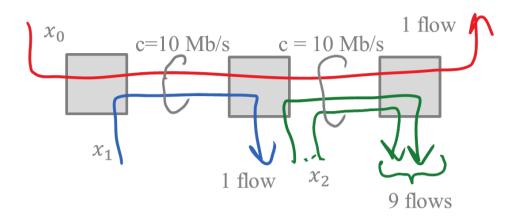
There *exists* one max-min fair allocation if the set of feasible rates is convex (this is the case for networks, as we have linear constraints)

The max-min fair allocation is Pareto-efficient (converse is not true)

For a set of feasible rates as in our case (the sum of the rates on every link is upper bounded), the (unique) max min fair allocation is obtained by water-filling

- 1 mark all sources as non frozen
- 2 Do
- 3 increase the rate of all non frozen sources to the largest possible common value
- 4 mark sources that use a saturated link as frozen
- 5 Until all sources are frozen

Water-Filling Example



Step 1:

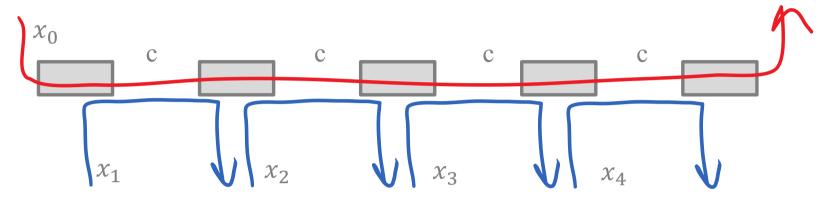
- maximize t such that $x_0=x_1=x_2=t$ and all constraints are satisfied; we find t=1, hence $x_0=x_1=x_2=1$;
- link 2 is saturated, is used by sources 0 and 2 ⇒ mark sources 0 and 2 as frozen

Step 2:

- maximize t such that $x_1=t$, with $x_0=1, x_2=1$ and all constraints are satisfied; we find t=9, hence $x_0=x_2=1$ and $x_1=9$
- link 1 is saturated, is used by sources 0 and 1 ⇒ mark source 1 as frozen; all sources are frozen, STOP.

The max-min fair allocation is $x_0 = x_2 = 1$ and $x_1 = 9$

What is the max-min fair allocation?



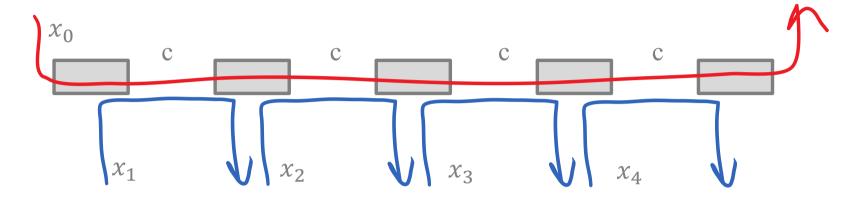
A.
$$x_i = \frac{c}{2} \ \forall i$$

B.
$$x_0 = \frac{c}{3}, \quad x_i = \frac{2c}{3} \ \forall i \neq 0$$

C.
$$x_0 = \frac{c}{4}, \quad x_i = \frac{3c}{4} \ \forall i \neq 0$$

D.
$$x_0 = \frac{c}{5}, \quad x_i = \frac{4c}{5} \ \forall i \neq 0$$

- E. None of the above
- F. I don't know



Answer A

The max-min fair allocation gives the same rate $\frac{c}{2}$ to all sources Some people think that x_0 should be penalized as it uses more of the network

This is what led to the definition of proportional fairness

Definition of Proportional Fairness

We say that a feasible allocation \vec{x} is *proportionally fair* iff $\vec{x} > 0$ and for any other feasible \vec{x}' , $\sum_i \frac{x_i' - x_i}{x_i} \leq 0$

In other words: an allocation is proportionnally fair if for any other allocation, the total rate of change $\sum_i \frac{\Delta x_i}{x_i}$ is ≤ 0

