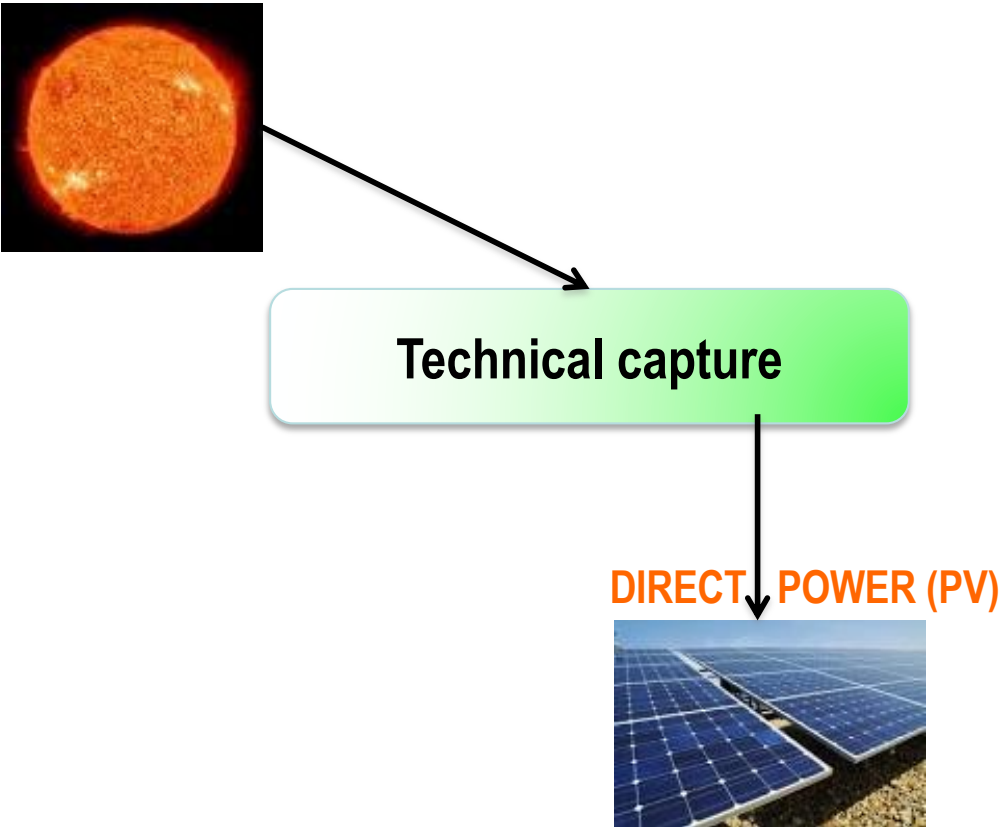


SOLAR ELECTRIC: PHOTOVOLTAÏCS (SOLAR CELLS)



Learning objectives in this chapter

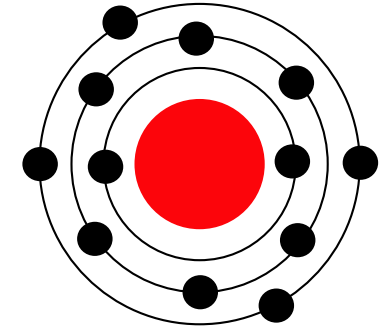
- Explain the operating principle of a solar cell
- Know the efficiency and power density of PV.
- Know different PV technologies
- Know to apply basic formulas (p. 38)

Principle of operation

The operating principle of a solar cell relies on the **direct** conversion :

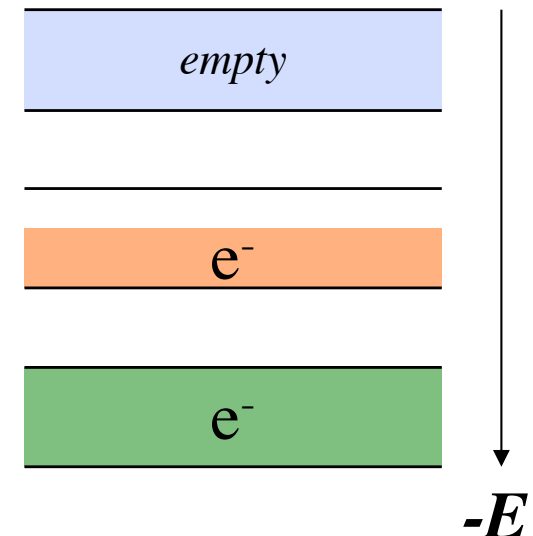
- 1) of incident energy of photons (=solar irradiation spectrum, see ‘Solar basics’ chapter) on a **semiconductor** (s.c.)
- 2) in electricity, by creation of charge carrier pairs (**electrons** (n^-) and **holes** (p^+)) in the s.c.
- 3) and **separation** of these thanks to a **p-n junction**

Reminder of semiconductor physics



- in atoms, electrons (= **particle + wave**) are found on precise and confined energy levels (= *s, p, d, f* orbitals => quantum mechanics)
- when closely arranging many identical atoms in a solid (=a crystal), these energy levels combine to form continuous **energy bands** between 2 energy values; these bands are one of the following:

- **filled** (shell electrons, close to the nucleus),
- **partially filled** (valence electrons, far from the nucleus)
- **empty** (allowed energy levels, but without electrons)



Fermi distribution:

→ all these electrons in the solid crystal interact

(i) with each other

(ii) with the nuclei

and due to the **Pauli exclusion** principle

(= no 'free' occupation on the available energy levels, and maximum 2 electrons (of opposite spin) on each level),

the density of **authorised energy levels for the electrons** in

the confined crystal volume is given by the Fermi distribution

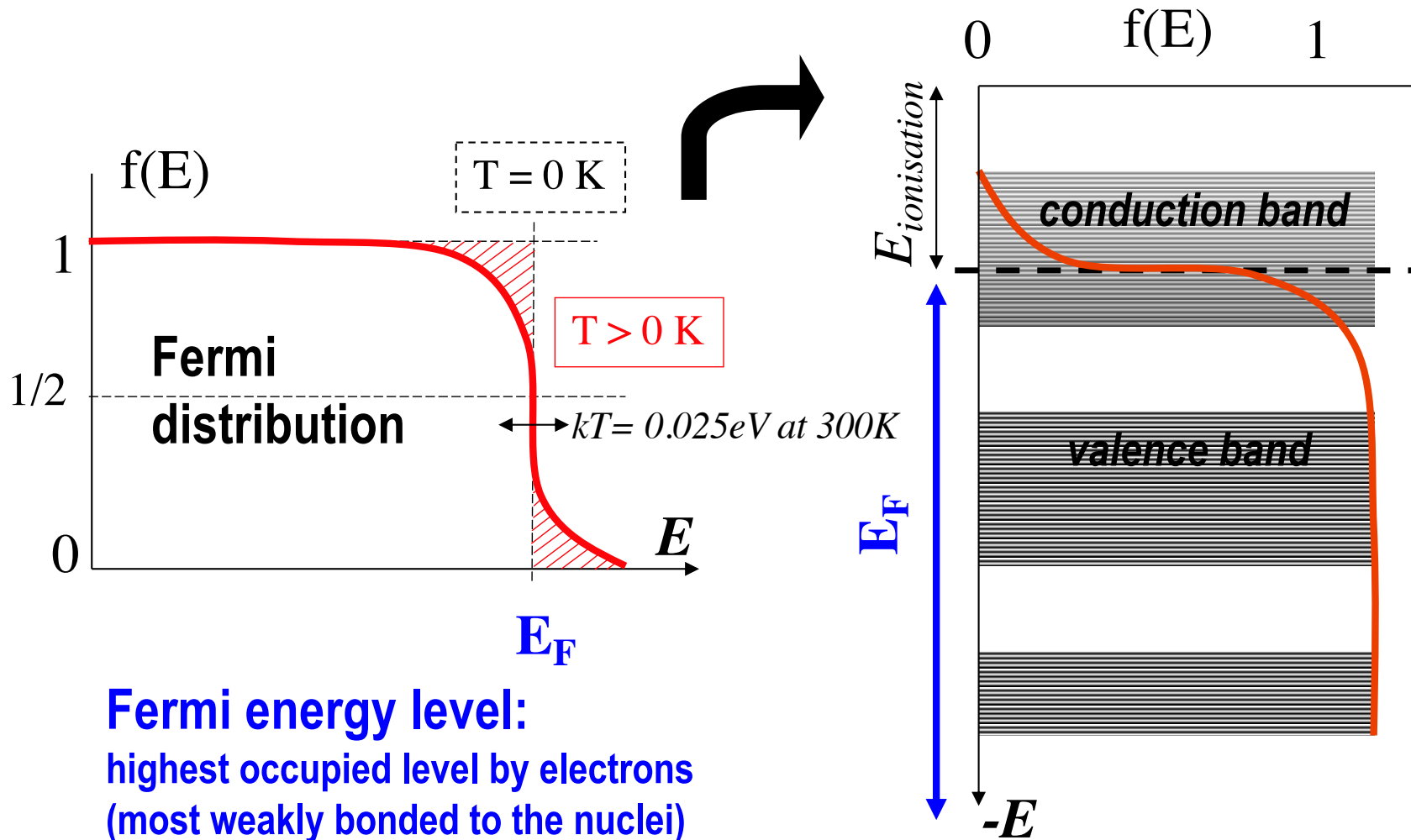
(different from that of free molecules in a gas, which is given by the Maxwell-Boltzmann distribution)

→ number dN of electrons in the energy level interval $E+dE$:

$$dN = N_0 f(E) dE \quad \text{avec} \quad f(E) = \frac{1}{1 + \exp\left[\frac{E - E_F}{kT}\right]}$$

Fermi distribution

↓
 N_0 : total number of e-



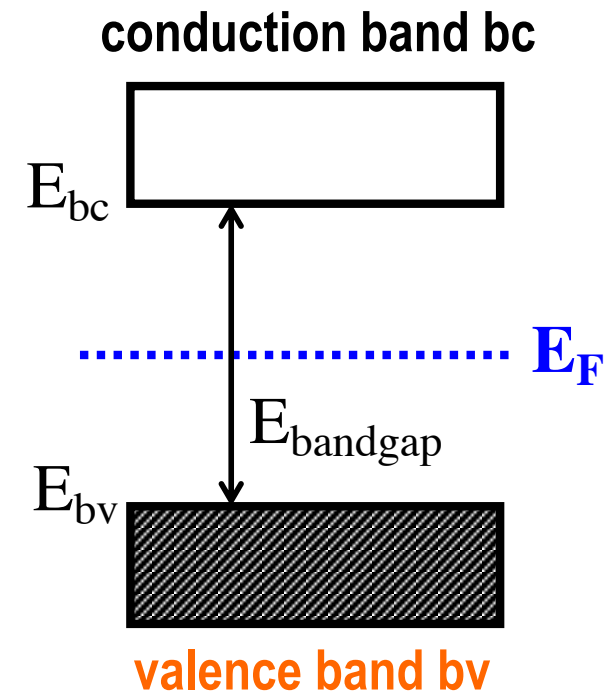
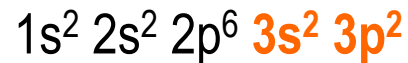
Fermi energy level:
 highest occupied level by electrons
 (most weakly bonded to the nuclei)

Electrical conduction in a solid

When an electric field acts on a solid, **only electrons close to the Fermi level** (= weakly bonded) acquire energy (kinetic, translational), and can hence **conduct electricity**, but only when they are **in a partially filled energy band**, and if the Fermi level is located in this band (which is the typical case for a **metal**; which is why metals conduct electricity)

Semiconductor

- for a semiconductor (f.ex. Silicium, Si), the Fermi level E_F is located between 2 bands
- above E_F = **conduction** band bc (*empty*), $3sp^{3*}$
- below E_F = **valence** band bv (*full*)
(filled with the **4** valence (=outer) electrons of each Si atom)

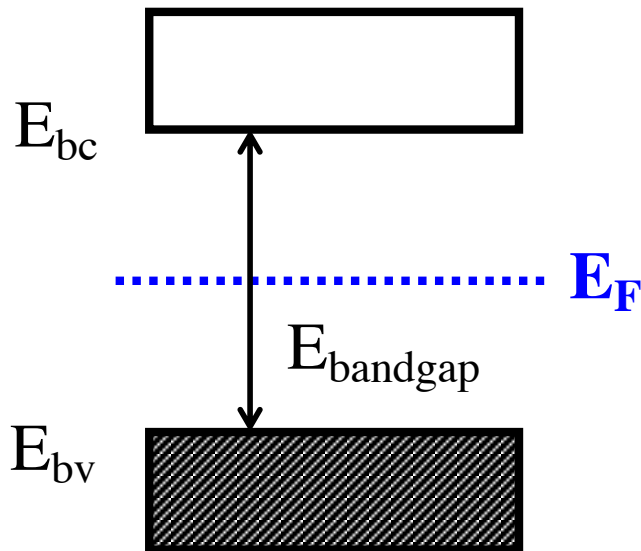


- electrical conductivity of semiconductors
= 10^5 - 10^{10} times lower than metals (the bv is already full)
= increases with temperature (contrary to metals)
(since some electrons will populate the free bc when they acquire thermal energy)

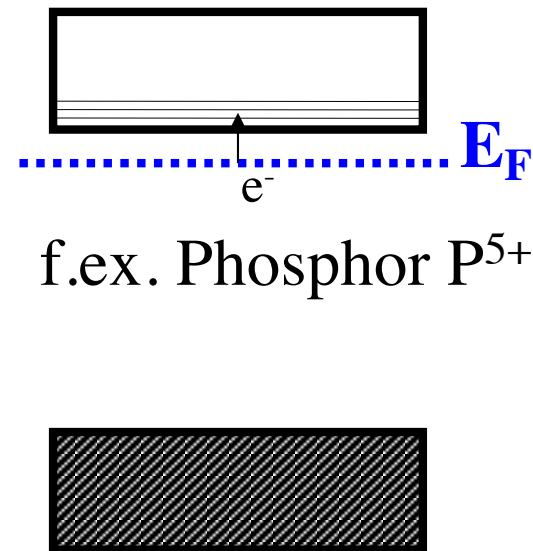
Fermi level / *intrinsic* semiconductor vs. *doped* semiconductor

5 B Boron 2.34	6 C Carbon 2.62	7 N Nitrogen 1.251
13 Al Aluminum 2.70	14 Si Silicon 2.33	15 P Phosphorus 1.82
31 Ga Gallium 5.91	32 Ge Germanium 5.32	33 As Arsenic 5.72

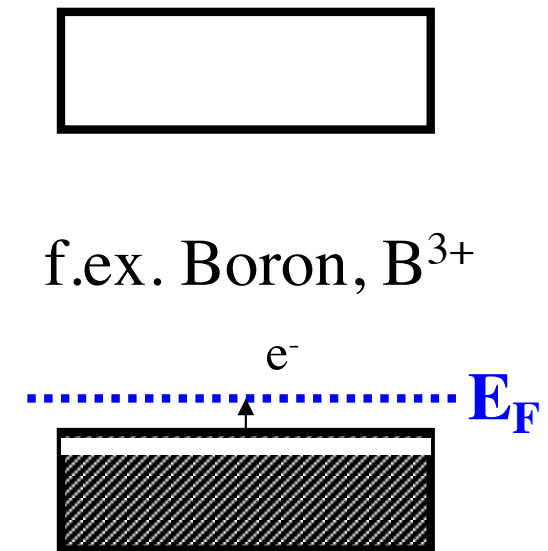
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s.c. **intrinsic**



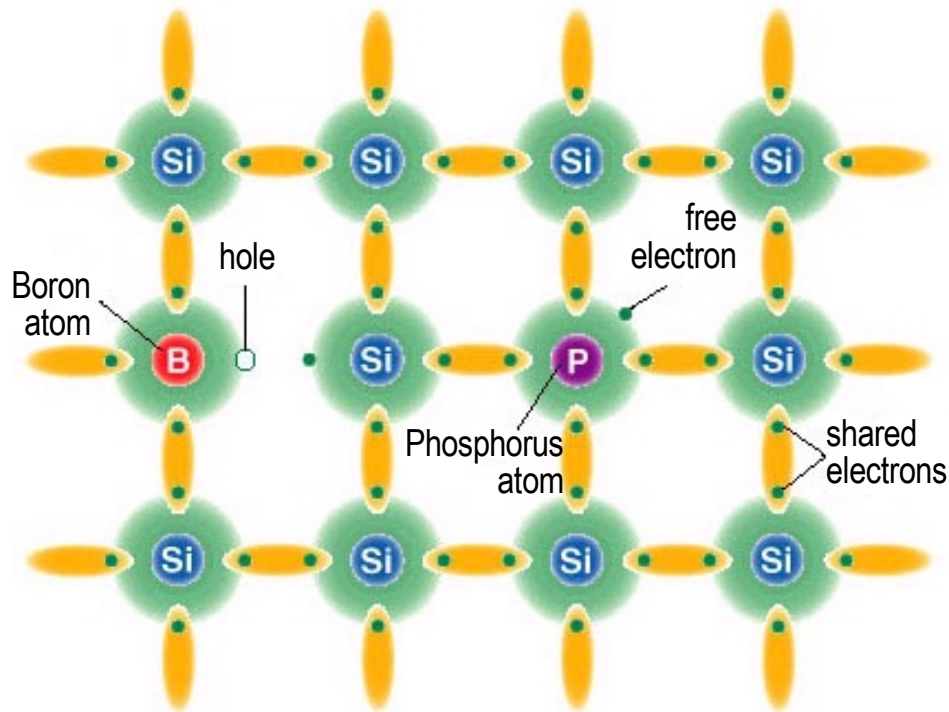
s.c. **doped “n”**
(donor of e^-)



s.c. **doped “p”**
(acceptor of e^-)

Example of silicon **doping** of p-type and n-type

Both p- and n-layers are electrically neutral, yet n-type silicon has excess **mobile** electrons and p-type silicon has excess **mobile** holes



Sandwiching the two layers together creates a **p-n junction** at their interface, which creates an internal electrical field, necessary to keep electrons and holes separated => P.V.

Let n_c be the number of **mobile electrons**,

p_v the number of **mobile holes**,

N_c the number of levels for electrons e^- ,

P_v the number of levels for holes p^+

*2 electrons per orbital
(downspin/upspin)*

*g: degenerescence of the
orbital energy level*

$$n_c = \int_{E_c}^{\infty} 2g_c(E) \frac{1}{1 + \exp\left[\frac{E - E_F}{kT}\right]} dE \quad \text{et} \quad p_v = \int_{-\infty}^{E_v} 2g_v(E) \frac{1}{1 + \exp\left[\frac{E_F - E}{kT}\right]} dE$$

$$n_c = \int_{E_c}^{\infty} 2g_c(E) \exp\left[\frac{-(E - E_F)}{kT}\right] dE = \int_{E_c}^{\infty} 2g_c(E) \exp\left[\frac{-(E - E_C)}{kT}\right] dE \cdot \exp\left[\frac{-(E_C - E_F)}{kT}\right]$$

$$n_c = N_c \cdot \exp\left[\frac{-(E_C - E_F)}{kT}\right] \quad \text{et analogue} \quad p_v = P_v \cdot \exp\left[\frac{-(E_F - E_V)}{kT}\right]$$

$$n_c p_v = N_c P_v \exp\left[\frac{-E_{\text{gap}}}{kT}\right] = \text{const} = n_{\text{intrinsèque}}^2$$

$$\frac{n_c}{p_v} = \frac{N_c}{P_v} \exp\left[\frac{-(E_C - E_F)}{kT} + \frac{-(E_F - E_V)}{kT}\right] = \frac{N_c}{P_v} \exp\left[\frac{2E_F - E_C - E_V}{kT}\right]$$

$$E_F = \underbrace{\frac{E_C + E_V}{2} + \frac{kT}{2} \ln\left(\frac{n_c}{p_v}\right)}_1 + \underbrace{\frac{kT}{2} \ln\left(\frac{P_v}{N_c}\right)}_1$$

for s.c. intrinsic: $1 \quad 1$

The Fermi level is located exactly midway between v and c

⇒ an intrinsic semiconductor is a poor electrical conductor

f.ex. Silicon : $n_{\text{intrinsic}} = 10^{10} \text{ e}^-/\text{cm}^3$, but $5 \cdot 10^{22} \text{ atoms}/\text{cm}^3$, hence $2 \cdot 10^{-13} \text{ mol e}^-$

⇒ $\rho = 10 \text{ k}\Omega\text{cm}$

Doping of a semiconductor

Doping n : $n_c \gg p_v$ $n_c = N_c \cdot \exp\left[\frac{-(E_C - E_F)}{kT}\right]$ donc $E_F = E_C + kT \ln\left(\frac{n_c}{N_c}\right)$

The Fermi level is very close to the conduction band bc

Doping p : $p_v \gg n_c$ $p_v = P_v \cdot \exp\left[\frac{-(E_F - E_V)}{kT}\right]$ donc $E_F = E_V - kT \ln\left(\frac{p_v}{P_v}\right)$

The Fermi level is very close to the valence band by

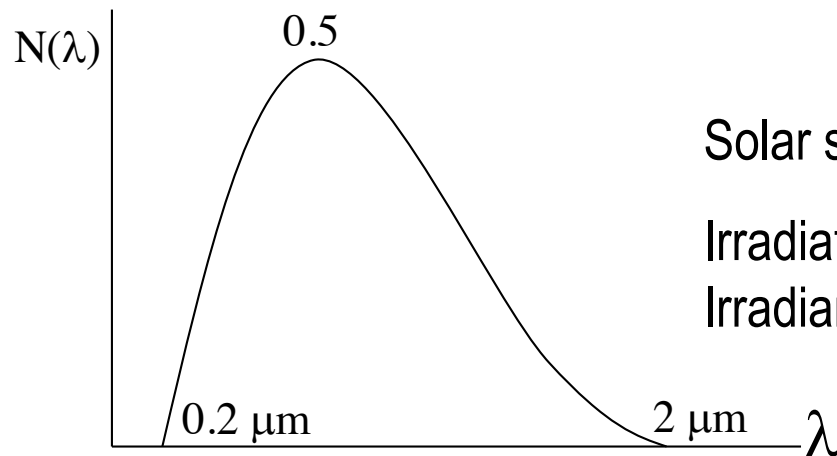
f.ex. 2 ppm P^{5+} or $\text{B}^{3+} = 10^{17} \text{ atoms}/\text{cm}^3 = 10^{17} \text{ e}^-/\text{cm}^3$

⇒ $\rho = 0.3 \Omega\text{cm}$

→ ... which is why we need clean rooms in s.c. manufacturing!

Solar spectrum - see 'Solar basics' chapter

- Energy of photons is given by the Planck equation : $E_{\text{photon}} = h\nu = hc/\lambda$
 h = Planck's constant = $6.6262 \cdot 10^{-34}$ Js
 c = speed of light = $3 \cdot 10^8$ m/s
 λ = wavelength (m) and ν = frequency (s^{-1})



Solar spectrum on Earth = 49% IR, 46% VIS, 5% UV

Irradiation from the sun on earth = $178 \cdot 10^{15}$ Wyr/yr

Irradiance = **1367 W/m²** \pm 3% (Solar constant)

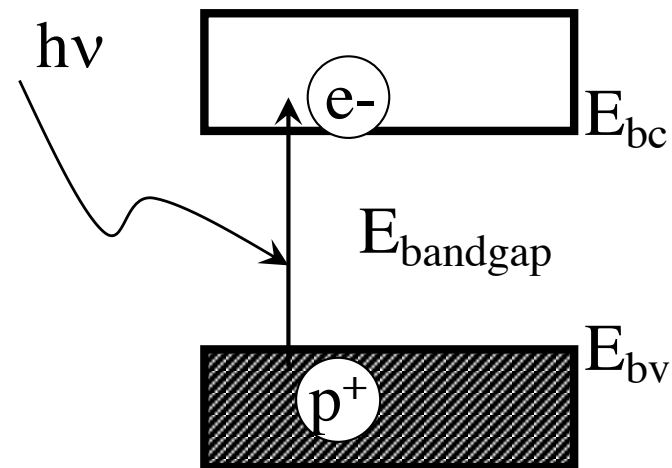
- From this irradiance, 29% is reflected, the rest absorbed (38% by oceans, 24% by atmosphere, 9% by continents) => **1 kW/m²** at the zenith
- depends on latitude + season: for Lausanne: 750 W/m² in summer, 360 W/m² in winter
- solar energy is *direct* (=sunny weather) and *diffuse* (=cloudy weather)
- Swiss year average : 140 W/m² (day and night)

Band-gap

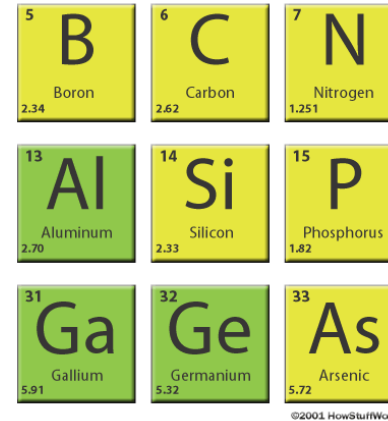
- When irradiating a semiconductor, photons with energy $E_{\text{photon}} \geq E_{\text{bandgap}}$ excite electrons from E_{bv} to E_{bc} , thereby creating a **charge carrier pair** (e^- , p^+)

- The following relation applies :

$$\lambda \text{ (nm)} * E_{\text{bandgap}} \text{ (eV)} = 1240$$



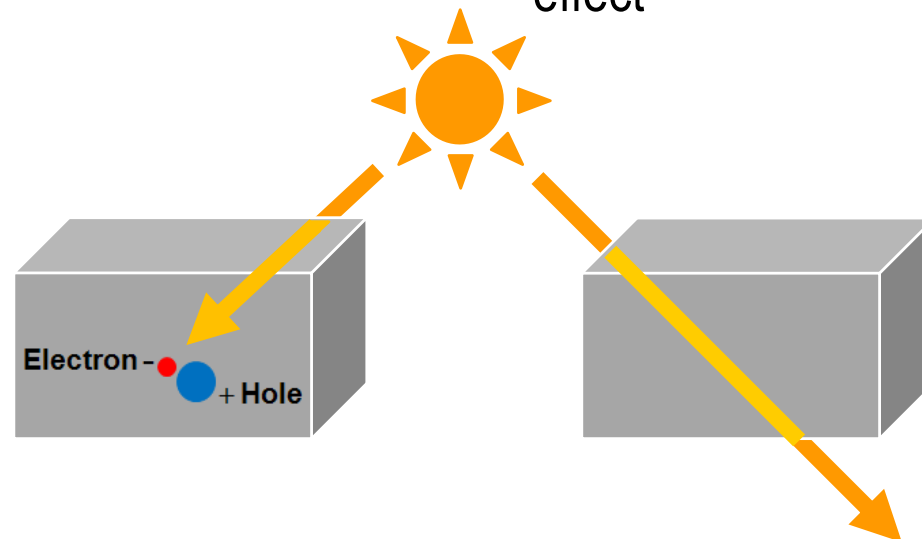
Different PV materials have different energy band gaps (E_{gap})



Material	E_{gap} [eV]
Silicon	1.11
Gallium arsenide	1.43
Aluminium-Gallium arsenide	1.70

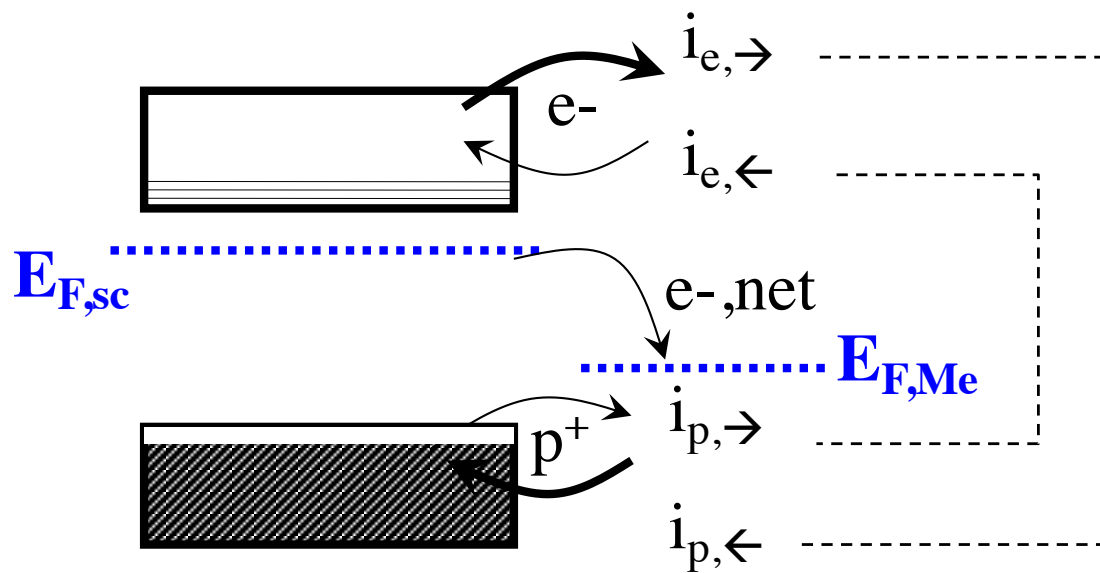
Photons with energy > the band gap energy are absorbed to create free electrons and holes

Photons with less energy pass through the material without PV effect



Band bending:

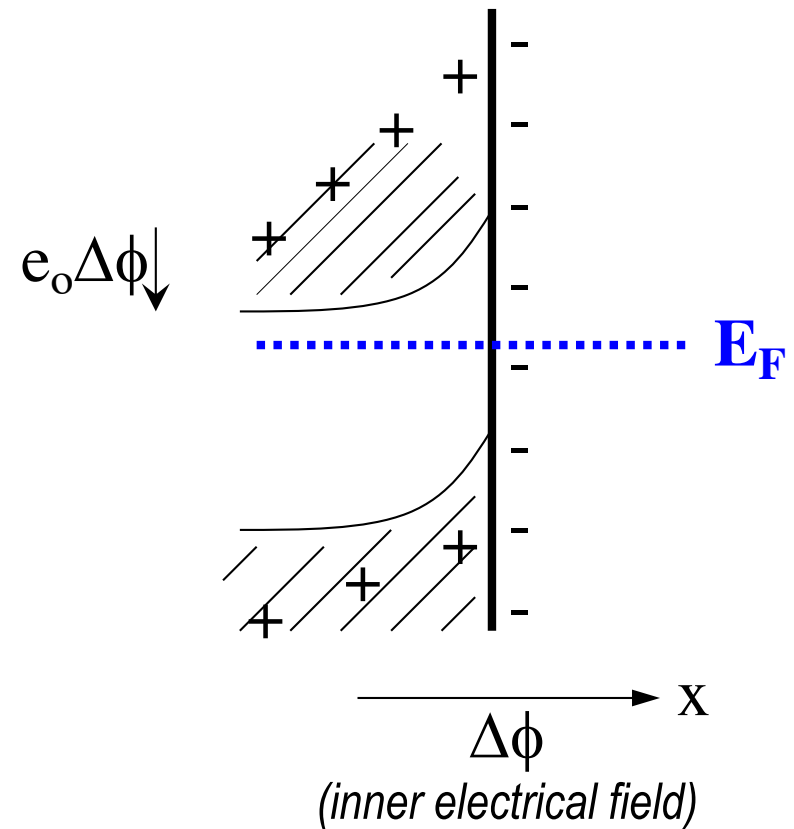
(1) junction between s.c. and metal



s.c. (n)

metal, Me

before junction



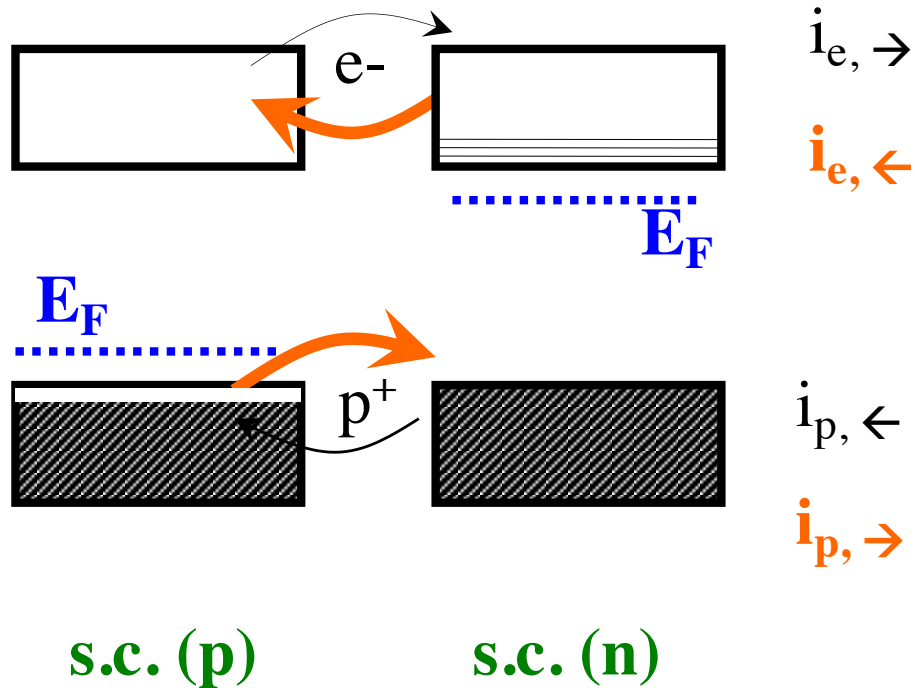
after junction

Explanation:

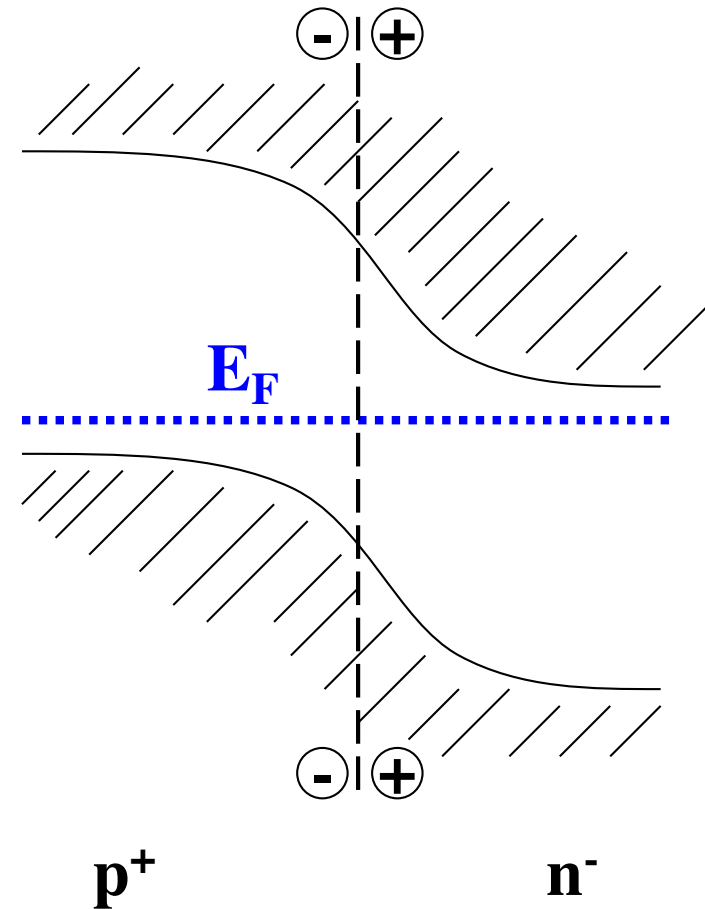
- charge exchange between **Me** and **s.c.** until equilibrium
- compensation by an **internal electrical field**
- a **single Fermi level** exists at equilibrium
- a charge “double layer” develops, with potential difference
 $\Delta\phi = \phi_{\text{Me}} - \phi_{\text{sc}}$
- from Poisson' s equation, we know that:
 $\nabla\phi = d\phi^2/dx^2 = -4\pi q(x)/\epsilon_0$ (ϵ_0 = dielectric constant), i.e.
a **charge distribution** $q(x)$ is associated to this potential difference, which extends **solely into the s.c.** (=space charge layer)
(since the metal conductivity is much higher)
=> band- "bending"

Band bending:

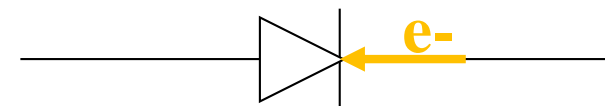
(2) junction s.c / s.c (p-n, diode)



before junction



after junction



- charge exchange (e-,p+) occurs across both bands bc, bv until **equilibrium** is reached (=the **Fermi levels equalize**)
- an **internal field** exists (=a **voltage barrier**) which opposes the natural charge flows of e⁻ (←) and p⁺ (→)

With an applied voltage V, it follows:

elementary charge

dynamic exchange current across the junction

thermal agitation (Arrhenius)

$$i_{p,\rightarrow} = i_{p,0} \cdot \exp\left[\frac{e_0 V}{kT}\right] \quad \text{and} \quad i_{p,\leftarrow} = i_{p,0}$$

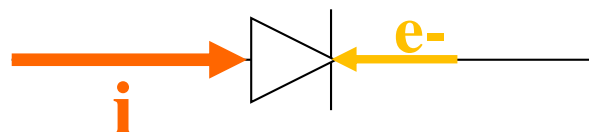
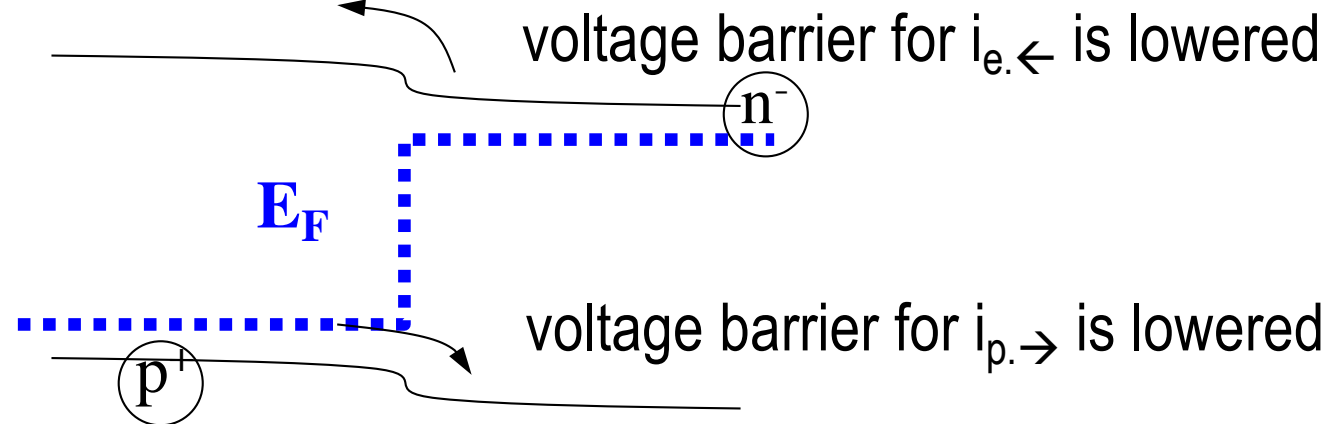
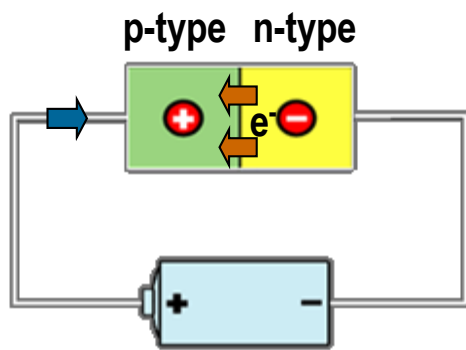
$$i_{tot} = i_e + i_p = i_{e,\rightarrow} + i_{e,\leftarrow} + i_{p,\rightarrow} + i_{p,\leftarrow}$$

$$i_{tot} = i_{e,0} \cdot \left(1 - \exp\left[-\frac{e_0 V}{kT}\right]\right) + i_{p,0} \cdot \left(1 + \exp\left[\frac{e_0 V}{kT}\right]\right)$$

Forward bias (direct bias)

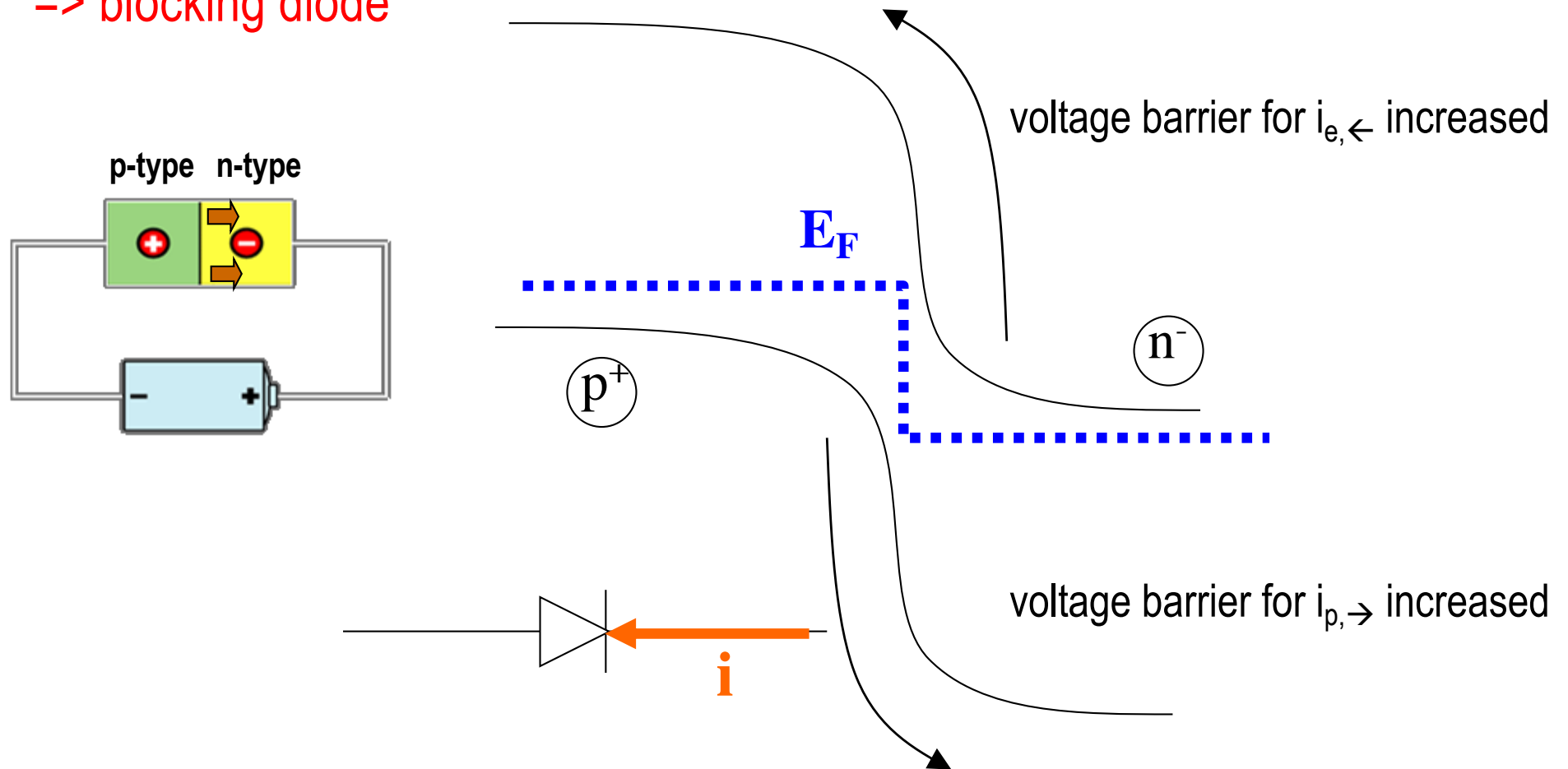
- $V_{\text{applied}} = \text{positive}$ between p and n (=anodic)
(= counteracting the band bending, reducing the internal electric potential)
- electrons from s.c. (n) are drawn into s.c. (p) (= the natural charge flow)
- => conducting diode

(above a threshold value, $V_{\text{applied}} \approx$ the internal electric potential)



Reverse bias (indirect bias)

- V_{applied} **negative** between p and n (= **cathodic**)
(= amplifying the band bending, increasing the internal electric potential)
- electrons from s.c. (**p**) are forced into s.c. (**n**) (= counternatural charge flow)
- => **blocking diode**