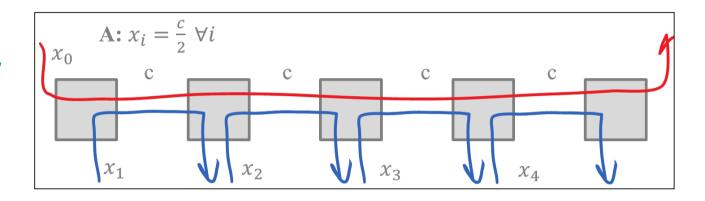
An allocation $\vec{x}>0$ is not proportionally fair iff there is some other allocation \vec{x}' such that $\sum_i \frac{x_i'-x_i}{x_i}>0$

Two effects

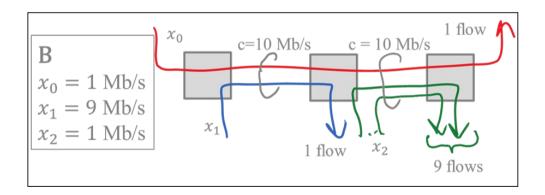
Relative shares matter, not absolute

Sum of all rates of changes

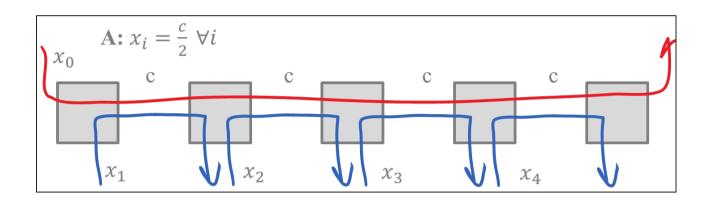
Which allocations are proportionally fair?



- A. A
- B. B
- C. A and B
- D. None
- E. I don't know



Solution



Answer D

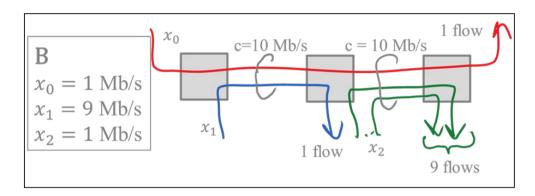
I can do $x_i \leftarrow x_i + \delta$ for $i=1\dots 4$ and $x_0 \leftarrow x_0 - \delta$; if δ is small enough (i.e. $0<\delta\leq \frac{c}{2}$) the new allocation is feasible

The total rate of change is $-\frac{\delta}{\frac{c}{2}} + 4\frac{\delta}{\frac{c}{2}} > 0$

We could change the allocation and obtain a positive total rate of change.

A is not proportionally fair

Solution



I can do $x_2 \leftarrow x_2 + \delta$ and $x_0 \leftarrow x_0 - 9\delta$; $x_1 \leftarrow x_1 + 9\delta$; if δ is small enough (i.e. $0 < \delta \le \frac{1}{9}$) the new allocation is feasible

The total rate of change is $-\frac{9\delta}{1} + \frac{9\delta}{9} + 9\frac{\delta}{1} = \delta > 0$ We could change the allocation and obtain a positive total rate of change.

B is not proportionally fair

The Maths of Proportional Fairness

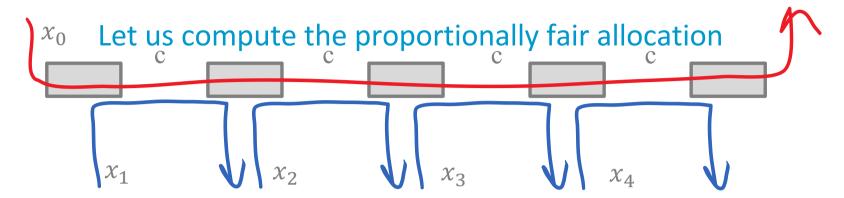
- 1. A proportionally fair allocation is Pareto-efficient.
- 2. Given a set of constraints for the rates that is convex: The proportionally fair allocation *exists* and is *unique* It is obtained by maximizing

$$J(\vec{x}) \coloneqq \sum_{i} \log x_{i}$$

over all feasible allocations

Intuitive explanation:

$$dJ(\vec{x}) = \sum_{i} \frac{dx_i}{x_i}$$



We have to solve the optimization problem:

$$\max U = \log x_0 + \log x_1 + \log x_2 + \log x_3 + \log x_4$$
subject to

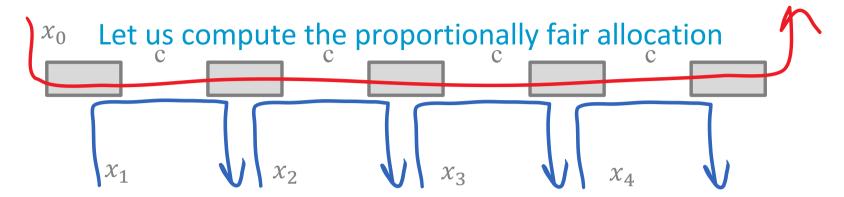
$$x_0 + x_1 \le c$$

$$x_0 + x_2 \le c$$

$$x_0 + x_3 \le c$$

$$x_0 + x_4 \le c$$

We can use convex programming, but here we can also do a direct solution



We have to solve the optimization problem:

$$\max U = \log x_0 + \log x_1 + \log x_2 + \log x_3 + \log x_4$$

subject to
$$x_0 + x_1 \le c$$

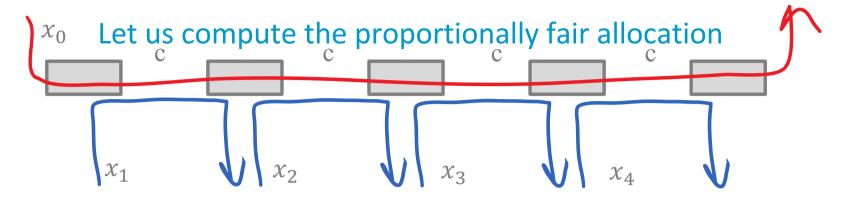
$$x_0 + x_2 \le c$$

$$x_0 + x_3 \le c$$

$$x_0 + x_4 \le c$$

We must have equality everywhere otherwise we can increase x_i ($i \neq 0$) and increase U

Therefore we must have $x_1 = x_2 = x_3 = x_4 = c - x^*$ and $x_0 = x^*$ for some x^*



We have to solve the optimization problem:

$$\max U = \log x^* + 4 \log(c - x^*)$$

subject to $0 < x^* < c$

This is a 1d problem, can be solved by computing the derivative

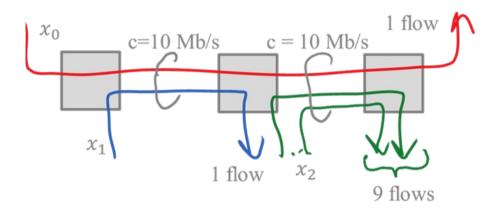
We find
$$\frac{dU}{dx^*} = \frac{1}{x^*} - \frac{4}{c - x^*}$$

There is a maximum for $x^* = \frac{c - x^*}{4}$ i.e. $x^* = \frac{c}{5}$

The proportionally fair allocation is

$$x_0 = \frac{c}{5}$$
, $x_1 = x_2 = x_3 = x_4 = \frac{4c}{5}$

Which one is the proportionally fair allocation ? (in Mb/s) (only one answer)



A.
$$x_0 = 1, x_1 = 9, x_2 = 1$$

B.
$$x_0 = 0.909, x_1 = 9, x_2 = 1.010$$

C.
$$x_0 = 1.009, x_1 = 8.991, x_2 = 0.999$$

D.
$$x_0 = 0.909, x_1 = 9.091, x_2 = 1.010$$

E. I don't know

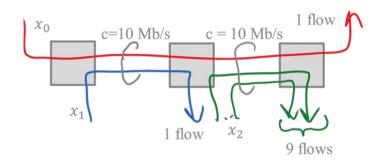
Solution

A.
$$x_0 = 1, x_1 = 9, x_2 = 1$$

B.
$$x_0 = 0.909, x_1 = 9, x_2 = 1.010$$

C.
$$x_0 = 1.009, x_1 = 8.991, x_2 = 0.999$$

D.
$$x_0 = 0.909, x_1 = 9.091, x_2 = 1.010$$



Answer D

We know A is not proportionally fair

B is not Pareto-efficient (you can increase x_1 only) therefore is also not proportionally fair

C goes in the wrong direction (gives more to 0 than to 2) and is probably not proportionally fair