CHARACTERISTIC i-V (current-voltage curve) OF A DIODE

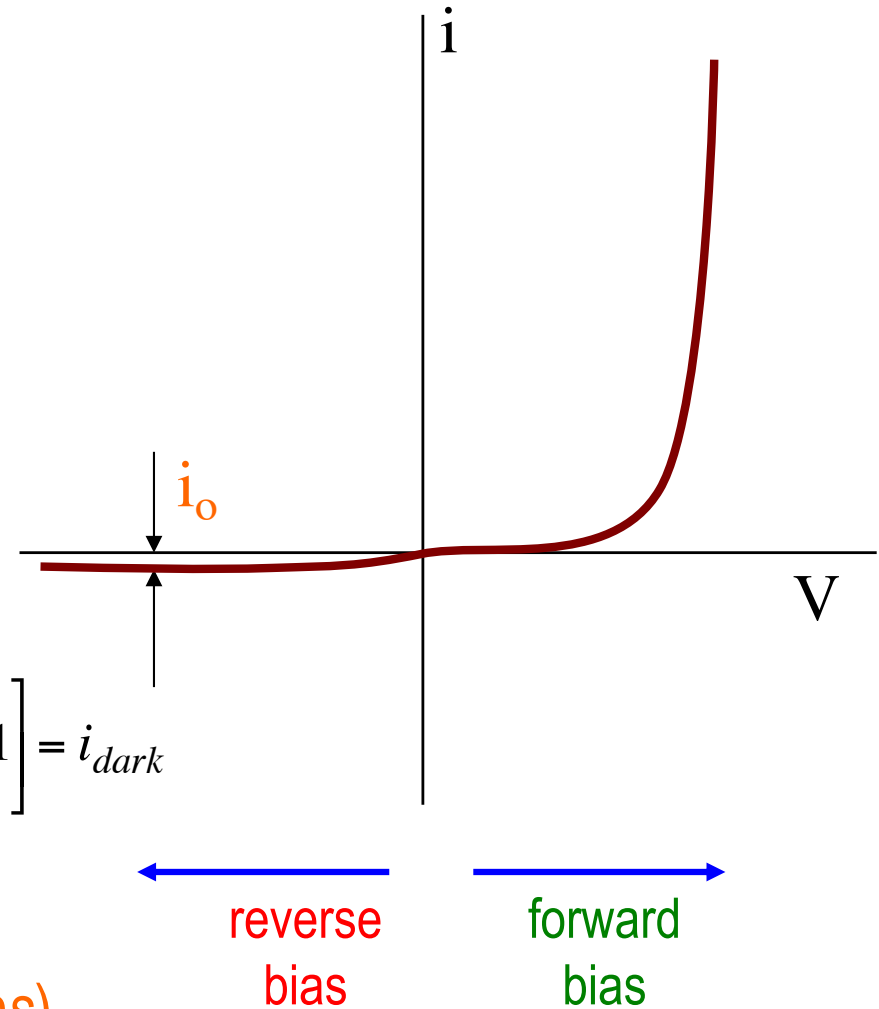
$$i_{p,\rightarrow} = i_{p,0} \cdot \exp\left[\frac{e_0V}{kT}\right] \quad \text{and} \quad i_{p,\leftarrow} = i_{p,0}$$

$$i_{e,\leftarrow} = i_{e,0} \cdot \exp\left[\frac{e_0V}{kT}\right] \quad \text{and} \quad i_{e,\rightarrow} = i_{e,0}$$

$$i_{e,tot} = i_{e,\leftarrow} - i_{e,\rightarrow} = i_{e,0} \cdot \left[\exp\left[\frac{e_0V}{kT}\right] - 1 \right]$$

$$i_{p,tot} = i_{p,\rightarrow} - i_{p,\leftarrow} = i_{p,0} \cdot \left[\exp\left[\frac{e_0V}{kT}\right] - 1 \right]$$

$$i_{tot} = i_{e,tot} + i_{p,tot} = \underbrace{(i_{e,0} + i_{p,0})}_{i_0} \cdot \left[\exp\left[\frac{e_0V}{kT}\right] - 1 \right] = i_{dark}$$

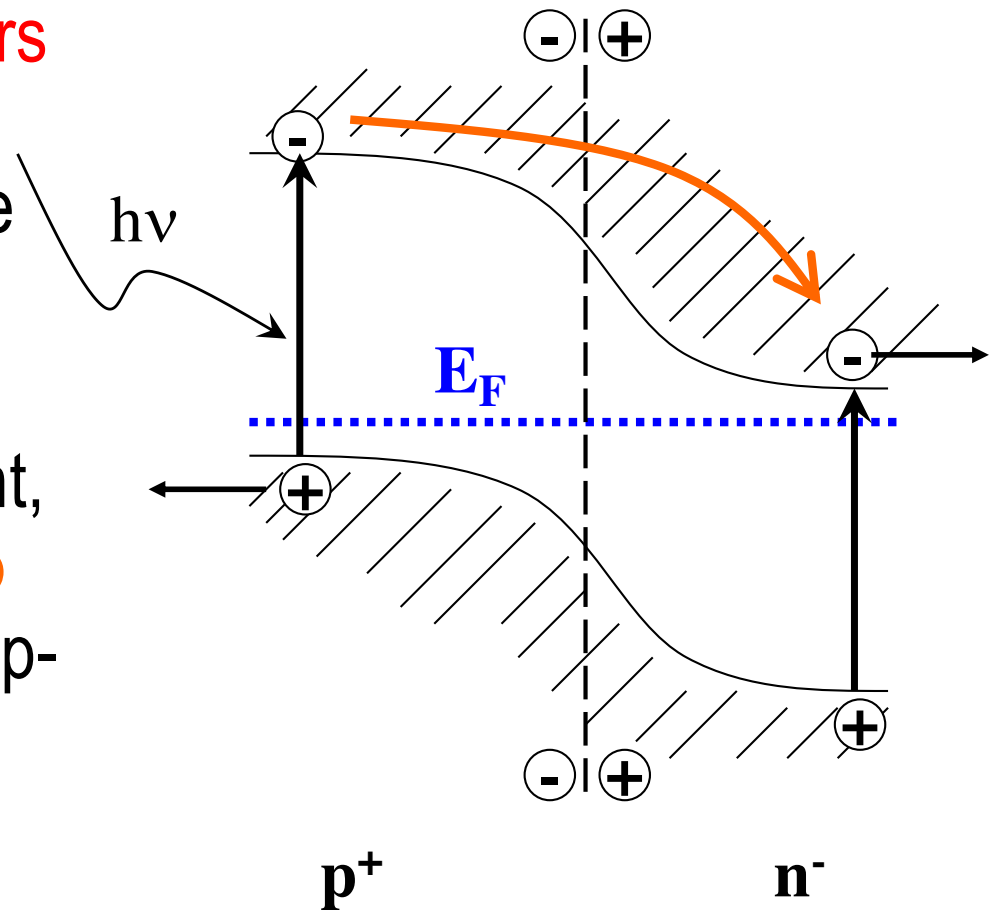


saturation or leakage current (< picoAmps)

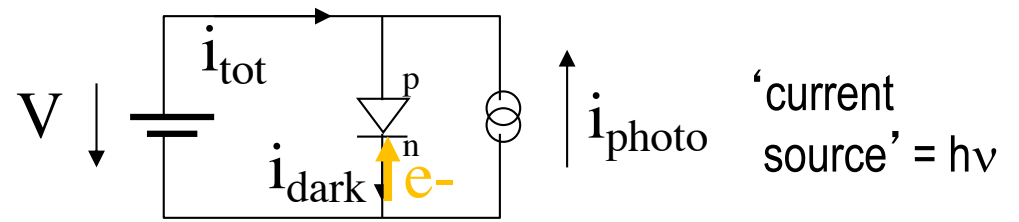
Illumination of a p-n diode (= PV solar cell)

- The photon energy $h\nu$ promotes electrons from bv to bc across the band gap.
- generation of charge carrier pairs (e^- , p^+) in the bv and bc bands, **and separation of these** by the **internal voltage barrier** (band bending) at the **p-n-junction**
- electrical current created by light, $h\nu$ (‘ i_{photo} ’), is thus **opposite to the natural charge flow** of the p-n diode (‘ i_{dark} ’)

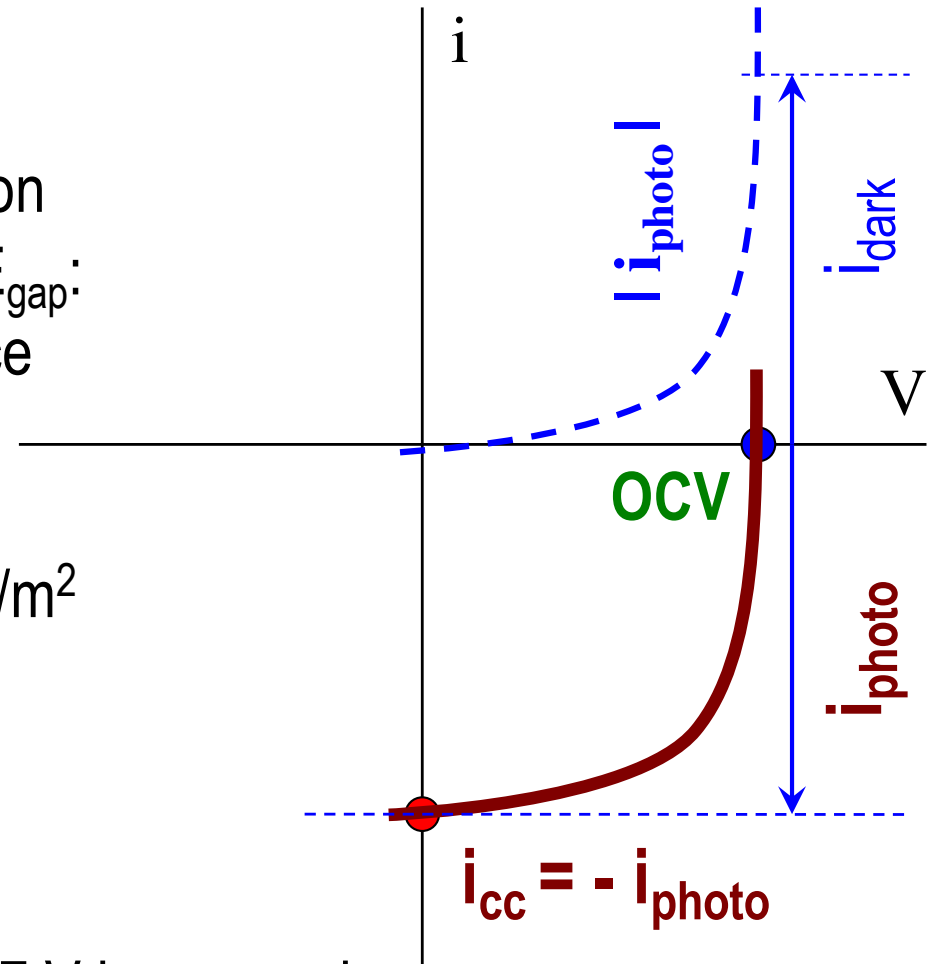
$$i_{\text{tot}} = i_{\text{dark}} - i_{\text{photo}}$$



$$i_{\text{tot}} = i_0 \left(\exp \left[\frac{e_0 V_{\text{appl}}}{kT} \right] - 1 \right) - i_{\text{photo}}$$



- for $V_{\text{appl}} = 0$, $i_{\text{tot}} = -i_{\text{photo}} = i_{\text{cc}}$:
 the short circuit current (i_{cc}) depends on
 the irradiance IRR and the bandgap E_{gap} :
 $i_{\text{cc}} = \text{sensibility } S \text{ (mA/mW)} * \text{IRR} * \text{surface}$
 $\rightarrow 42 \text{ mA/cm}^2$ in research,
 $\rightarrow 30 \text{ mA/cm}^2$ in practice
 for IRR = 50-100 mW/cm² = 0.5-1 kW/m²



- for $i_{\text{tot}} = 0$ (V_{OCV}), $i_{\text{dark}} = i_{\text{photo}}$:

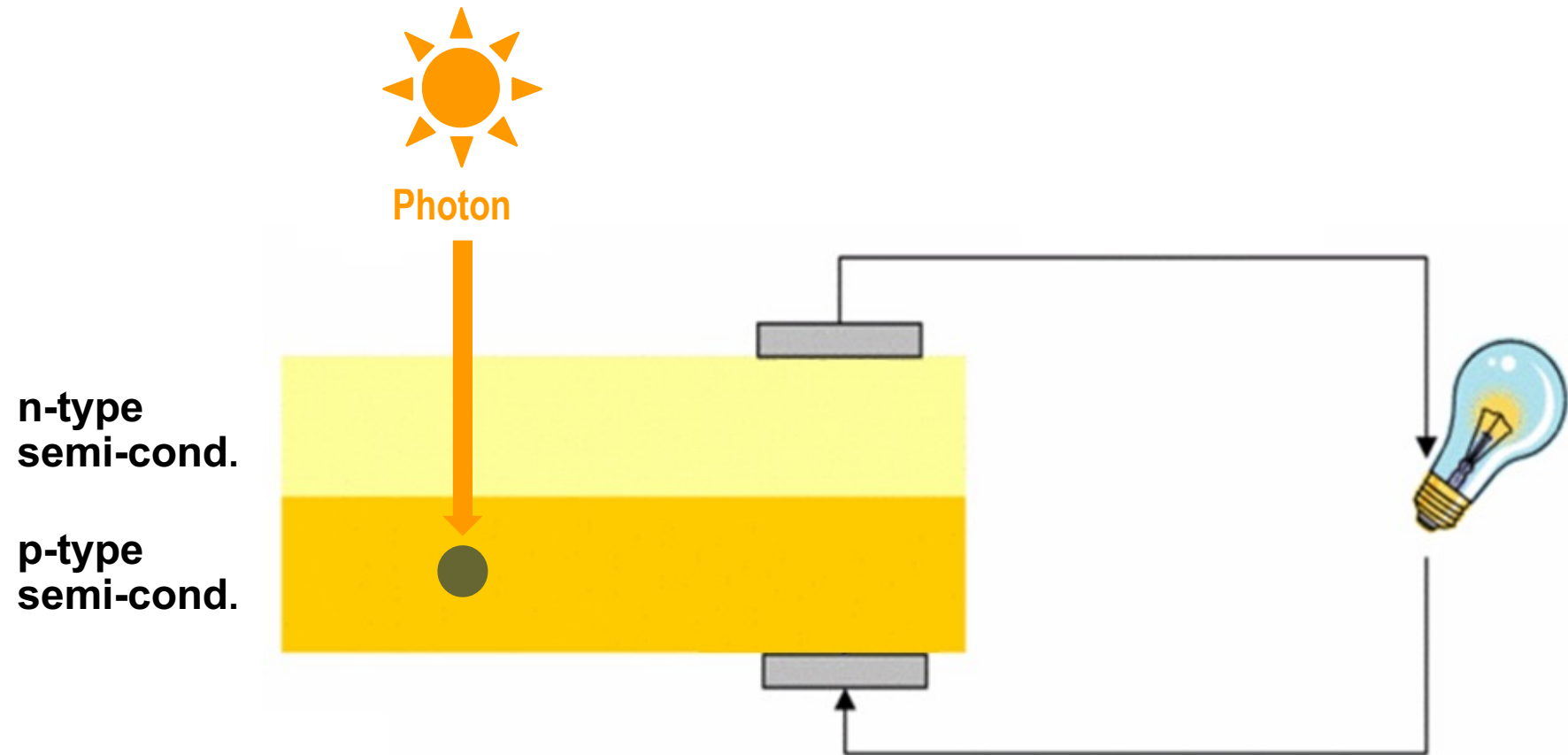
$$i_0 \left(\exp \left[\frac{e_0 V_{\text{OCV}}}{kT} \right] - 1 \right) = -i_{\text{cc}}$$

$$V_{\text{OCV}} = \frac{kT}{e_0} \ln \left(1 - \frac{i_{\text{cc}}}{i_0} \right) = V_T \ln \left(-\frac{i_{\text{cc}}}{i_0} \right)$$

- $\rightarrow 0.7 \text{ V}$ in research
- $\rightarrow 0.6 \text{ V}$ in practice

“thermal voltage”: 25.7 mV @ 298K

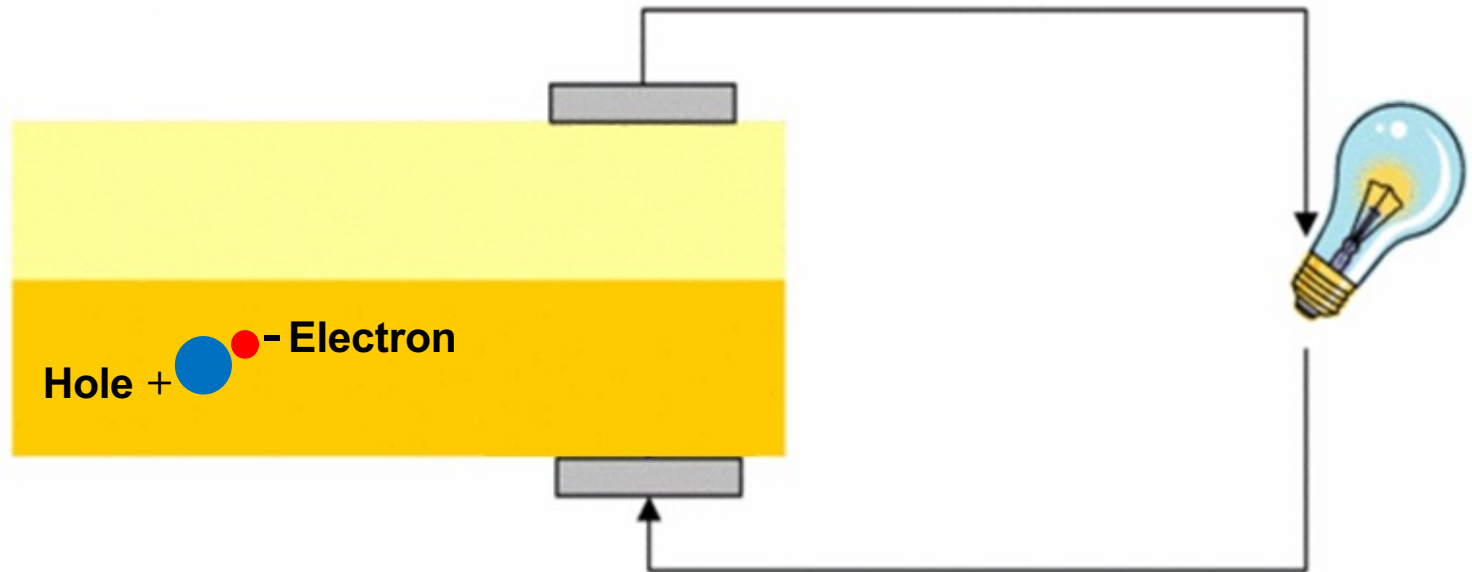
Animation:





**n-type
semi-cond.**

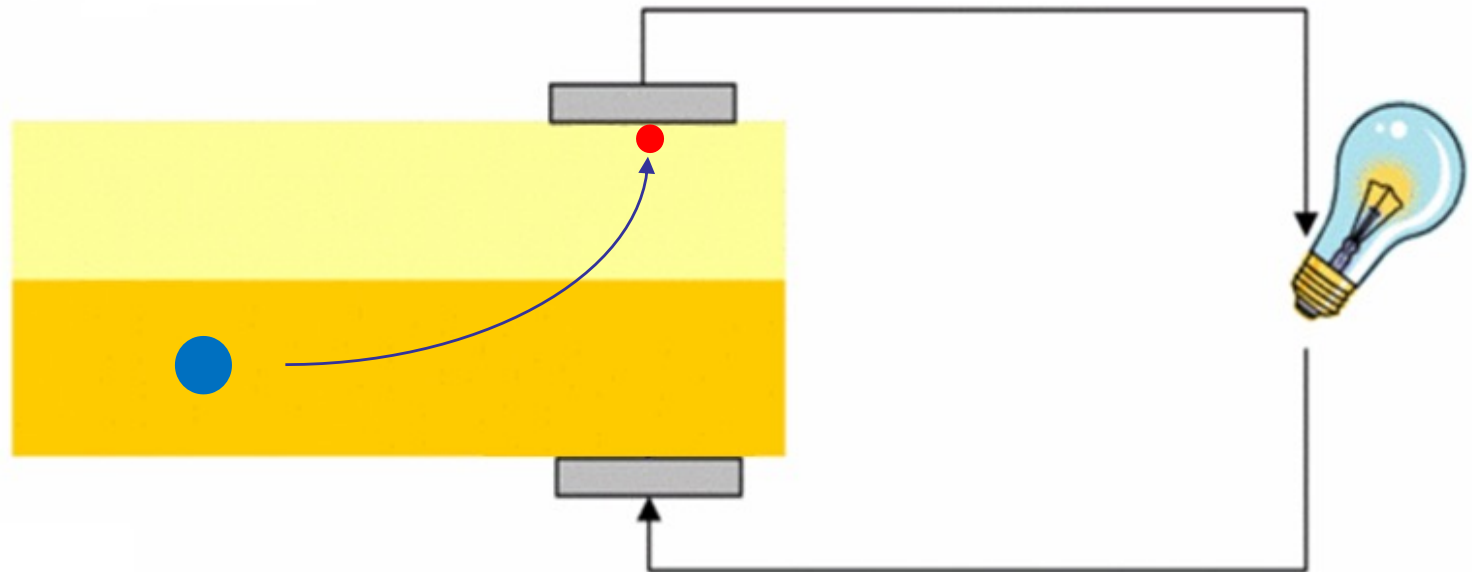
**p-type
semi-cond.**





**n-type
semi-cond.**

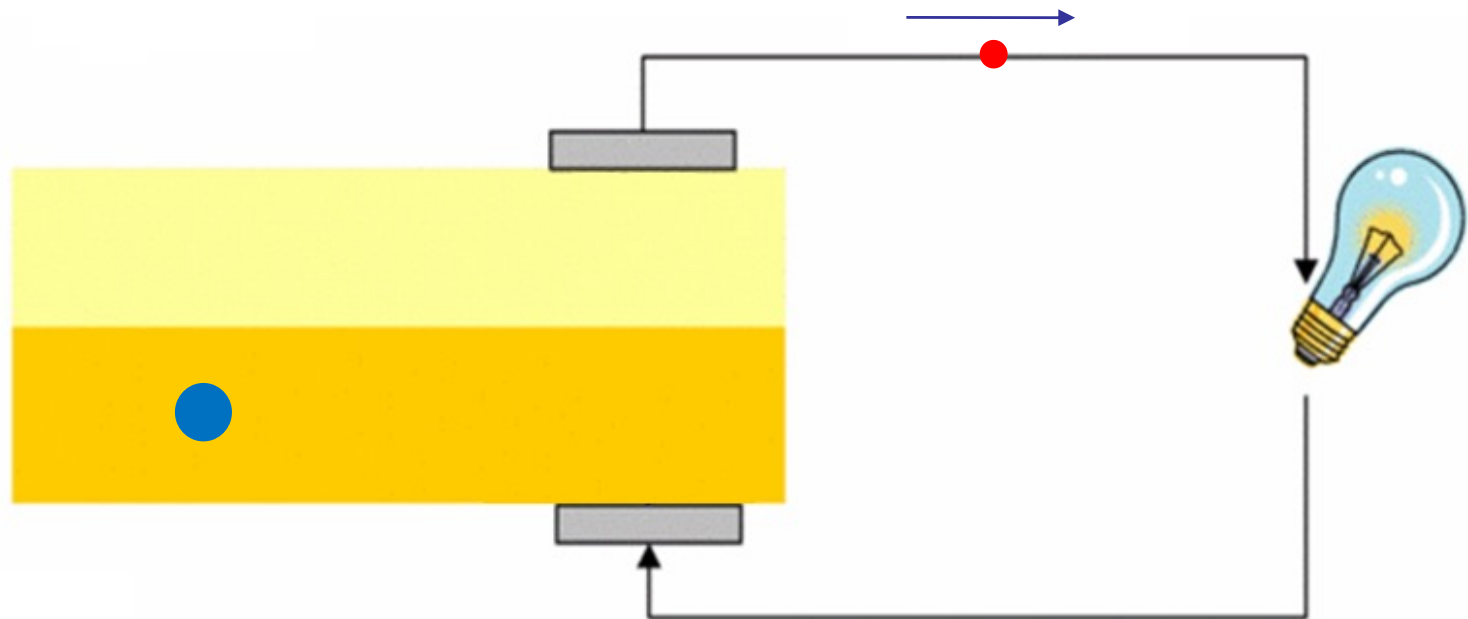
**p-type
semi-cond.**





**n-type
semi-cond.**

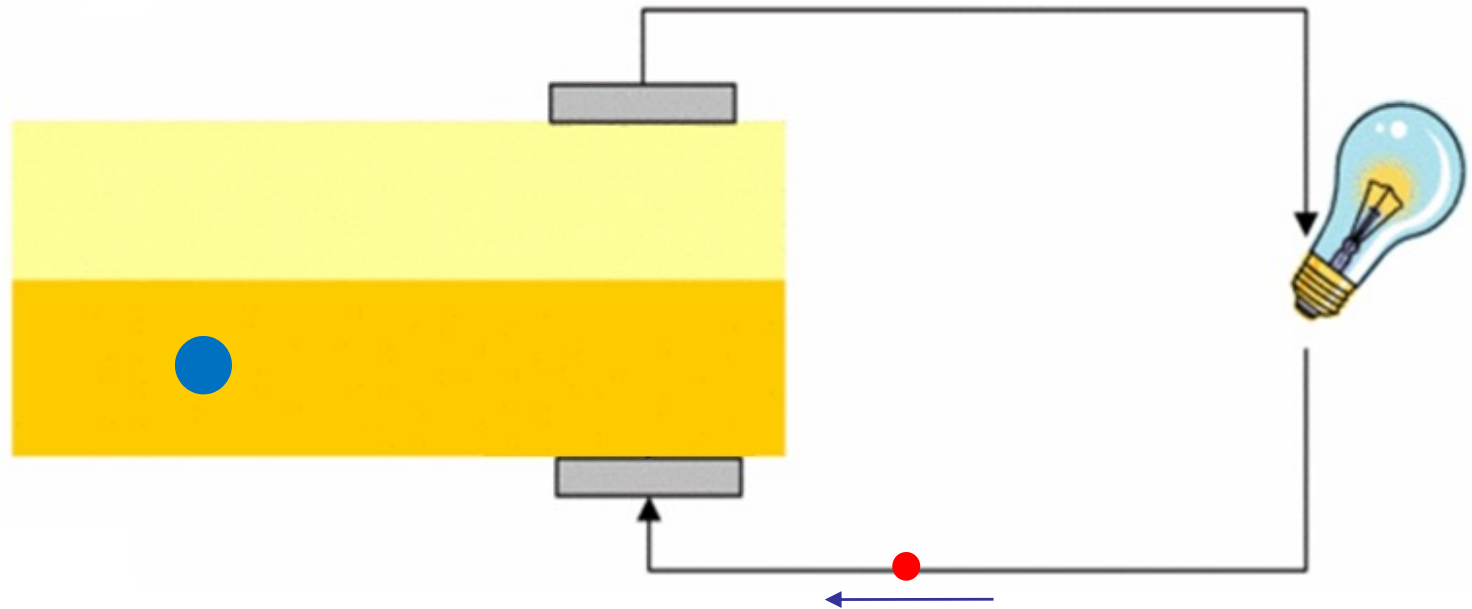
**p-type
semi-cond.**





**n-type
semi-cond.**

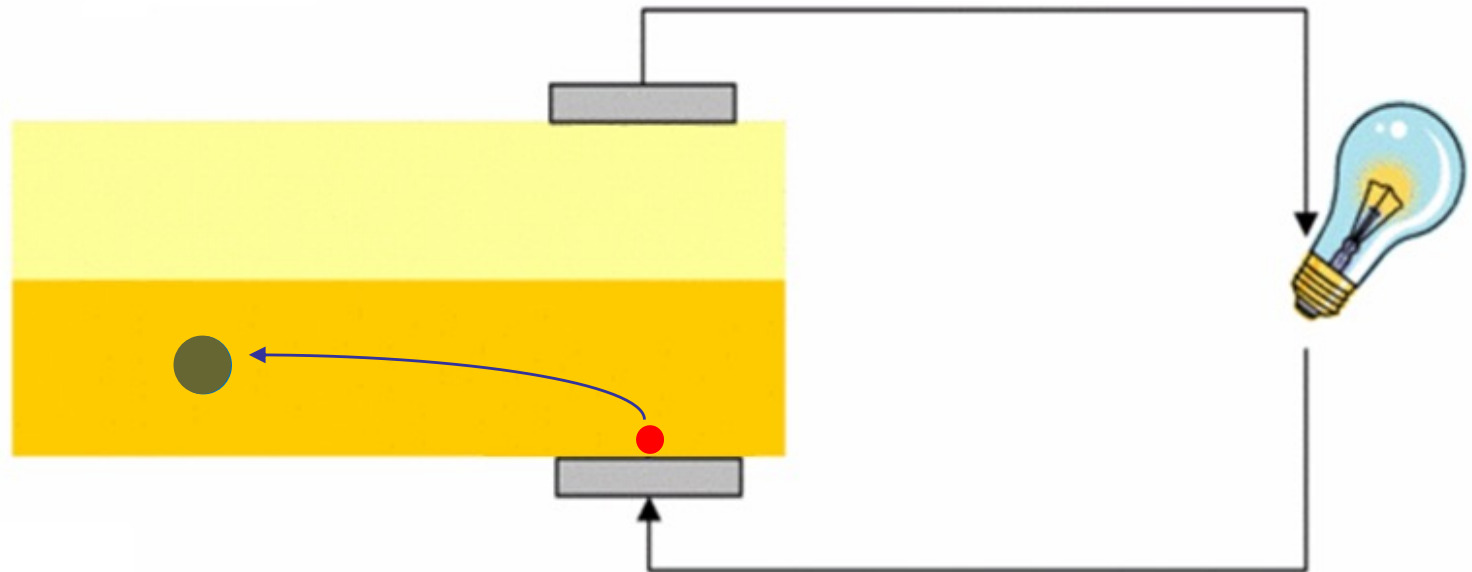
**p-type
semi-cond.**



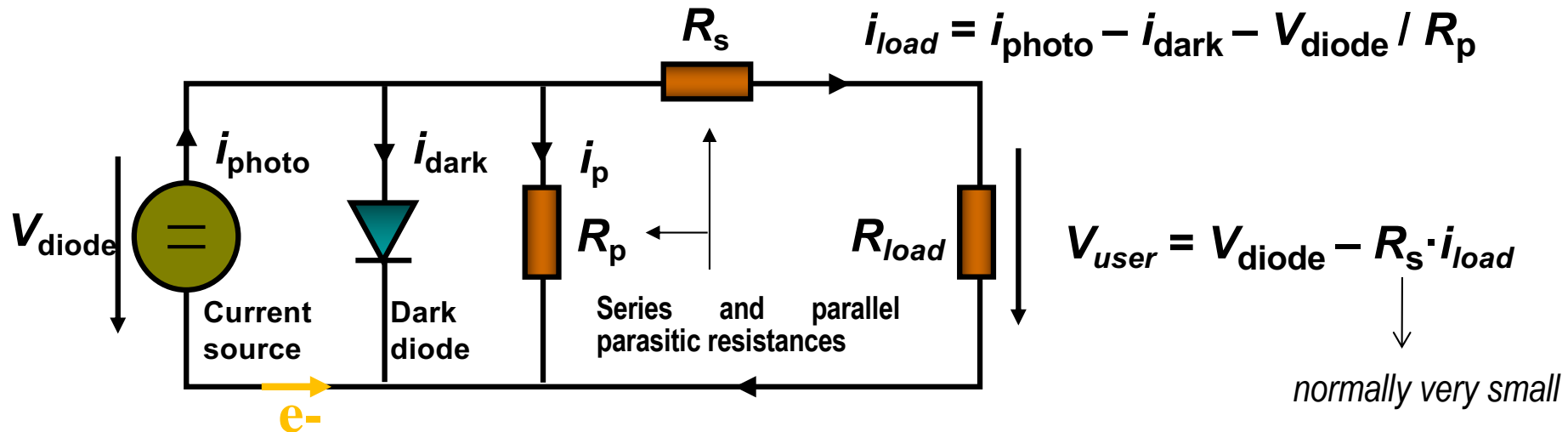


**n-type
semi-cond.**

**p-type
semi-cond.**



Equivalent electrical circuit, with a consumer (=load)



Diode characteristic: $i_{dark} = i_0 \cdot [\exp(e_0 V / kT) - 1]$

short-circuit current ($V_{user} = 0 \Rightarrow V_{diode} = R_s \cdot i_{load} \Rightarrow i_{load} = i_{photo} - i_{dark} - (R_s / R_p) \cdot i_{load}$
 $\Rightarrow i_{load} (1 + (R_s / R_p)) = i_{photo} - i_{dark}$

$V_{OCV} (i_{load} = 0; \text{ and } i_p \approx 0) :$

$$i_{photo} = i_{dark} = i_0 \left(\exp\left[\frac{e_0 V_{OCV}}{kT}\right] - 1 \right)$$

$$i_{photo} + i_0 = i_0 \exp\left[\frac{e_0 V_{OCV}}{kT}\right] \longrightarrow V_{OCV} = \frac{kT}{e_0} \cdot \ln\left[\frac{i_{photo}}{i_0} + 1\right] = V_T \cdot \ln\left[\frac{i_{cc}}{i_0}\right]$$

Power from a solar cell ('fill-factor')

- Power $P = I \cdot V$

$$P = V * \left[i_{cc} - i_0 \left(\exp \left[\frac{e_0 V}{kT} \right] - 1 \right) \right]$$

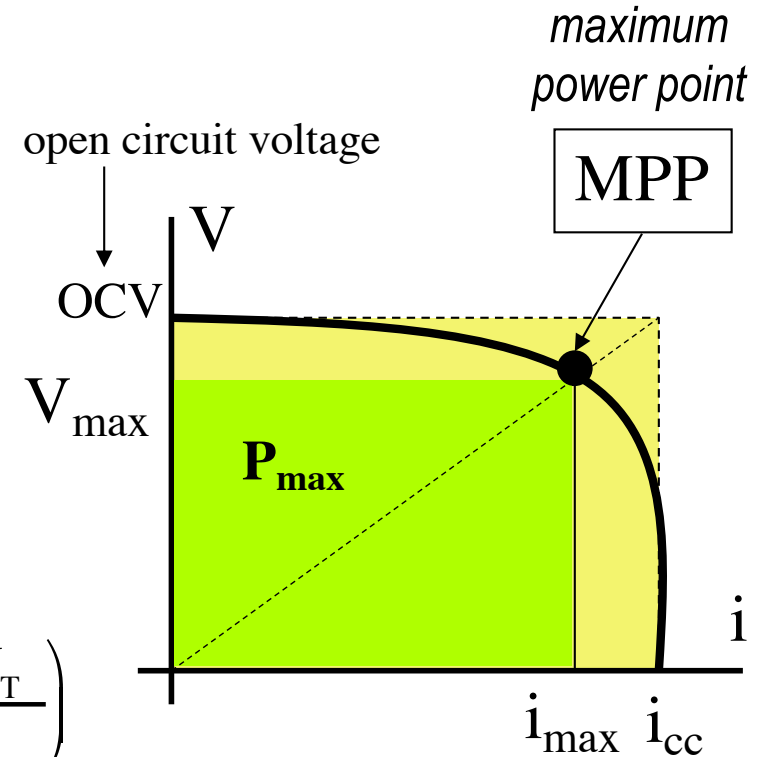
- Fill-factor FF (%): 

$$FF = \frac{P_{max}}{V_{OCV} \cdot I_{cc}} \quad V_{max} = V_{OCV} + V_T \ln \left(\frac{V_T}{V_{max}} \right)$$

$$FF = \frac{V_{max}}{V_{OCV}} \left[1 - \frac{\exp \left(\frac{V_{max}}{V_T} \right) - 1}{\exp \left(\frac{V_{OCV}}{V_T} \right) - 1} \right]$$

→ FF = 0.83 in research

→ FF = 0.70 in practice



Solar cell efficiency

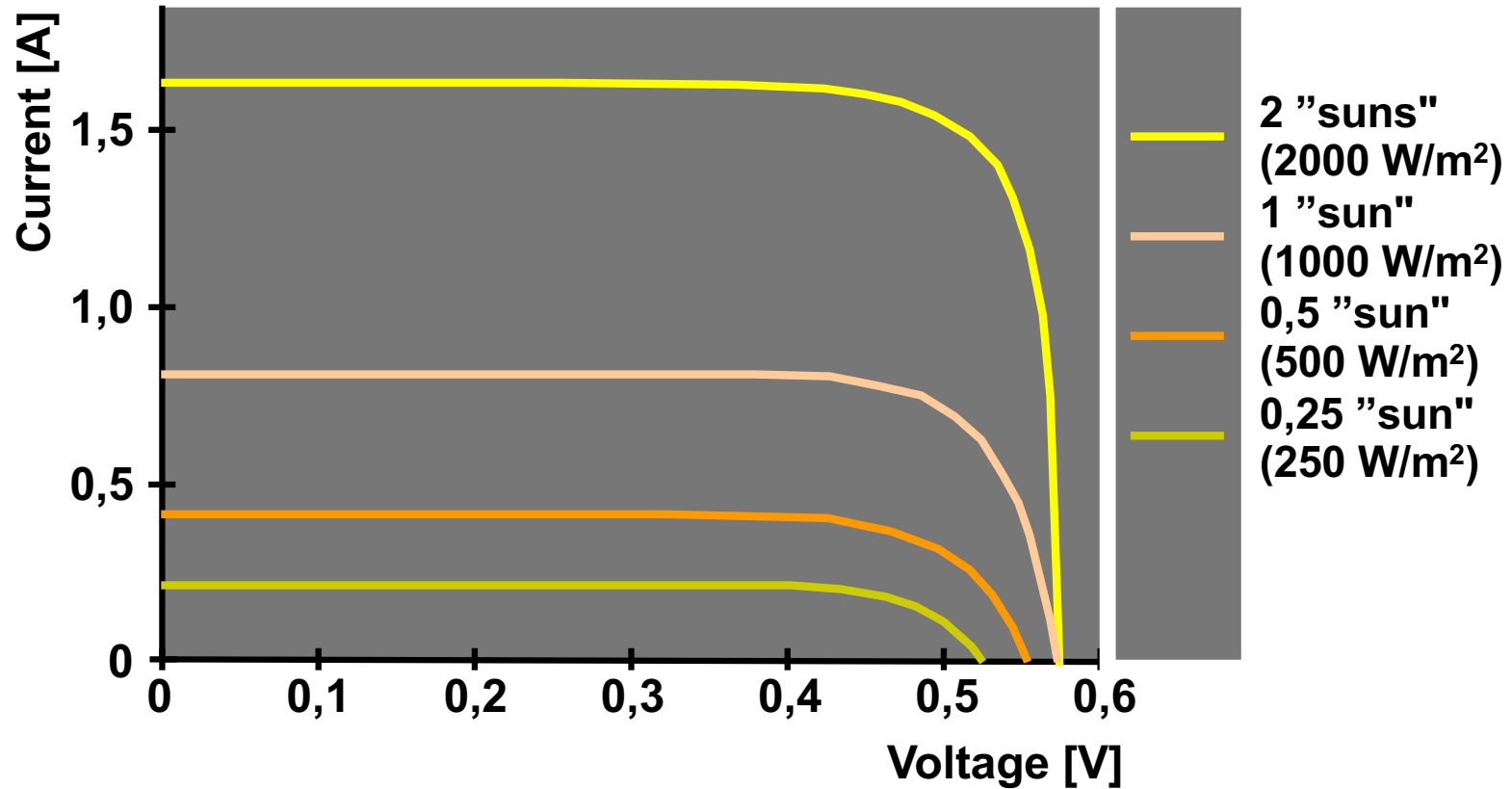
$$\eta = \frac{P_{\max}}{\text{irradiance} \left[\frac{W}{cm^2} \right] * \text{surface}} = \frac{P_{\max}}{i_{cc} \left[\frac{A}{cm^2} \right] / \text{sensibility } S \left[\frac{A}{W} \right]} = S.FF.V_{OCV}$$

in research: $\eta = 29\%$ (Si), in practice: $\eta = 15\%$

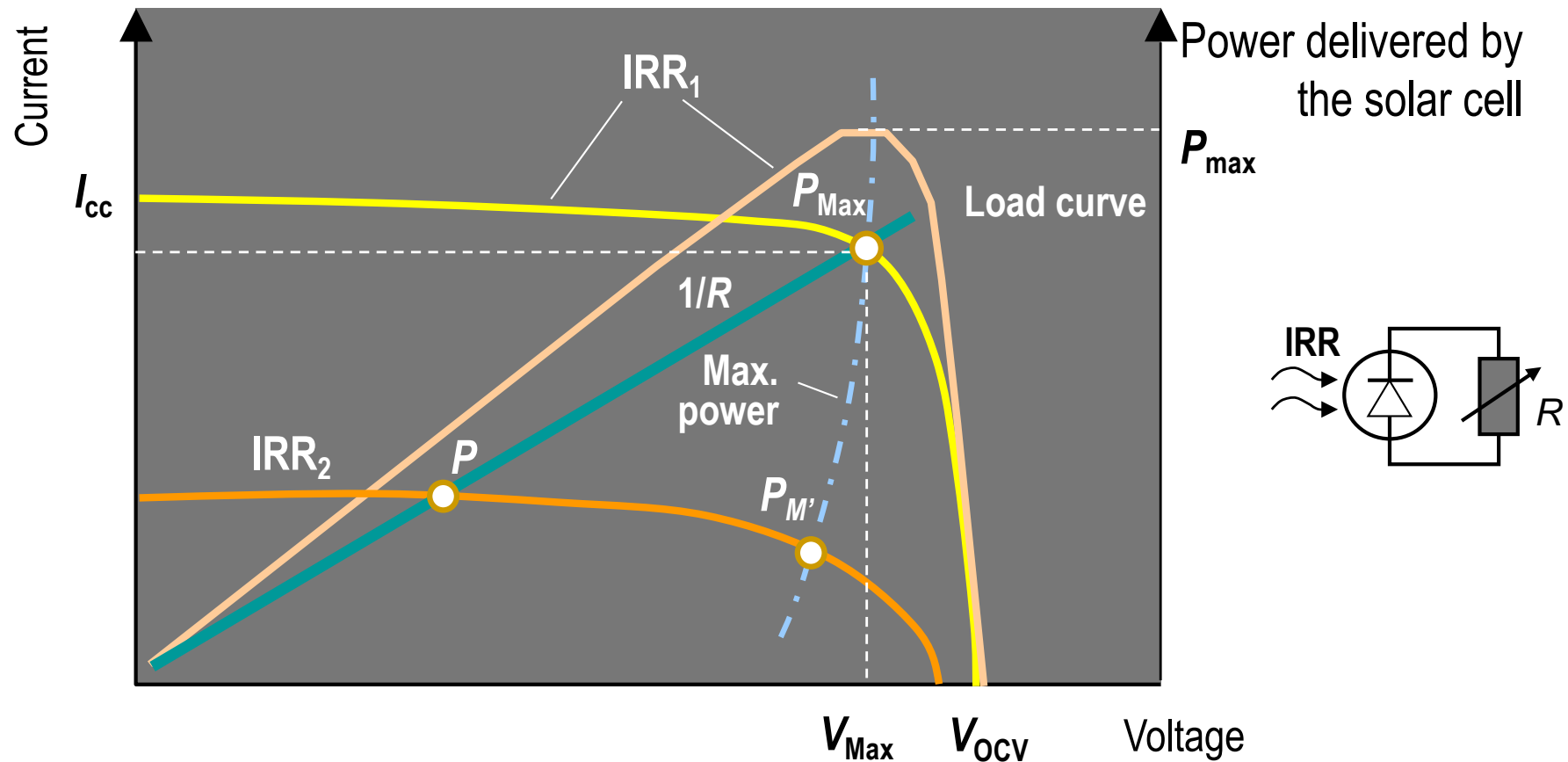
Effect of temperature :

- $dV/dT = \text{ca. } -2 \text{ mV/K}$
- very small effect on i_{cc} (IRR is more important)
- best location for solar panels = high mountain area (cold; snow albedo ($IRR_{\text{effective}} = IRR_{\text{incident}} * 1.3$))

i-V characteristic under variable irradiation



Real operation with consumer (=load R)



\Rightarrow MPP : maximum power point tracking

Summary of useful formulas

$$V_{OCV} = \frac{kT}{e_0} \cdot \ln \left[\frac{i_{photo}}{i_0} + 1 \right] = V_T \cdot \ln \left[\frac{i_{cc}}{i_0} \right]$$

$$V_{max} = V_{OCV} + V_T \ln \left(\frac{V_T}{V_{max}} \right) \quad i_{max} = i_{cc} \left(1 - \frac{V_T}{V_{OCV}} \right)$$

$$FF = \frac{P_{max}}{V_{OCV} \cdot I_{cc}}$$

$$\eta = \frac{P_{max}}{\text{irradiance} \left[\frac{W}{cm^2} \right] * \text{surface}}$$

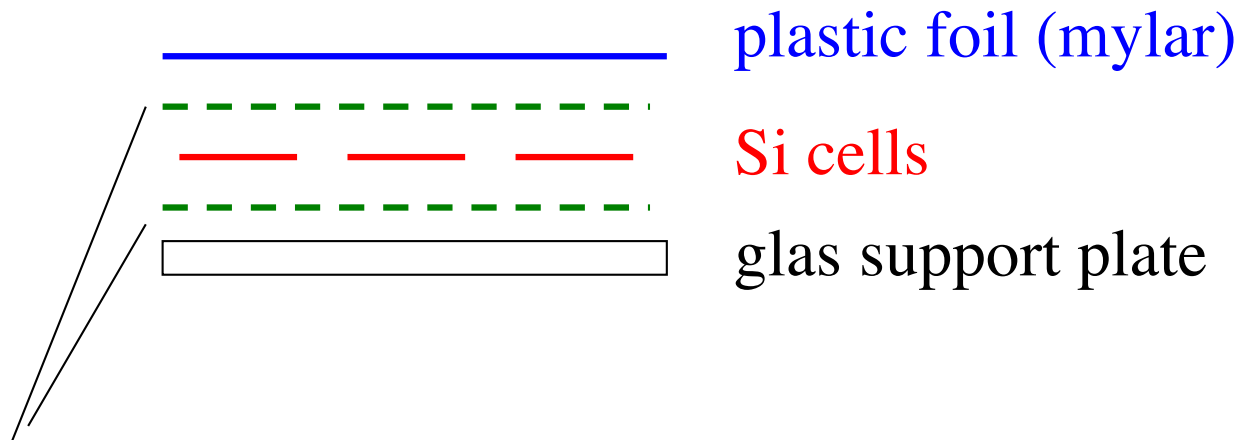
Solar panels

- series + parallel connection of cells (each cell = 100 cm²),
f.ex. 30 in series (30 mA/cm² @ 0.5 V) → 15 V x 3 A
- cells are *classified* according to their i_{cc} - value
- **MPP : maximum power point tracking**
- to avoid “hot spots” (= a cell in reverse bias), *shunt* diodes are used to deviate excess current