D is probably the correct answer

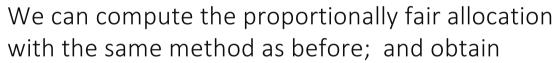
Solution

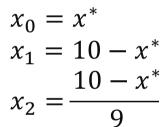
A.
$$x_0 = 1, x_1 = 9, x_2 = 1$$

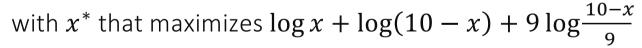
B.
$$x_0 = 0.909, x_1 = 9, x_2 = 1.010$$

C.
$$x_0 = 1.009, x_1 = 8.991, x_2 = 0.999$$

D.
$$x_0 = 0.909, x_1 = 9.091, x_2 = 1.010$$

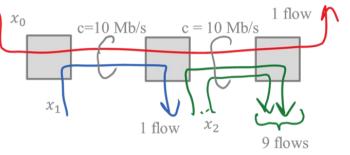






$$x^* = \frac{10}{11} \, \text{Mb/s}$$

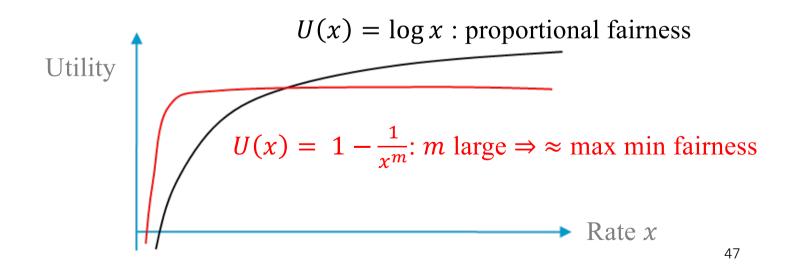
This is allocation D



Utility Fairness

One can *interpret* proportional fairness as the allocation that maximizes a global utility $\sum_i U_i(x_i)$ with $U_i(x_i) = \log x_i$. If we take some other utility function we have what is called a utility fairness

It can be shown that max-min fairness is the limit of utility fairness when the utility function converges to a step function but max-min fairness cannot be expressed exactly as a utility fairness



Take Home Message

Sources should adapt their rate to the state of the network in order to avoid inefficiencies and congestion collapse

This is called "congestion control"

A rate adaptation mechanism should target some form of fairness

E.g. max-min fairness or proportional fairness

4. Additive Increase Multiplicative Decrease

How can congestion control be implemented?

Explicit (rate based): tell every host how fast it can send MPLS networks (smart grid)

Cellular networks

Hop by hop = backpressure: STOP/GO signals sent upstream Gigabit LAN switches

Fair Queuing per Flow: One queue per flow / per user, served round robin Cellular networks, industrial networks, in-vehicle networks

End-to-end: hosts taste the water and increase or decrease their sending rate using a host congestion control algorithm

The solution in the Internet

Additive Increase Multiplicative Decrease (AIMD)

The first congestion control algorithm deployed in the Internet and before that, in Decnet (the "Decbit").

Still widely deployed today

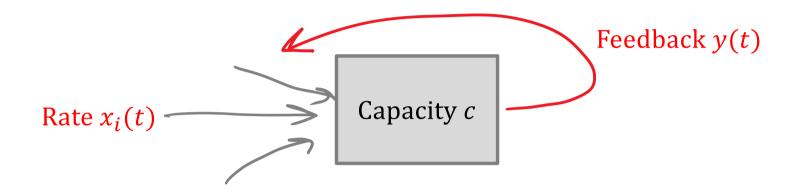
We have designed a scheme that allows a network to operate at its knee. As shown in Figure 3, the scheme uses one bit called the **congestion avoidance bit** in the network layer header of the packet for feedback from the subnet to the users. A source clears the congestion avoidance bit as the packet enters the subnet. All routers in the subnet monitor their load and if they detect that they are operating above the knee, they set the congestion avoidance bit in the packets belonging to users causing overload. Routers operating below the knee pass the bit as received. When the packet is received at the destination the network layer passes the bit to the destination transport, which takes action based on the bits.



Raj Jain

Raj Jain, K.K. Ramakrishnan, and Dah-Ming Chiu. Congestion avoidance in computer networks with a connectionless network layer. Technical Report DEC-TR-506, Digital Equipment Corporation, August 1987.

A Simple Network Model



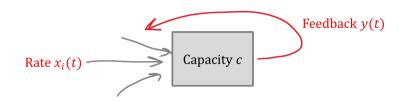
Network sends a one-bit feedback:

$$y(t) = 0$$
 if $\sum_i x_i(t) \le c$, $y(t) = 1$ if $\sum_i x_i(t) > c$

Sources reduce rate $x_i(t + 1)$ if y(t) = 1, increase otherwise

Question: what form of increase/decrease laws should one pick?

Linear Laws



We consider linear laws

if
$$y(t) = 1$$
 then $x_i(t+1) = u_1 x_i(t) + v_1$

if
$$y(t) = 0$$
 then $x_i(t + 1) = u_0 xi(t) + v_0$

We want to decrease when y(t) = 1, so

 $(u_1 \leq 1 \text{ and } v_1 \leq 0 \text{ and at least one inequality must be strict}$

Multiplicative Additive

decrease decrease term

factor

We want to increase when y(t) = 0, so

 $u_0 \ge 1$ and $v_0 \ge 0$ and at least one inequality must be strict

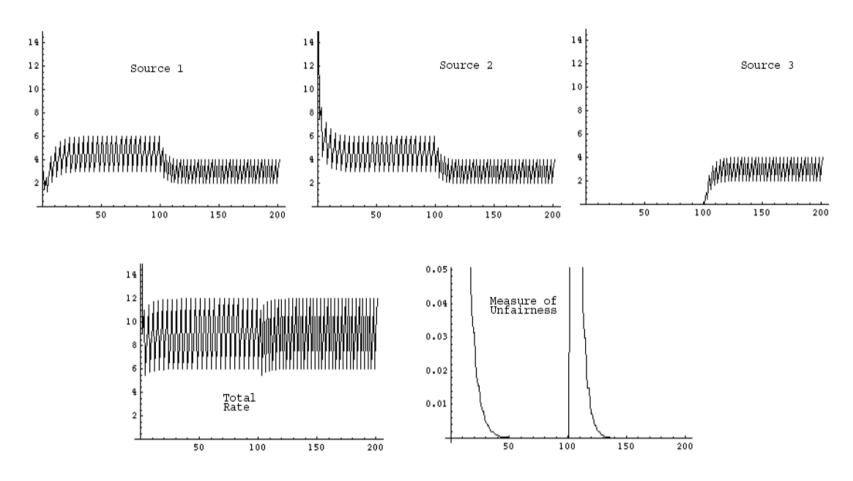
Multiplicative Additive

increase increase term

factor

Example

$$u_1 = 0.5, v_1 = 0$$
 (multiplicative decrease)
 $u_0 = 1, v_0 = 1$ (Mb/s) (additive increase)