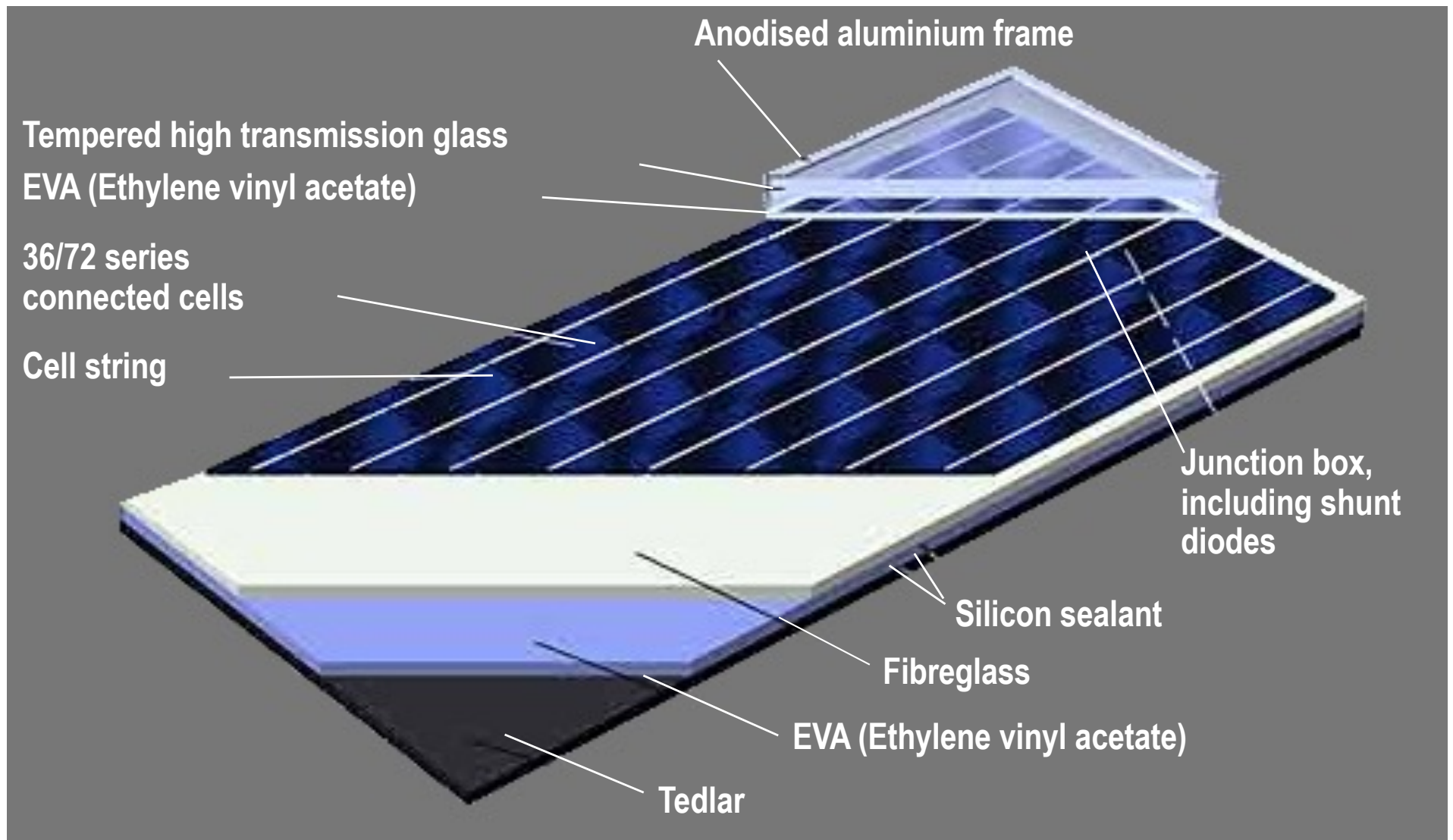
f.ex. a tree leaf falls on a cell and blocks the sunlight

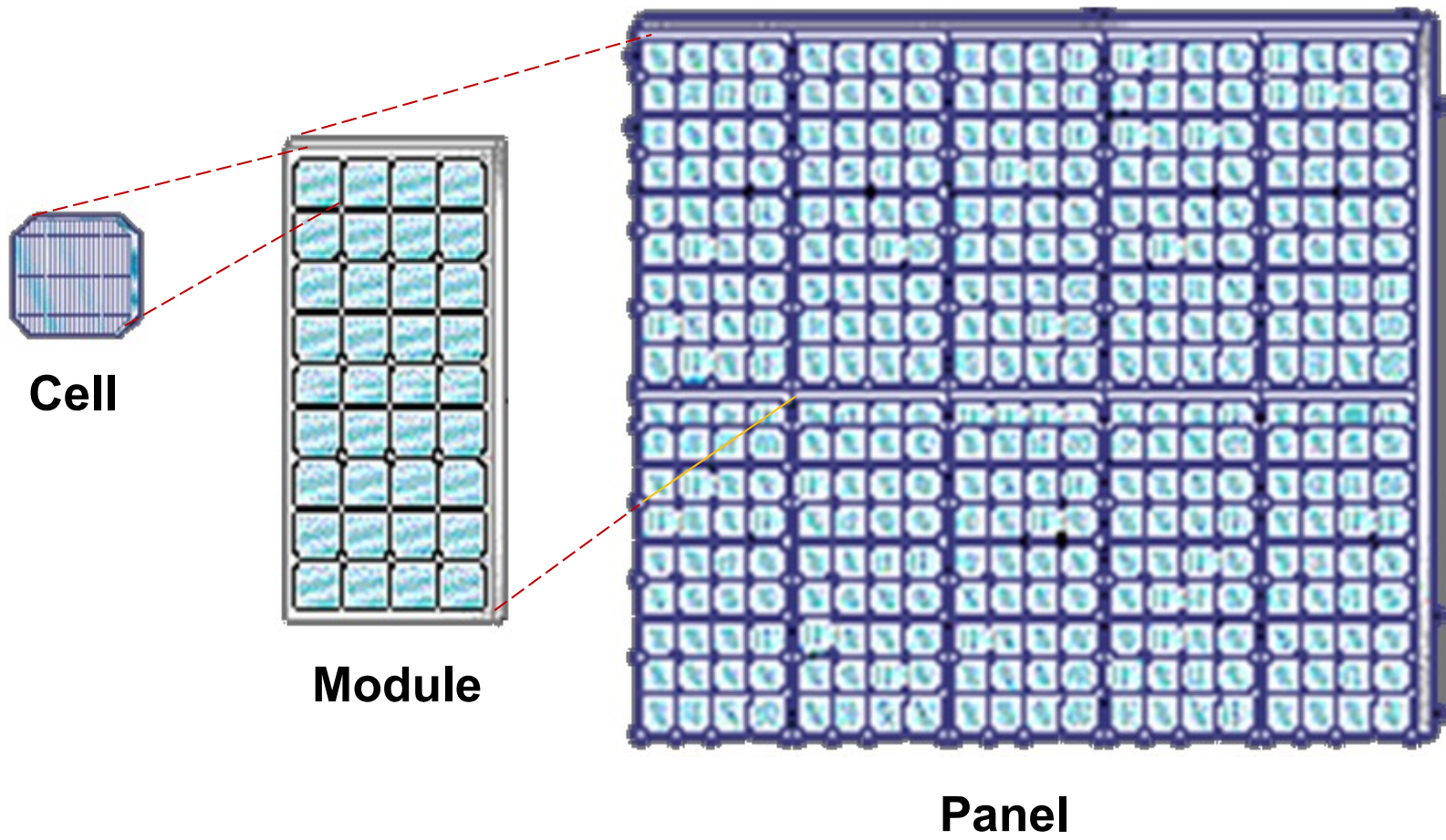
P.V. module assembly

series of cells in 4 x 8 or 3 x 12 arrangement
(classified by the i_{cc} - value)



EVA : EthyleneVinylAcetate polymer
(liquefied to 150° C, then cooled to remove air bubbles)



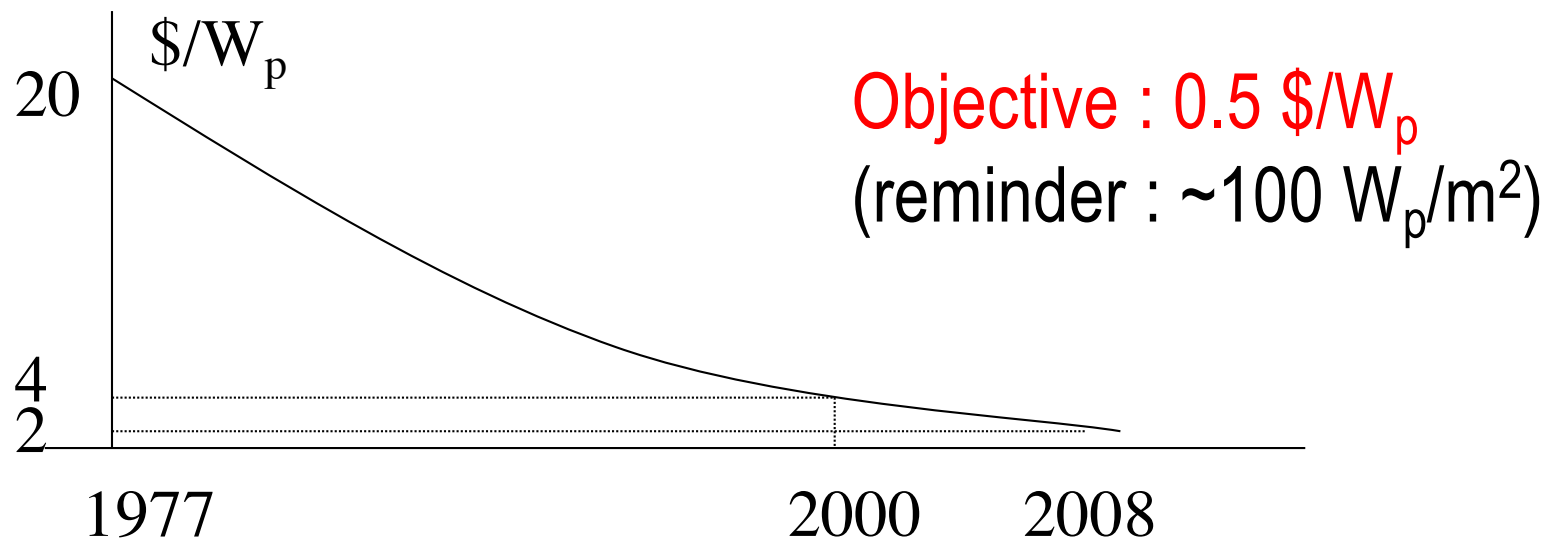


Solar PV 'power plants'

- should be $>100 \text{ kW}_p$, to benefit from an economy of scale and a very efficient **DC/AC inverter**
- connection at 400 V
- with batteries, disjunctors, fuses
- existing installations from 100 kW_p to 10 MW_p
e.g. 10 MW_p (800 x 800 m), efficiency 15%, load factor 18%,
needs IRR of $\geq 1800 \text{ kWh/m}^2\cdot\text{yr}$

Market

- **1185 GW_p** installed late 2022
- **1040 TWh** produced (almost 4% of world electricity)
- consistent growth of **>20% / yr**
- monopolised by silicon technology



Recombinations

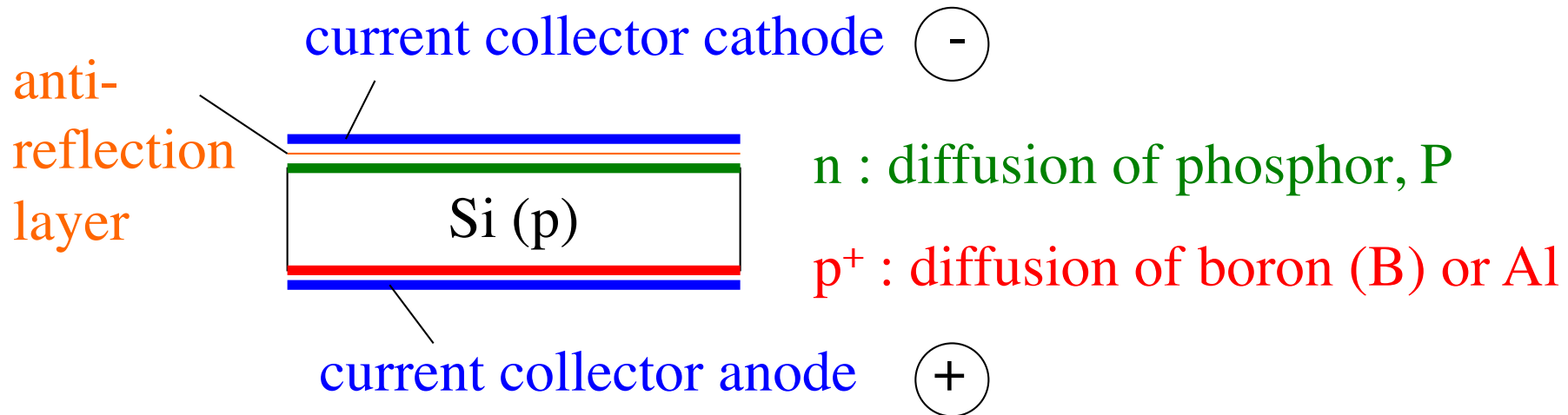
mechanisms of **destruction of charge** carriers (e^- , p^+) (=losses)

1. return of electrons from bc band to bv band, emitting a photon (**luminescence**) : this effect is very small in Si
2. SRH (**Shockley-Read-Hall**) : **impurities** and structural **defects** capture e^- and p^+ (= recombination centers, occurring in cascade between the bc and bv energy levels);
→ to reduce this effect : **ultrapure** material is needed (→ up to **monocrystals**)
3. effect **Auger** (in heavily doped s.c.): the recombination energy is transferred to a third particle (e^- or p^+) as kinetic energy

global recombination rate: $\sim 1/\tau_p$ (n-type) or $\sim 1/\tau_n$ (p-type)

with τ = lifetime of (e^- , p^+) : nano- to milliseconds

Solar cell layers, in more detail



Incident photons in Si(p) create the pairs (e^- , p^+), with
 e^- migrating to n and via the external circuit to the anode
 p^+ migrating to p⁺ and via the external circuit to the cathode

$$e_{\text{out}} = i_n = -e_0 \int_{\text{volume } V} (g - r) dV$$

g : pair generation rate (e,p)
 r : recombination rate

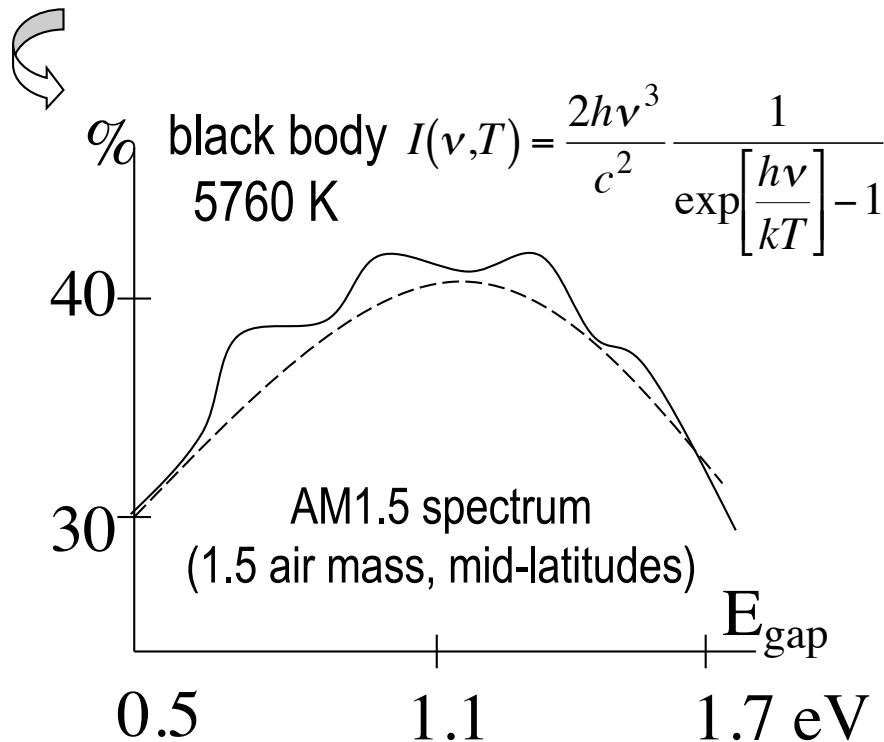
$$p_{\text{out}} = i_p = e_0 \int_{\text{volume } V} (g - r) dV$$

Theoretical efficiency

In theory : photons are generated at 5760 K (sun surface temperature)

→ Carnot efficiency at 293K would then be 95% ...

A detailed treatment shows that in practice we find :



Remark :

a high energy photon can create several pairs (e^- , p^+) !

A stack of cells with decreasing E_{gap} can increase the efficiency (record = 44%).

for a single cell: record for Si = 29%

PV technology

- Fabrication of **high purity Si**
- Fabrication of crystalline Si (3 methods)
- Cutting to wafers and cells
- Costs
- New technologies
 - thin layers (amorphous Si)
 - concentration cells (reflected light multiplication)

									VIIIA
									2 He 4.003
		IIIA	IVA	VA	VIA	VIIA			10
		5 B 10.811	6 C 12.011	7 N 14.007	8 O 15.999	9 F 18.998			Ne 20.183
		13 Al 26.982	14 Si 28.086	15 P 30.974	16 S 32.064	17 Cl 35.453			18 Ar 39.948
	IB	IIB							
29 Cu 63.54	30 Zn 65.37	31 Ga 69.72	32 Ge 72.59	33 As 74.922	34 Se 78.96	35 Br 79.909			36 Kr 83.80
47 Ag 107.870	48 Cd 112.40	49 In 114.82	50 Sn 118.69	51 Sb 121.75	52 Te 127.60	53 I 126.904			54 Xe 131.30
79 Au 196.967	80 Hg 200.59	81 Tl 204.37	82 Pb 207.19	83 Bi 208.980	84 Po (210)	85 At (210)			86 Rn (222)

PV technologies: an overview

Crystalline silicon (c-Si) modules represent 85-90% of the global annual market today. C-Si modules are subdivided in two main categories: *i)* single crystalline (sc-Si) and *ii)* multi-crystalline (mc-Si).

Thin films currently account for 10% to 15% of global PV module sales. They are subdivided into three main families: *i)* amorphous (a-Si) and micromorph silicon (a-Si/ μ c-Si), *ii)* Cadmium-Telluride (CdTe), and *iii)* Copper-Indium-Diselenide (CIS) and Copper-Indium-Gallium-Diselenide (CIGS).

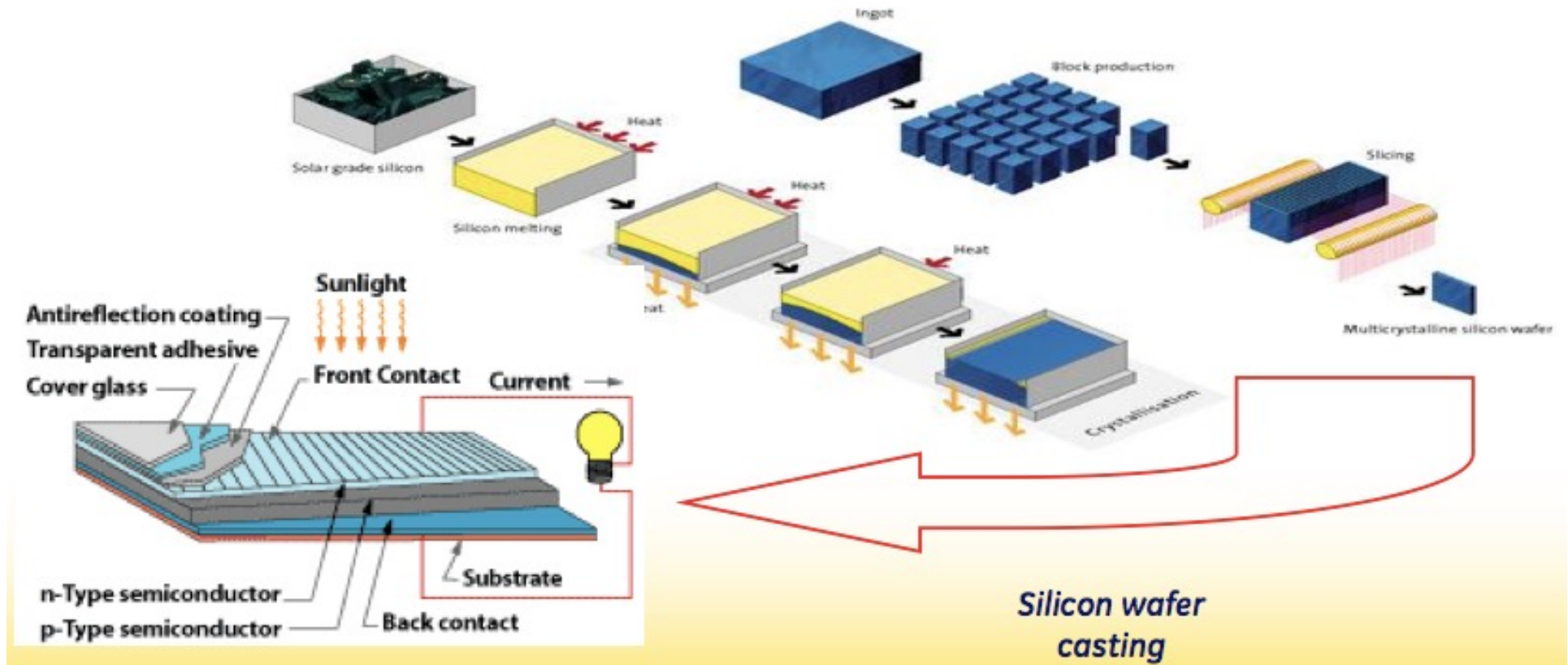
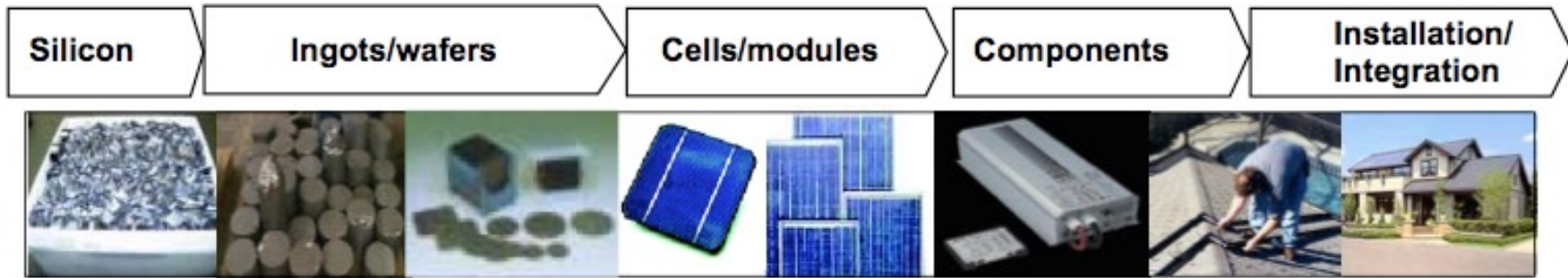
Emerging technologies encompass advanced thin films and organic cells. The latter are about to enter the market via niche applications.

Concentrator technologies (CPV) use an optical concentrator system which focuses solar radiation onto a small high-efficiency cell. CPV technology is currently being tested in pilot applications.

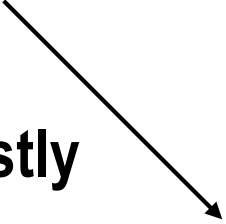
Novel PV concepts aim at achieving ultra-high efficiency solar cells via advanced materials and photo-chemical processes. They are currently the subject of basic research.

Detailed information on technologies can also be found in the IEA PVPS Implementing Agreement website www.iea-pvps.org

Solar PV value chain



Silicon PV technology

- Silicon : > 80% of the market
 - for Si only:
 - 40% monocrystalline
 - 25% polycrystalline
 - 35% amorphous
 - $E_{\text{bandgap}} = 1.12 \text{ eV}$ (= close to the optimum of the solar spectrum)
 - bad infrared absorption → **wafer must be thick** : 0.3 mm
→ disadvantage: long current path for (e^- , p^+)
 - must then be **ultrapure** to avoid recombinations : **costly**
- 
- diamond saw: 0.35 mm thick (14 wafers/cm)
→ 50% per wafer high purity Si is lost by sawing!
 - multi-wire saw : 0.15 mm thick (30 wafers/cm)

Ultrapure Si fabrication

- 1) reduction of sand, SiO_2 , by carbon :
 $\text{SiO}_2 + \text{C} \rightarrow \text{Si} + \text{CO}_2$ 98.7% pure, 1-3 €/kg
(CO_2 – emissions !)
- 2) chlorination: $\text{Si} + 3 \text{HCl} \rightarrow \text{SiHCl}_3$ (liq.) + H_2
then purification (till 2 ppb) by distillation
- 3) reduction of SiHCl_3 by H_2 (= the reverse of reaction 2) at
 1100°C : impurities down to 0.1 ppb, powder of 50 €/kg

Crystalline Si (3 methods)

- 1) **Czochralski** method (**costly**) : fusion at **1440° C**, growth of a tube (L=1 m, ϕ =30 cm) for 24 h, Si utilisation of 70%
- 2) **Floating-zone** method (**very costly**): polycrystalline Si is remolten against a monocrystal (no contamination, no loss), tubes of ϕ 10 cm
- 3) **Siemens** method (cheapest): molten block of 40x40x40 cm³ is cooled to 1 cm grains (*polycrystalline*)

Cell fabrication, step-by-step

- 1) chemical surface attack by **hot NaOH or HF** → **texturisation** (20 μm) to **reduce** the surface light **reflexion** from 40% to 15%
- 2) diffusion of phosphorous in the surface (+oxidation at **900° C**): n^-
- 3) screenprinting of aluminium on the back + fusion (**700° C**) : creation of the p^+ layer
- 4) deposition of silver-glass on the front (cathode collector) by screenprinting
- 5) deposit of silver on the back (aluminium) by screenprinting (anode)
- 6) titanium vapor treatment (**400° C**) on the front → TiO_2 layer for **antireflection** (reduced to 1-5%)
- 7) plasma attack** to remove n^- edges (phosphorous)

Payback time

- the ‘energy’ payback time is the duration the device has to operate in order to deliver the energy invested in fabrication:
 - 1.5 to 3.5 yr for crystalline Si
 - 1 to 1.5 yr for amorphous Si
- Remark : for solar thermal absorbers: < 1 yr

Alternative Technologies

- Objectives

- reduce the cost per module/m² ——— amorphous Si as thin layers
- increase the efficiency ————— concentration cells

- achieve >20% with cost effective manufacturing
(→ reduction from 3 to 2 €/W_p)

Thin film technology

- lower quality and efficiency, but lower cost (6\$/kg vs. 53\$/kg)
- short current paths : charge carrier lifetime τ can be short
- non-saturated Si (α -Si, Si:H), containing 10% H₂ (1.75 eV) : deposited from SiH₄ plasma at 250° C
- 40 μm thick
- continuous fabrication of the module simultaneously to the cells

Thin film technology

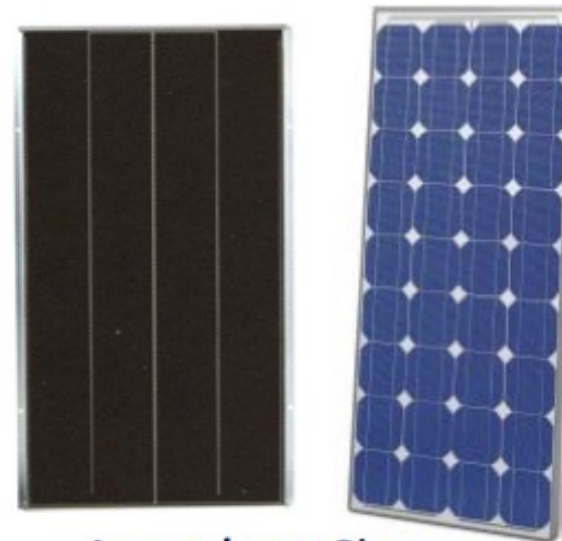
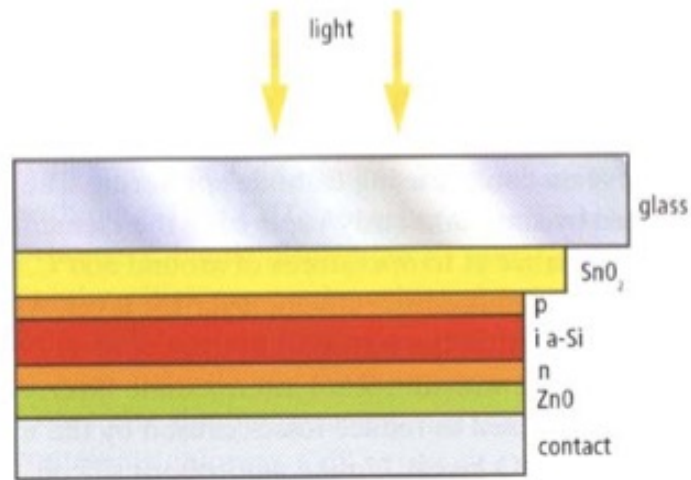
Challenges:

- lower efficiency (10% in research, 5% in modules)
 - improved by tandem concept (successive layers of $< 1 \mu\text{m}$ of SiC:H (2eV), Si:H (1.7 eV), SiGe:H (1.3 eV)) : 10% possible)
- intrinsic instability (rapid impurification)

Other thin layers :

- CIS (CuInSe_2 , $2 \mu\text{m}$, 1.1 eV) : 17% efficiency on module
- CdTe (1.5 eV, low cost by screenprinting, stable) : 17% on module

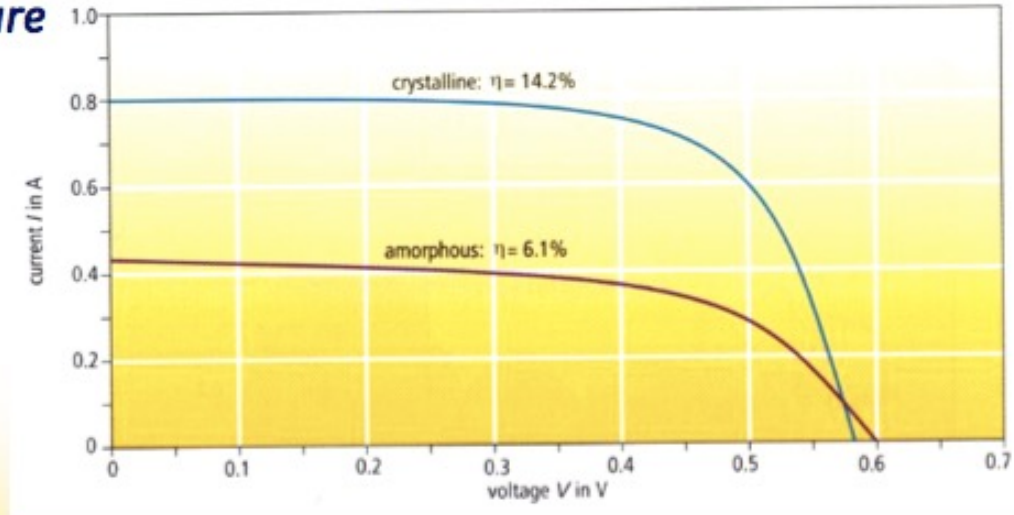
Thin film energy generation



Amorphous Si vs. Crystalline Si module

Amorphous Si thin film device structure

- pin diode consists of three separate thin a-Si films
- a thin conductive oxide on the glass serves as a window



Amorphous Si vs. crystalline Si I-V characteristic

Earthscan

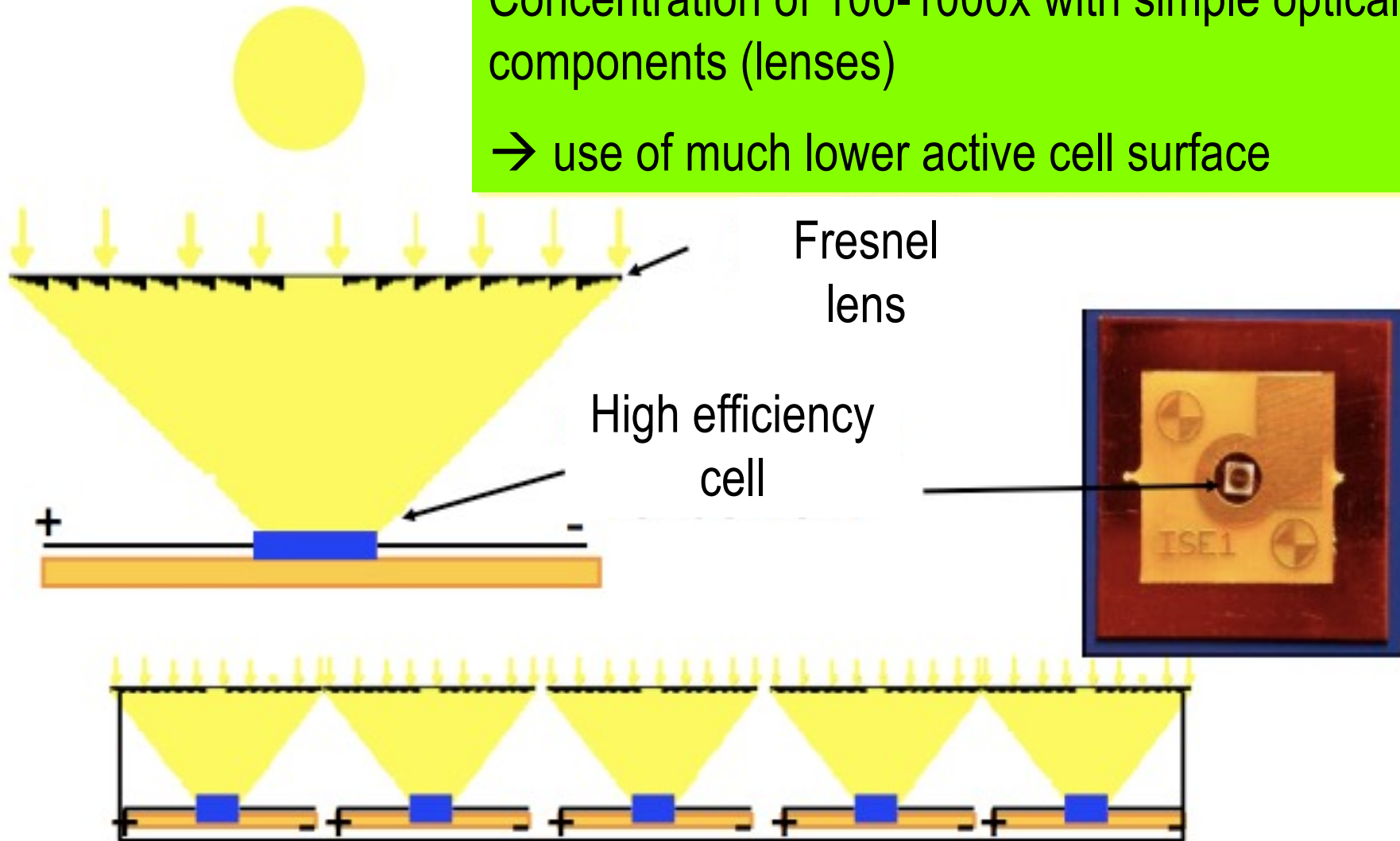
Concentrated PV

- small cells of high efficiency
- only direct solar irradiation is used (30-50 “suns” by focalisation)
- MPP (track the sun trajectory)
- point cell (Stanford, USA) : 26.5% @ 300 suns (1-4 \$/cm²)
- GaAs (OCV 1 V) : 28% @ 1000 suns
- tandem cells GaAs/GaSb : 33% (Boeing)
- triple junction: 44% efficiency
- secure and inexpensive to develop, high potential for low cost PV

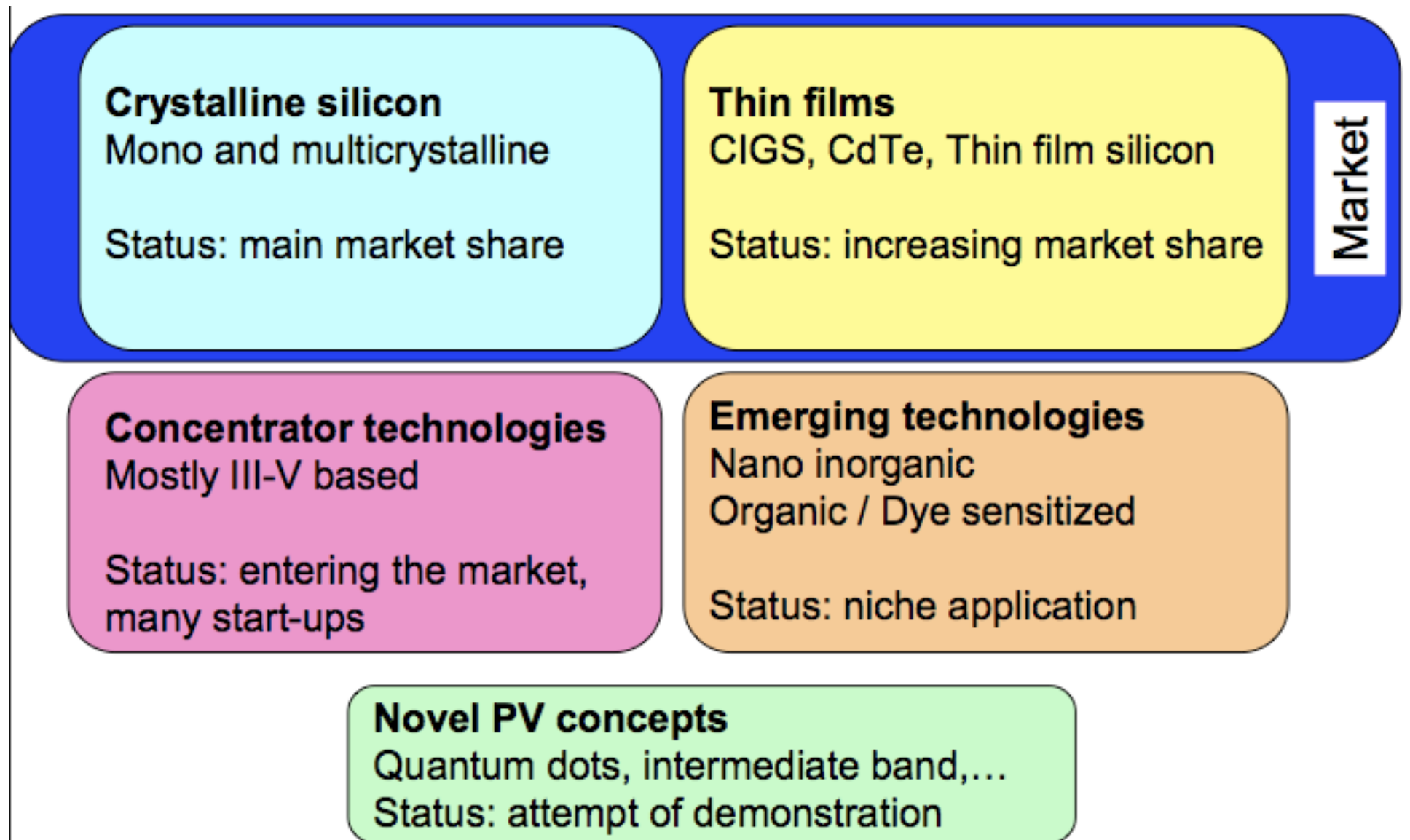
Concentrator systems

Concentration of 100-1000x with simple optical components (lenses)