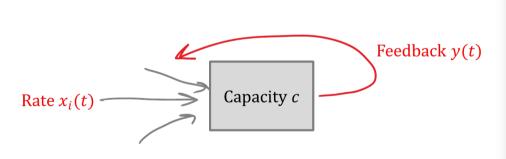
Analysis of Linear Control Schemes

We want to achieve efficiency and fairness

We could target either max-min fair or proportionally fair allocations

Here they are the same

We will now analyze the impact of each of the four coefficients u_0 , u_1 , v_0 and v_1 .



```
■ We consider linear laws

if y(t) = 1 then x_i(t+1) = u_1 x_i(t) + v_1

if y(t) = 0 then x_i(t+1) = u_0 xi(t) + v_0

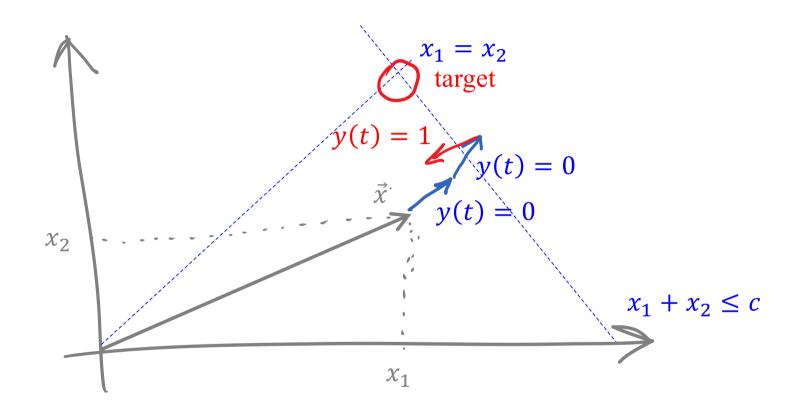
■ We want to decrease when y(t) = 1, so

u_1 \le 1 and v_1 \le 0 and at least one inequality must be strict Multiplicative decrease term

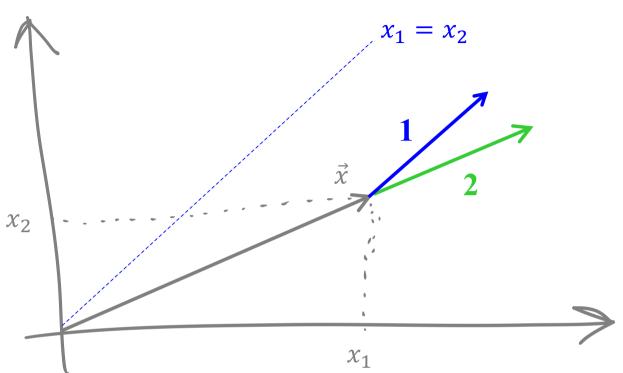
■ We want to increase when y(t) = 0, so

u_0 \ge 1 and v_0 \ge 0 and at least one inequality must be strict Multiplicative increase factor increase term
```

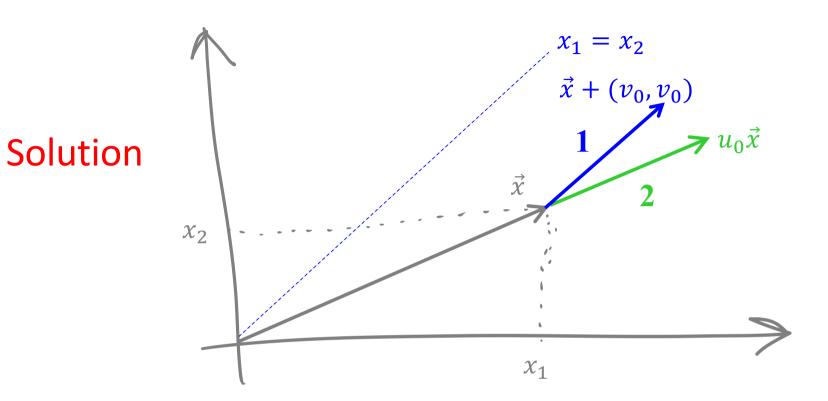
Zoom on 2 Sources



Zoom on 2 sources; say what is true

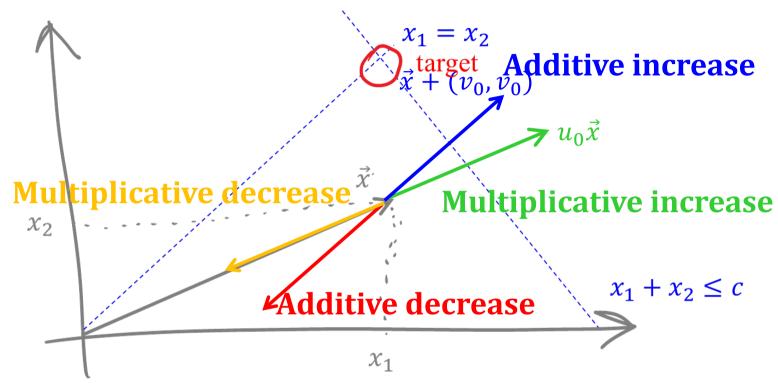


- A. 1 = additive increase, 2 = multiplicative increase
- B. 1 = multiplicative increase2 = additive increase,
- C. None of the above
- D. I don't know



- 1 = additive increase,
- 2 = multiplicative increase

Answer A



- 1. Additive decrease worsens fairness (goes away from $x_1 = x_2$) and should be avoided \Rightarrow decrease should be multiplicative
- 2. Additive increase is the only move that increases fairness and should be therefore be included ⇒ increase should be additive

Why AIMD

Among the linear controls, only additive increase – multiplicative decrease (AIMD) tends to bring the allocation towards fairness and efficiency.