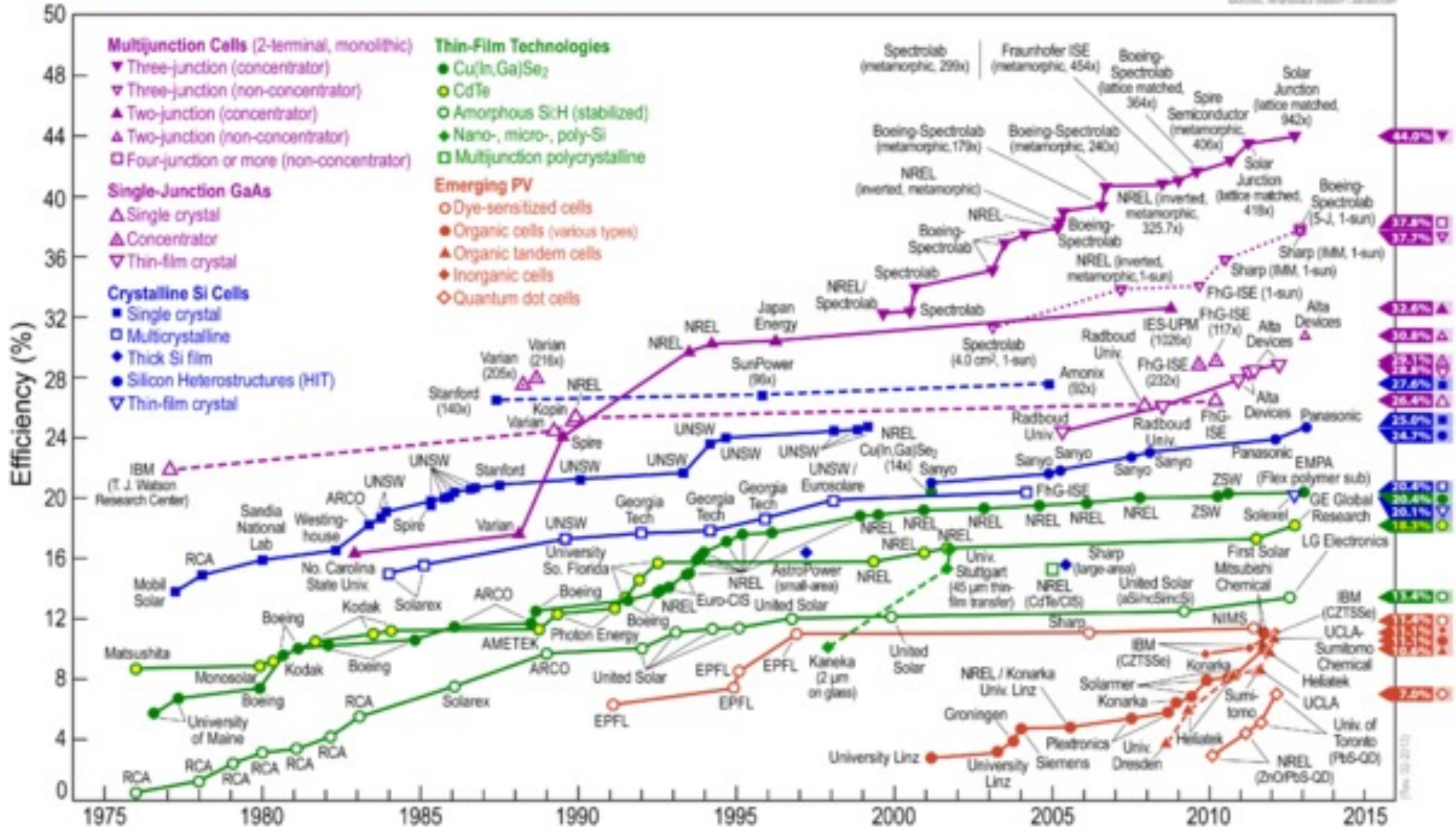
→ use of much lower active cell surface



PV technology overview

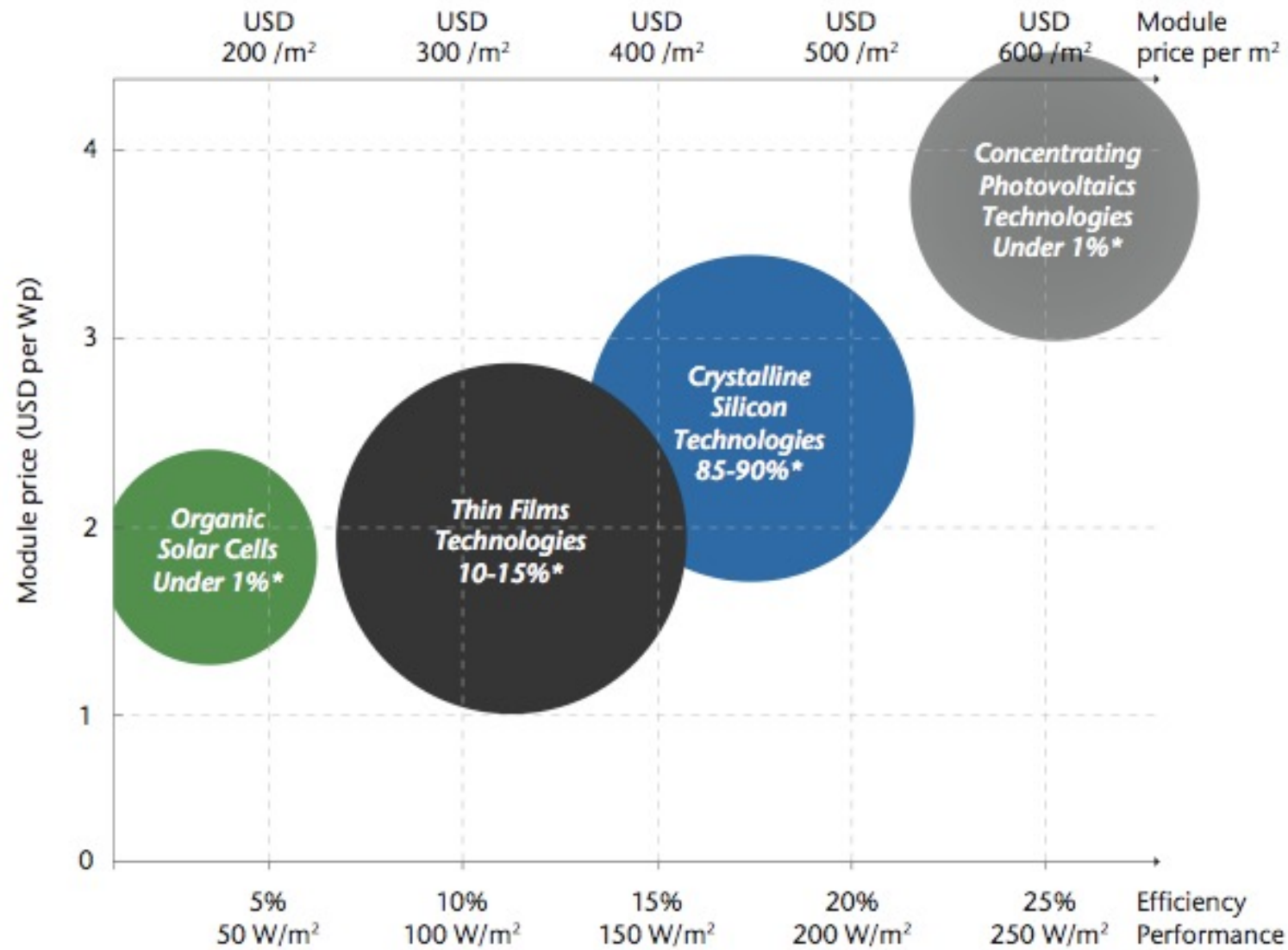


Best Research-Cell Efficiencies



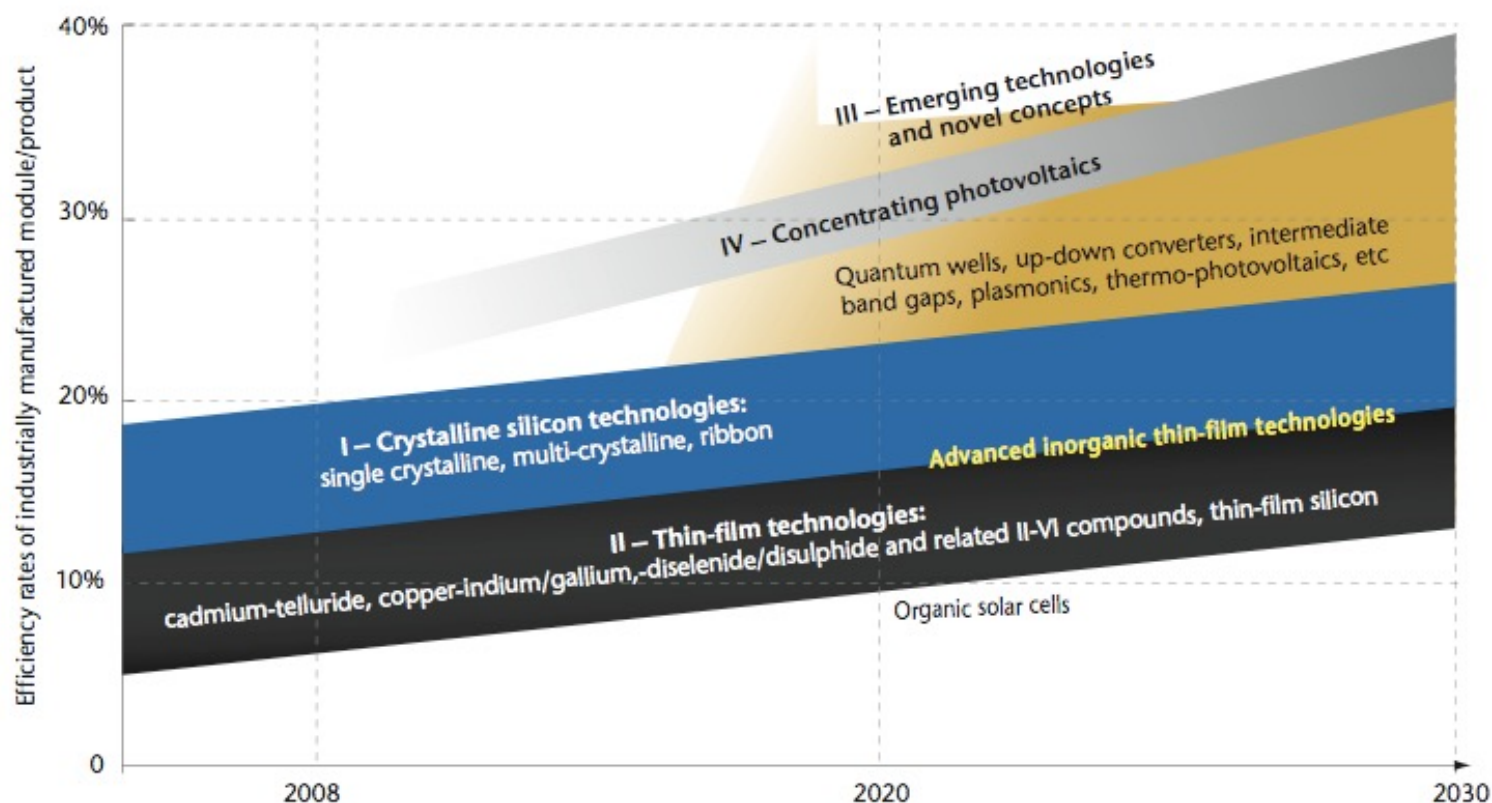
Current performance and price of different PV module technologies*

IEA PV Roadmap



* percentage share of 2008 market

Figure 11: Photovoltaic technology status and prospects



Source: IEA PVPS.

KEY POINT: Current technologies will co-exist with emerging technologies and novel concepts.

Table 1: Current efficiencies of different PV technology commercial modules

Wafer-based c-Si		Thin films		
sc-Si	mc-Si	a-Si; a-Si/ μ c-Si	CdTe	CIS/CIGS
14-20%	13-15%	6-9%	9-11%	10-12%

Each technology has pro and contra

	positive	Challenges
Crystalline Si	Proven, high efficiency	Reduced Si usage Cost decrease
Thin film Si	Lowest cost / m ² Unlimited supply	Medium efficiency High capex
CdTe	« simple process » Medium high-efficiency	Cd acceptance Te availability
CIGS	Best thin film efficiency	Difficult process In availability
Concentrator	Quick implementation of Ultra-high efficiency	Tracking, system costs

Technologies

- Efficiencies of various technologies:

- Crystalline (Si: mono and poly):

- Efficiency: 14-21%
 - Potential: 20-25%

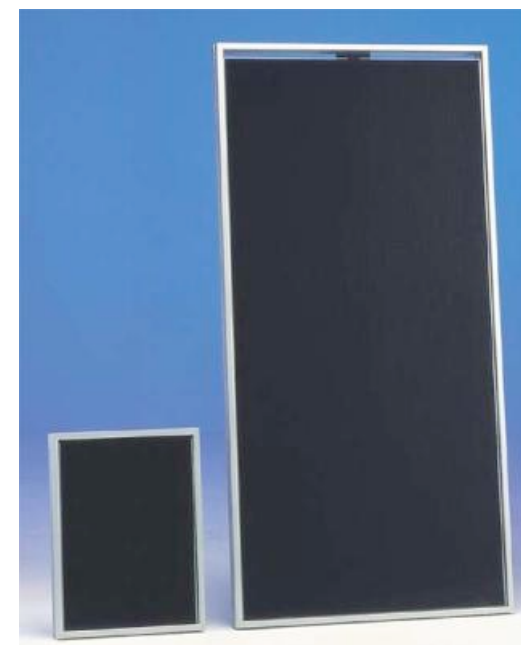
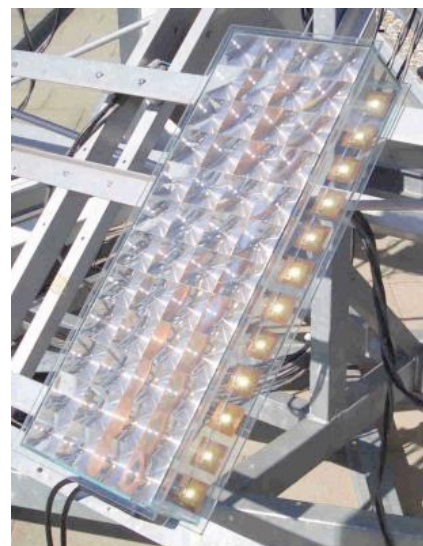


- Thin film (CdTe, CIGS a-Si / $\mu\text{c-Si}$):

- Efficiency: 14-16%
 - Potential: 16-20%

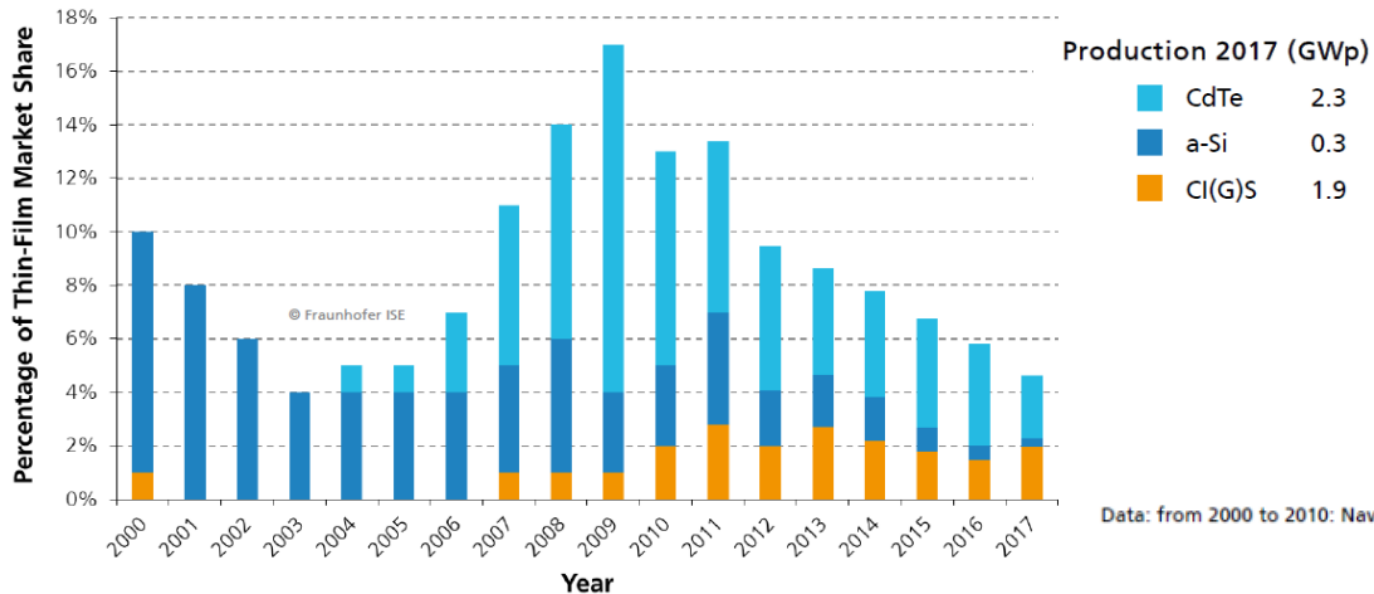
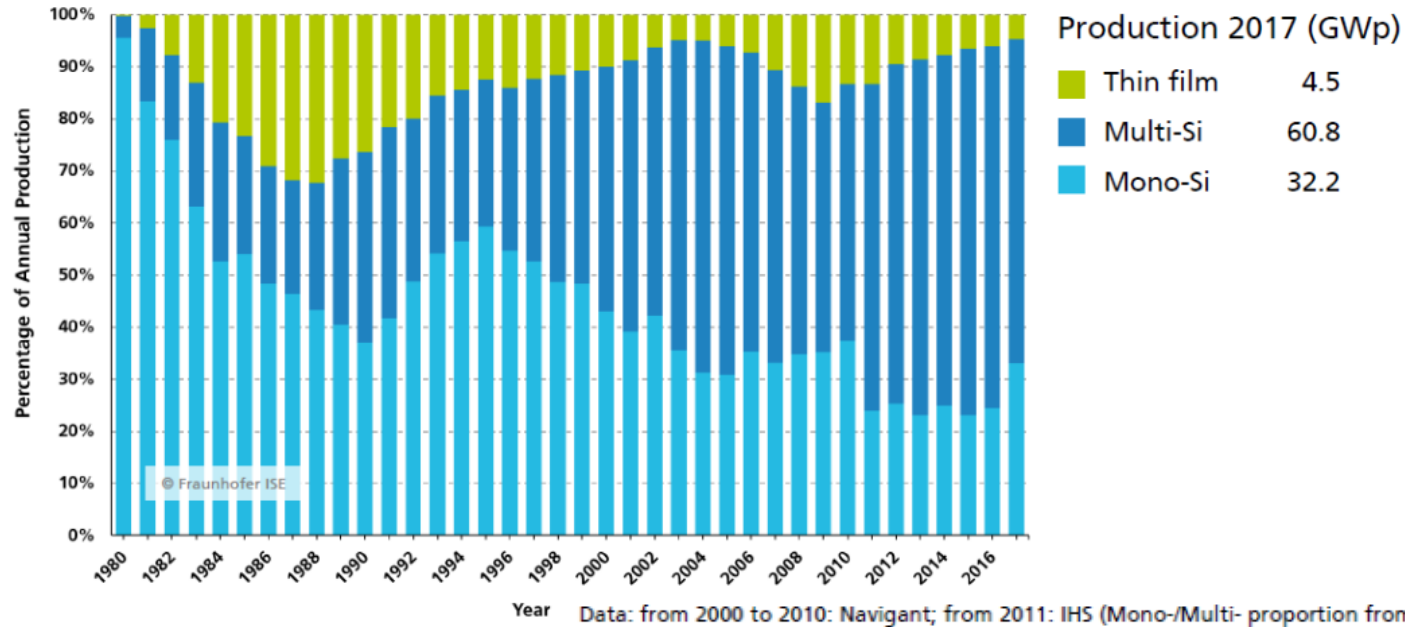
- Concentrated (III-V-based):

- Efficiency: 25-30%
 - Potential: 30-50%



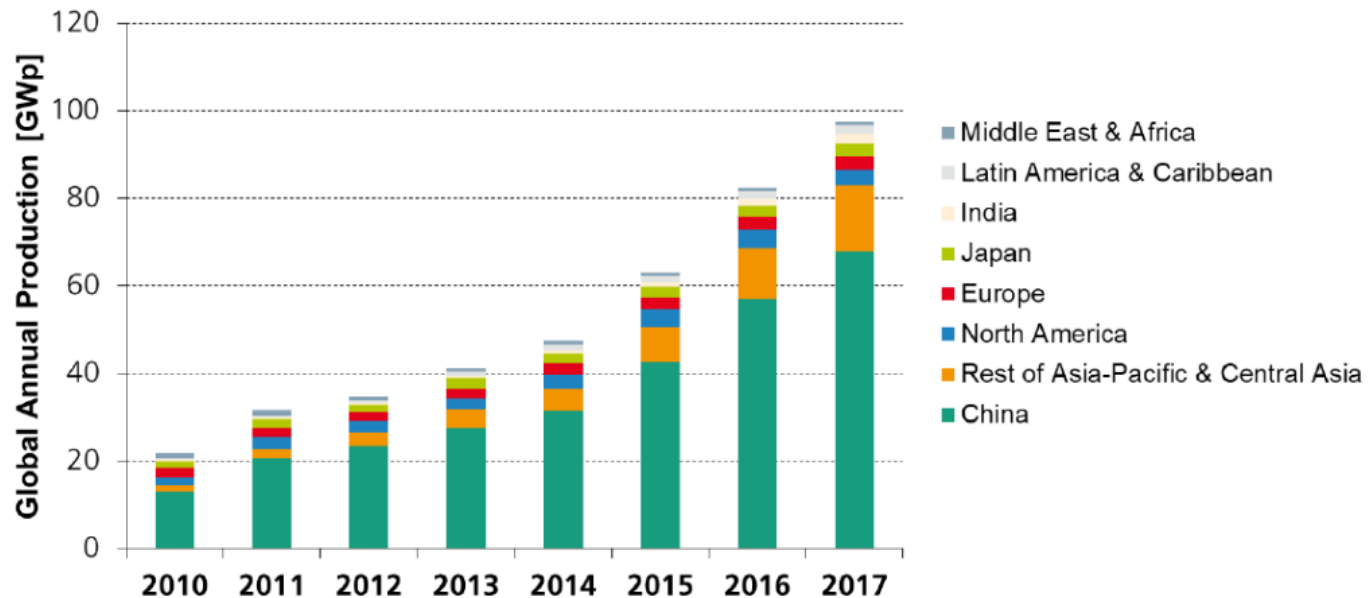
Technologies

- Market shares:



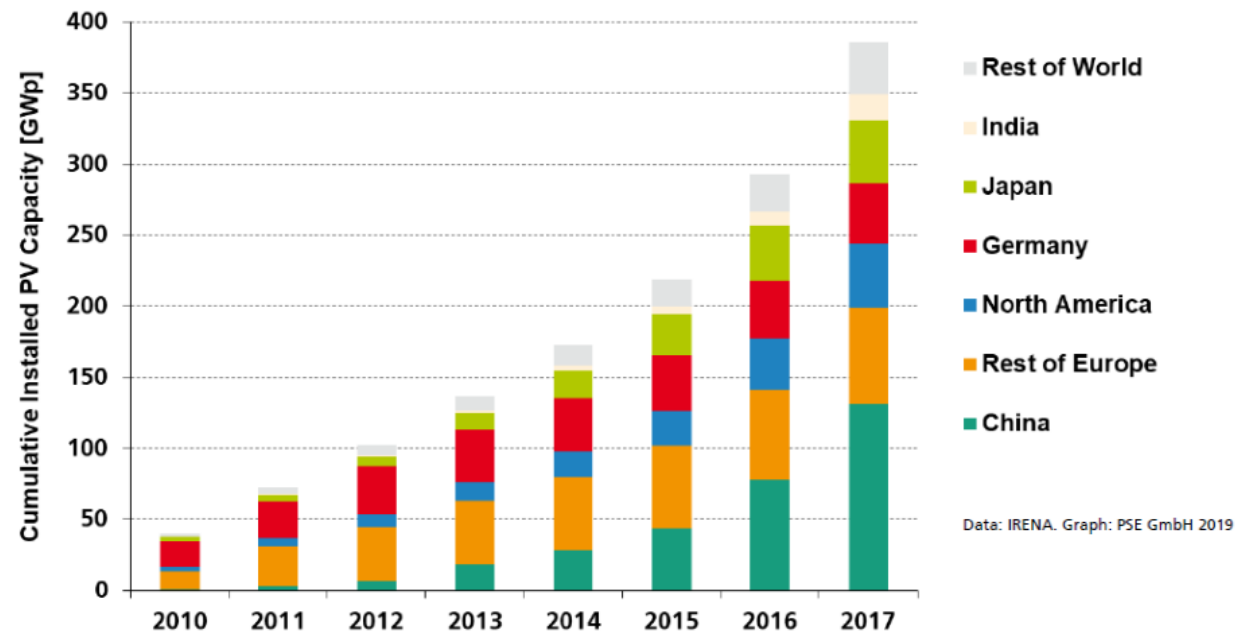
Production and Installation

- Production



Data: Up to 2009: Navigant Consulting; since 2010: IHS. Numbers for 2018 estimated Graph: PSE GmbH 2019

- Installation



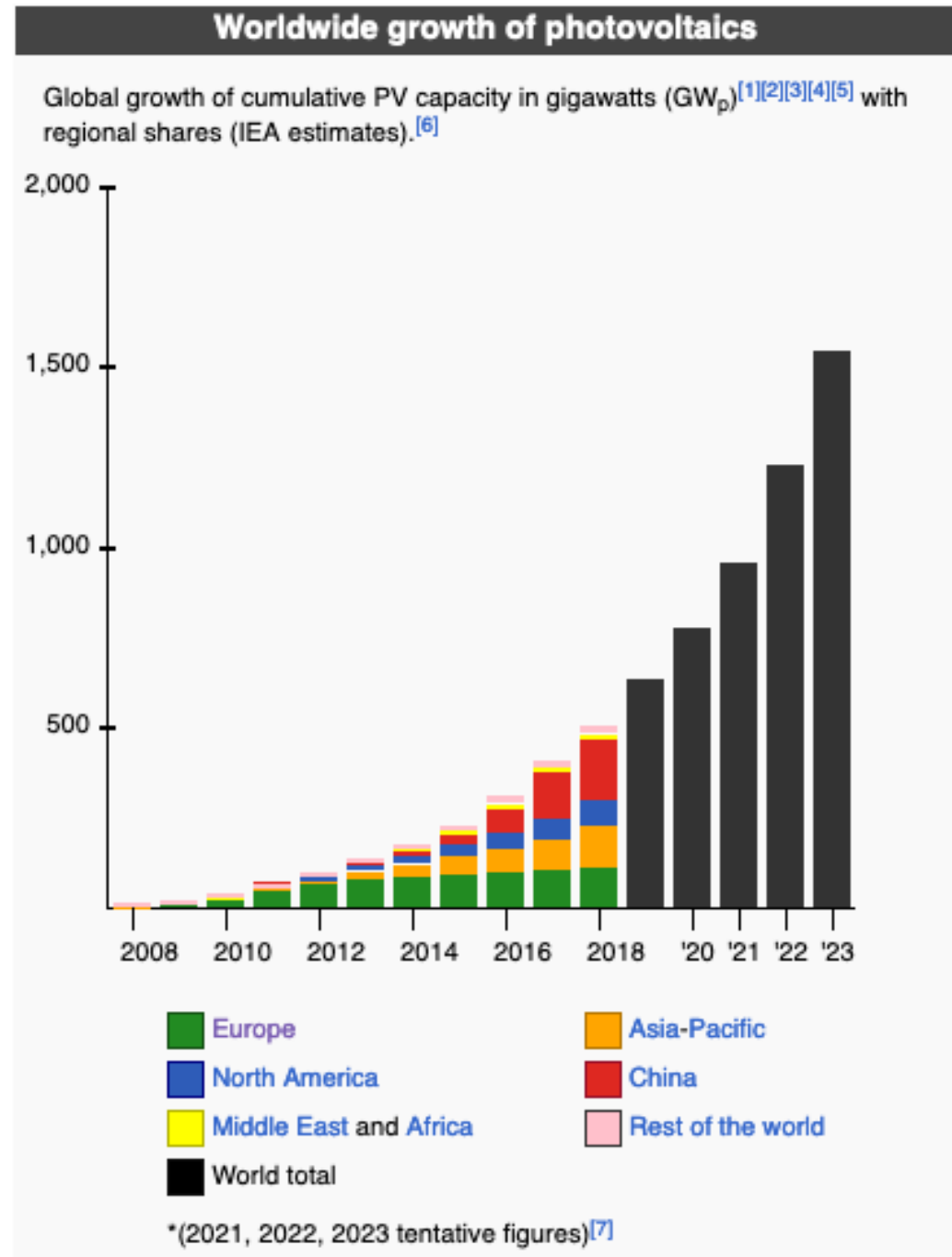
Data: IRENA. Graph: PSE GmbH 2019

World PV growth

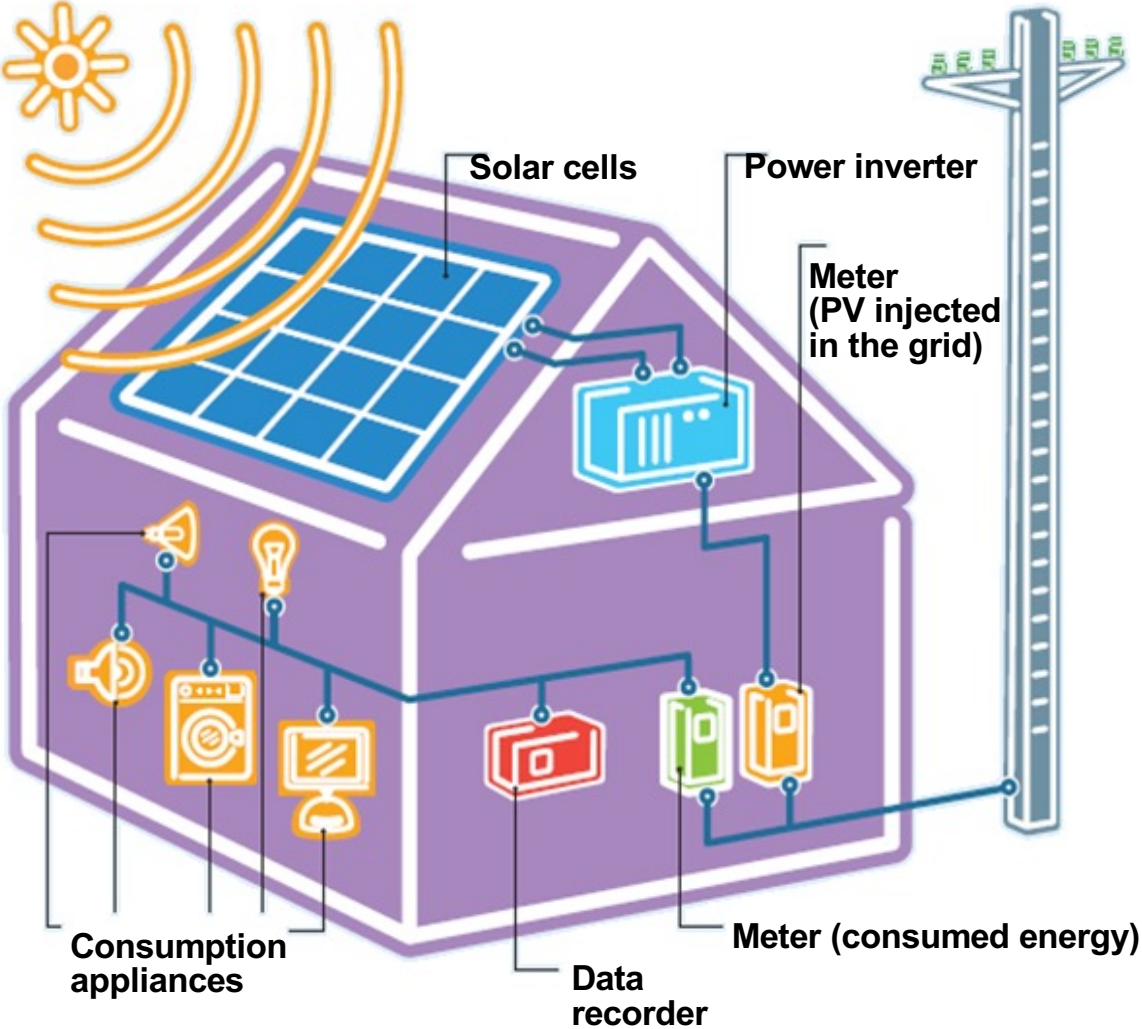
Recent and estimated capacity (GW _p)								
Year-end	2016 ^[8]	2017 ^[9]	2018 ^[7]	2019 ^[7]	2020 ^[7]	2021E ^[7]	2022E ^[10]	2023F ^[10]
Cumulative	306.5	403.3	512	630	774	957	1225	1541
Annual new	76.8	99	109 ^[11]	118	144 ^[7]	183 ^[7]	268 ^[10]	316 ^[10]
Cumulative growth	32%	32%	27%	23%	23%	24%	28%	26%