This is what was implemented in the Internet after the first congestion collapses.

In a more complex network setting, does AIMD distribute rates according to max-min fairness or proportional fairness?

- A. Max-min
- B. Proportional
- C. None of the above
- D. I don't know

Fairness of AIMD

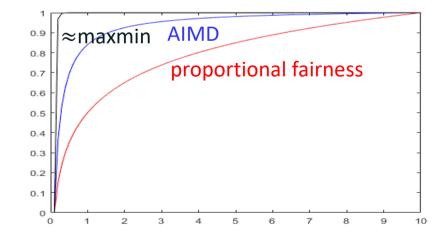
Answer C

AIMD with: additive increase +r, multiplicative decrease $\times (1 - \eta)$ and one update per time unit implements utility fairness, with utility of flow i given by

$$U(x_i) = \log \frac{x_i}{r + \eta x_i}$$

with x_i = rate. The fairness of AIMD is between maxmin fairness and proportional fairness, closer to proportional fairness.

(see "Rate adaptation, Congestion Control and Fairness: A Tutorial" https://ica1www.epfl.ch/PS_files/LEB3132.pdf)



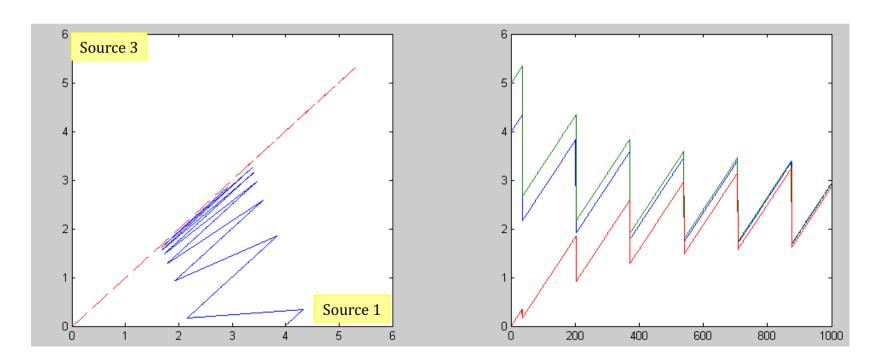
rescaled utility functions; AIMD is for $\eta=0.5~r=$ 1MSS per 100 ms maxmin approx. is $U(x)=1-x^{-5}$

5. Slow Start

AIMD convergence can be accelerated when initial conditions are very different

Slow start is an additional method, added to AIMD

Used at beginning of connection and at losses detected by timeout

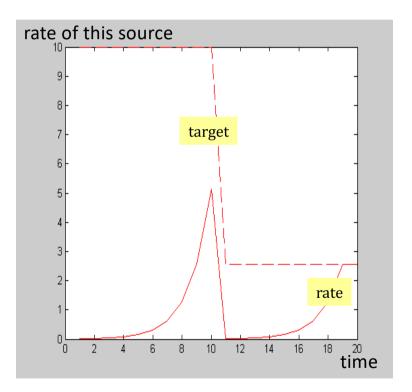


Slow Start

Increase the rate multiplicatively

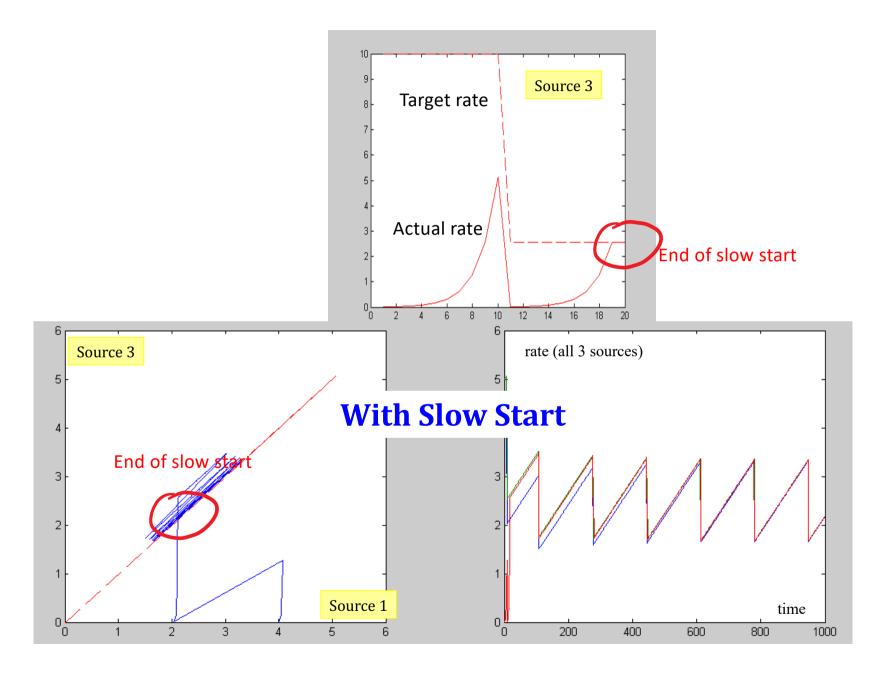
(by w_0 , e.g. $w_0=2$) until a target rate is reached or negative feedback is received Apply multiplicative decrease (by u_1 , e.g. $u_1=0.5$) to target rate if negative feedback is received.

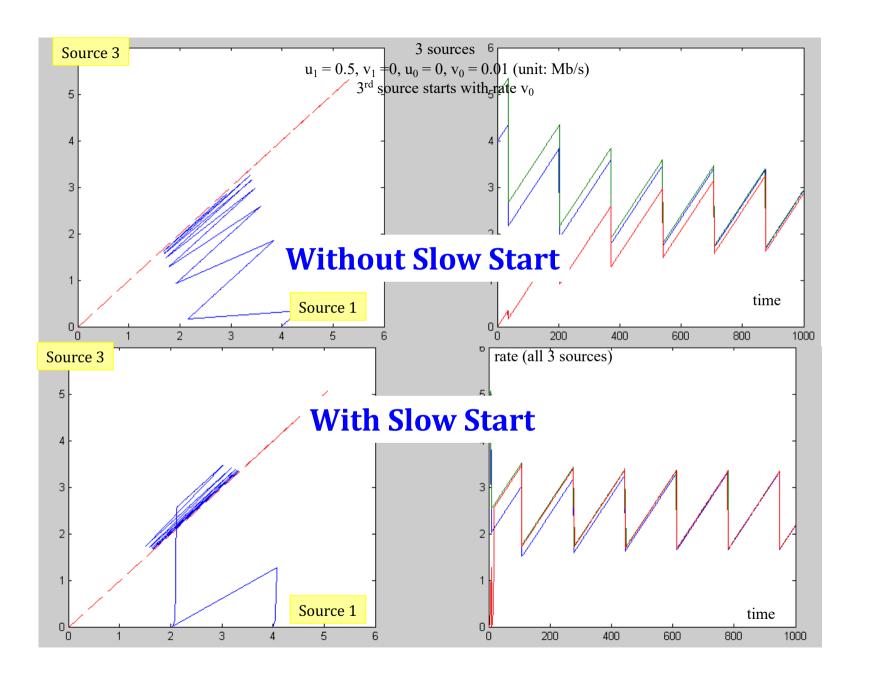
Exit slow start when target rate is reached



Algorithm 2 Slow Start with the following parameters: AIMD constants multiplicative increase factor $w_0 > 1$; maximum rate $r_{\text{max}} > 0$.

```
1: rate \leftarrow v_0
 2: targetRate \leftarrow r_{max}
 3: do forever
 4: receive feedback
 5: if feedback is positive then
                                               W= 2
        rate \leftarrow w_0 \cdot rate
 6:
         if rate \geq targetRate then
 7:
             rate \leftarrow targetRate
 8:
             exit do loop
 9:
         end if
10:
11: else
        targetRate \leftarrow max(u_1 \cdot rate, v_0)
12:
13:
         rate \leftarrow v_0
14: end if
15: end do
```





Summary

Congestion control is necessary to avoid inefficiencies and collapses

A congestion control scheme aims at allocating rates according to some form of fairness

In the internet, we use end-to-end congestion control with

≈ AIMD

Slow Start

and other refinements – see part 2.