China : 393 GW
 EU : 200 GW
 USA : 113 GW
 Japan : 79 GW
 Germany : 67 GW
 India : 63 GW
 AUS : 28 GW
 ...

https://en.wikipedia.org/wiki/Growth_of_photovoltaics



Residential application

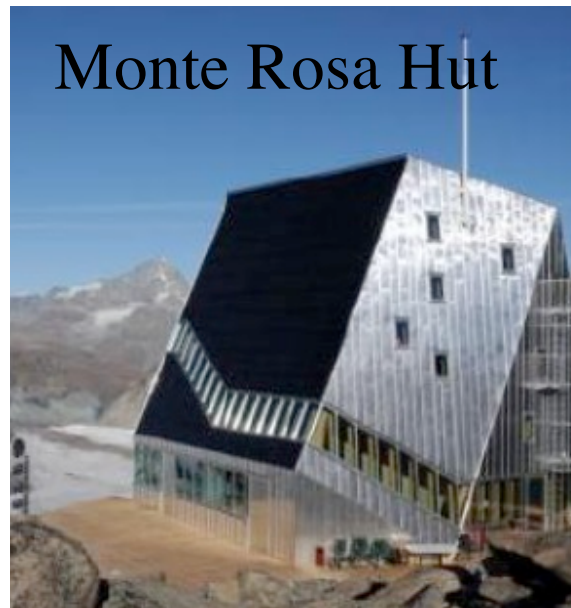


PV building integration



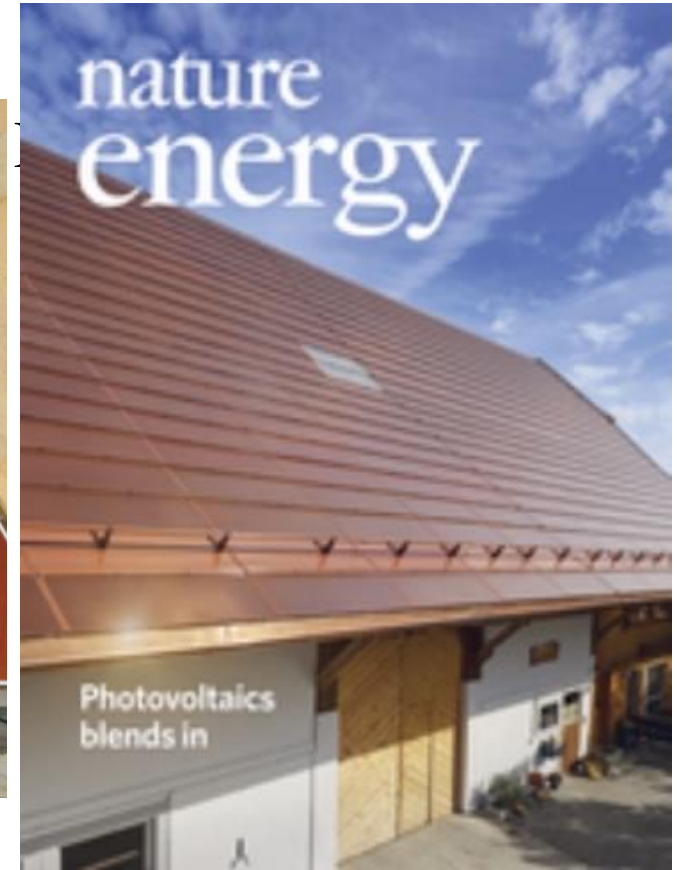
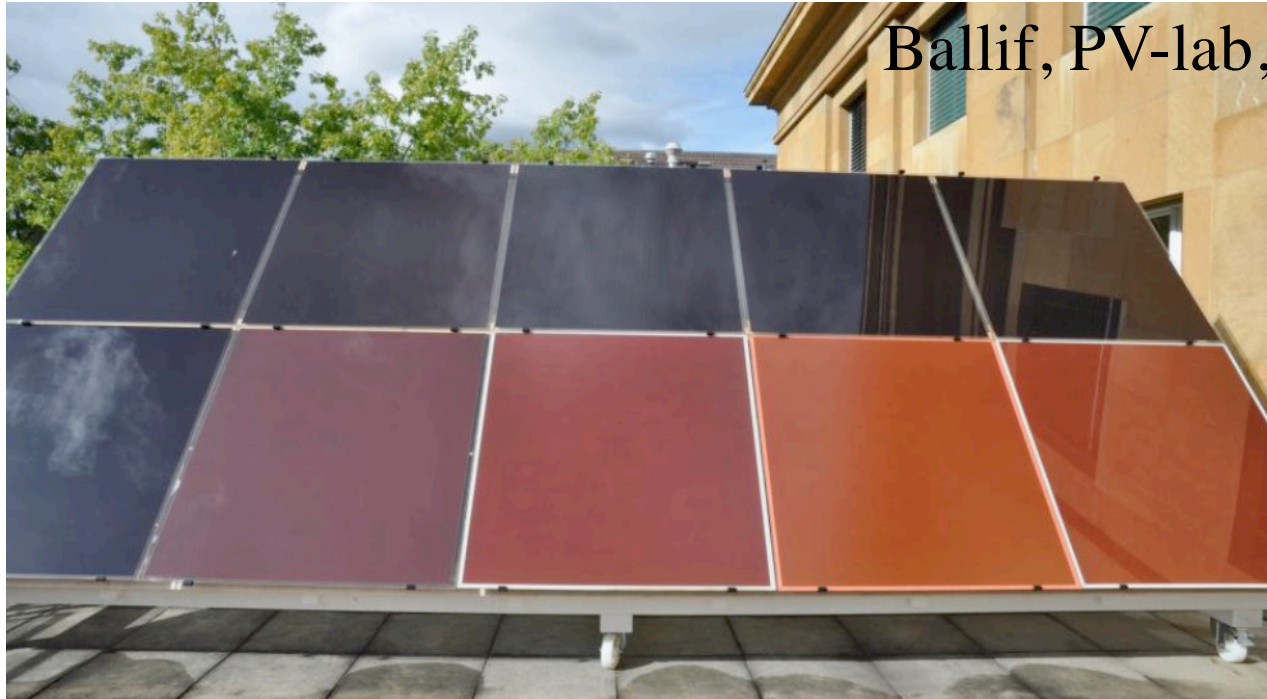
Aesthetics

- Photovoltaics: early modules
- Fully integrated today:



Aesthetics

- Photovoltaics: various colors



- Covered by prints



PV power plant



“Mont-Soleil” (in operation since 1992)

Biggest PV installation in Switzerland till 2005

4500 m² Si cells

720'000 kWh/yr

rated power: 500 kW

around 200 households

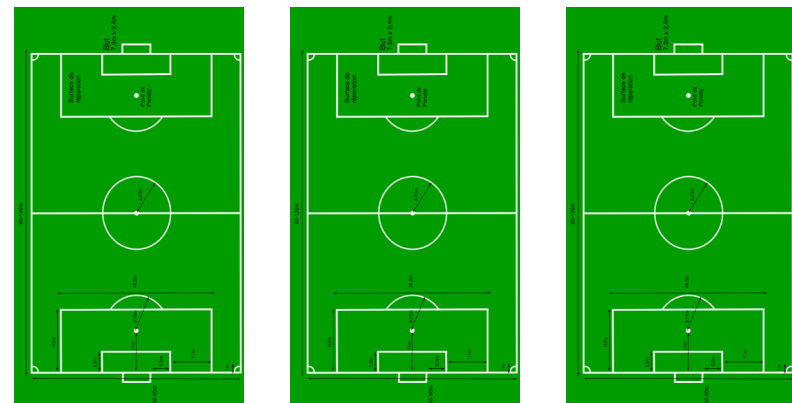
Cell efficiency: 12-17 %

Efficiency of the inverter: 96 %

Global efficiency: ~ 11.5 %

**real
land use
* 5**

Total occupied surface: 20'000 m²



Equivalent to ~ 3 soccer grounds

'Swiss stadium' Power Plant

7'000 panels (12'000 m²) of polycrystalline Si (efficiency : 15%)

1'200'000 kWh / yr (rated power: 1'300 kW)

around 400 households



Romande Energie – EPFL Solar Power Plant

(in operation since August 2010)

2 MWe
15 MCHF



In 2012 biggest PV installation in Switzerland, with 20'000 m² of PV and annual production of 2 GWh (~ 3% of EPFL consumption)

Solar shuttle boat

"Aquarel"



First regular shuttle service of electro-solar tourist boat in Europe; the autonomy of the boat is ensured by batteries that can receive or deliver electricity from/to the grid

Solar ship



World ' s largest solar-powered catamaran

102 feet long, 50 feet wide multi-hull vessel

500 m² black PV panels, containing 38 ' 000 SunPower next generation cells

top speed 27 km/h, seating capacity 50 passengers

Cost: 18 million €

Solar flight?

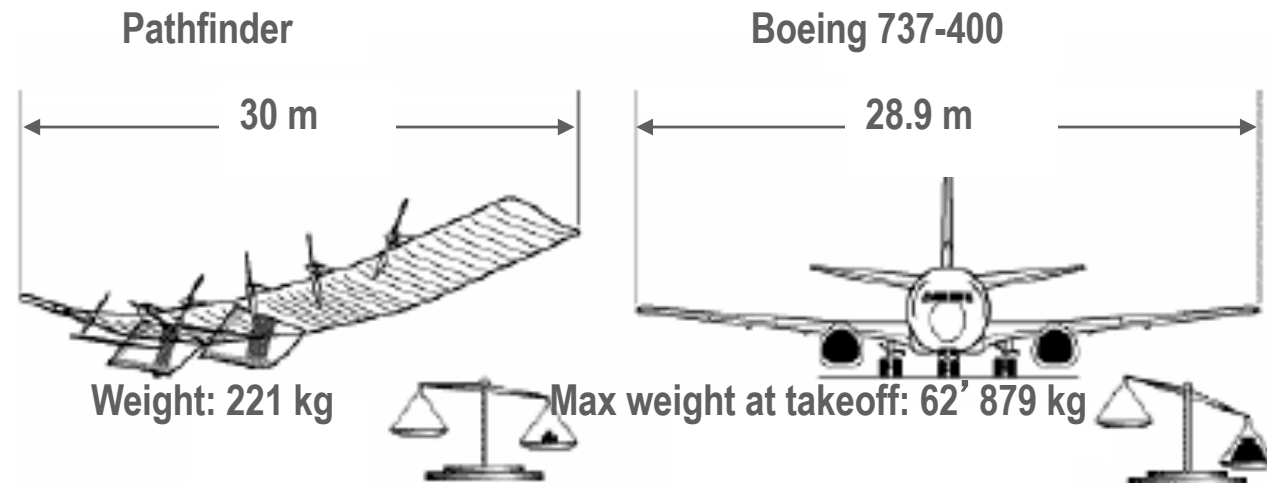
“Pathfinder”



Solar-powered,
remotely piloted
aircraft (USA, 1988)

7'200 W
6 electric engines
(2 h autonomy on
battery)

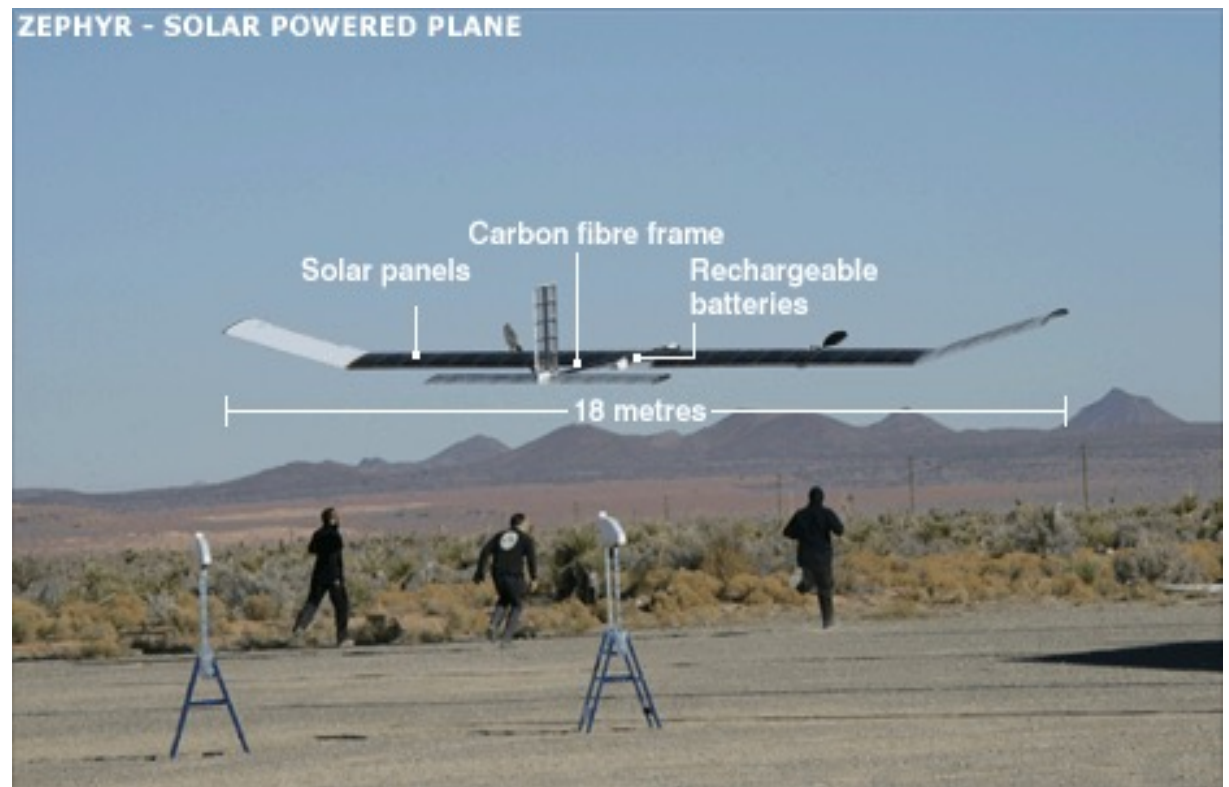
Successful record flight - 80'000 feet, in 1998 - a significant milestone on the way to commercial solar-powered aircraft acting as low-cost complements to satellites (operational flying altitude: more than 20 km)



“Zephyr-6” Solar-Powered Plane, the “eternal flight” plane

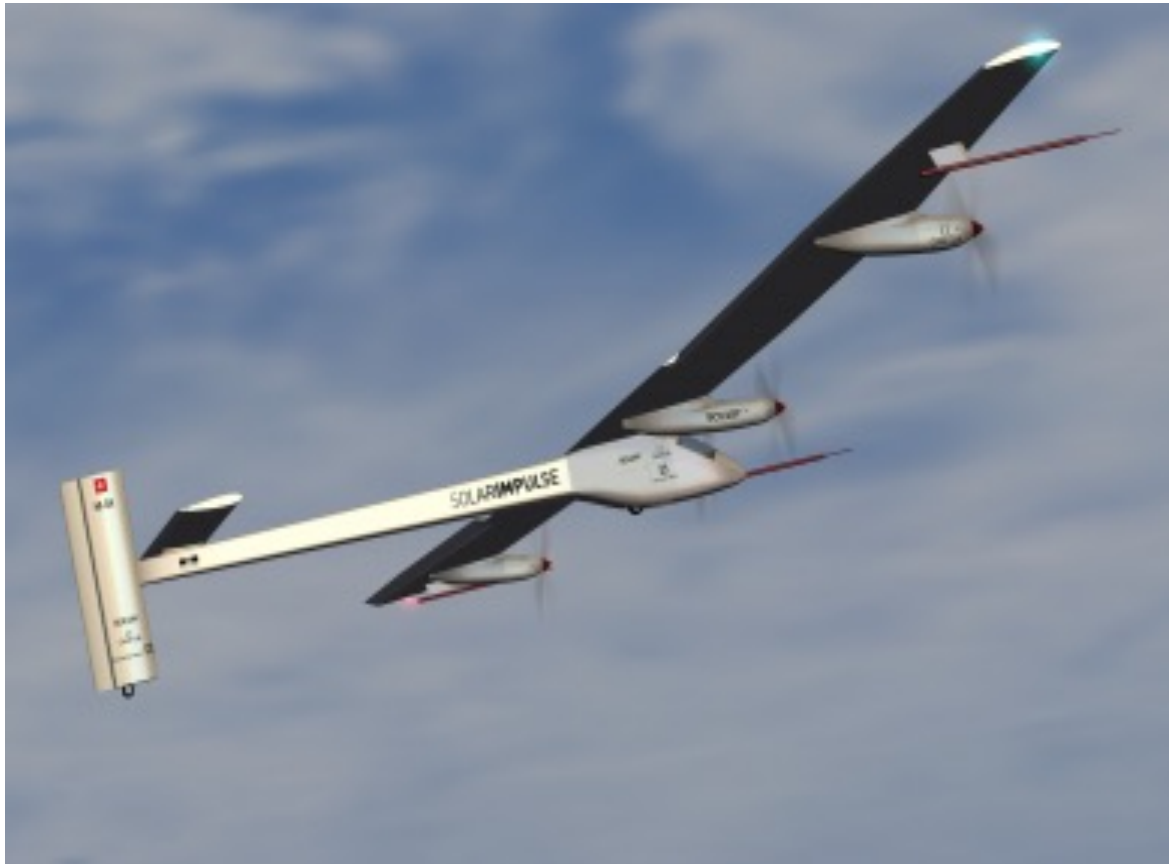
UK-built solar-powered plane that has set an unofficial world endurance record for a flight by an unmanned aircraft (14 days and 24 minutes, mid-July 2010)

Extremely thin and light solar panels cover its wings; Zephyr has a lot of surface for solar panels and a lot of lift relative to its 50 kg weight (thanks to a carbon-fiber body)



“Solar Impulse”

Proposed by Bertrand Piccard, this aircraft should achieve the first round-the-world manned solar airplane flight



With 200 m² of PV and 12 % total efficiency of the propulsion chain, the plane 's motors achieve just 8 horsepower or 6 kW

= the amount of power of the Wright brothers plane in 1903

Solar Impulse's wings (nearly the wingspan of an Airbus 340) are multifunctional:

they carry load, produce energy, and house an electrical network; they are to be ultra-strong, efficient and light structures



PV installed in Switzerland

M ²	Type	Production	Remark
30 mio m ² estimate (assumption: 100 W _p / m ²)	Silicon modules	2.6 TWhe (9.36 PJ) 2.97 GW installed peak power	
Potential	138 mio m ² on roofs 52 mio m ² on façades island installations	7 TWh (50% roof use) 2.6 TWh (cosφ factor) several TWh	calculated assuming 200 kWh/m ² .yr (20% efficiency)

>15% of electricity

Other estimates go from 30 TWhe to 60 TWhe / yr for Swiss PV potential

Compared to solar thermal installations (CH)

m ²	Type	Thermal prod. in PJ	Remark
1'544'500	glazed collectors on house roofs	2.5	space + hot water heating
175' 000	unglazed collectors not always on roofs	0.2	private/public pool heating
876' 000	agricultural collectors on roofs	0.4	for hay drying
Total : 2.6 mio		1.63	
Potential:	138 mio m ² roofs	100 PJ if 50% roof space used	Assumption : 30% eff. 400 kWh/m ² .yr

= 30% of space + HW heat

PV in Europe

- 2022: 209 GWe installed; 203 TWhe produced
 - 80% crystalline Si
 - 19% thin film cells (a-Si, CdTe, CuInSe, GaSe₂, tandem cells)
 - 1% concentration cells and organic cells
- combined with storage, hybridisation; smart grids

Target	2007	2020	2030	2050
GWp	5	150	397	962
TWh	5.4	180	556	1347

→ 1100-1400 h / yr load factor at peak

Potential of PV electricity generation

With 10% efficiency PV panels



*Ch. Baillif
PV Lab
EPFL NE*

■ Total US electricity

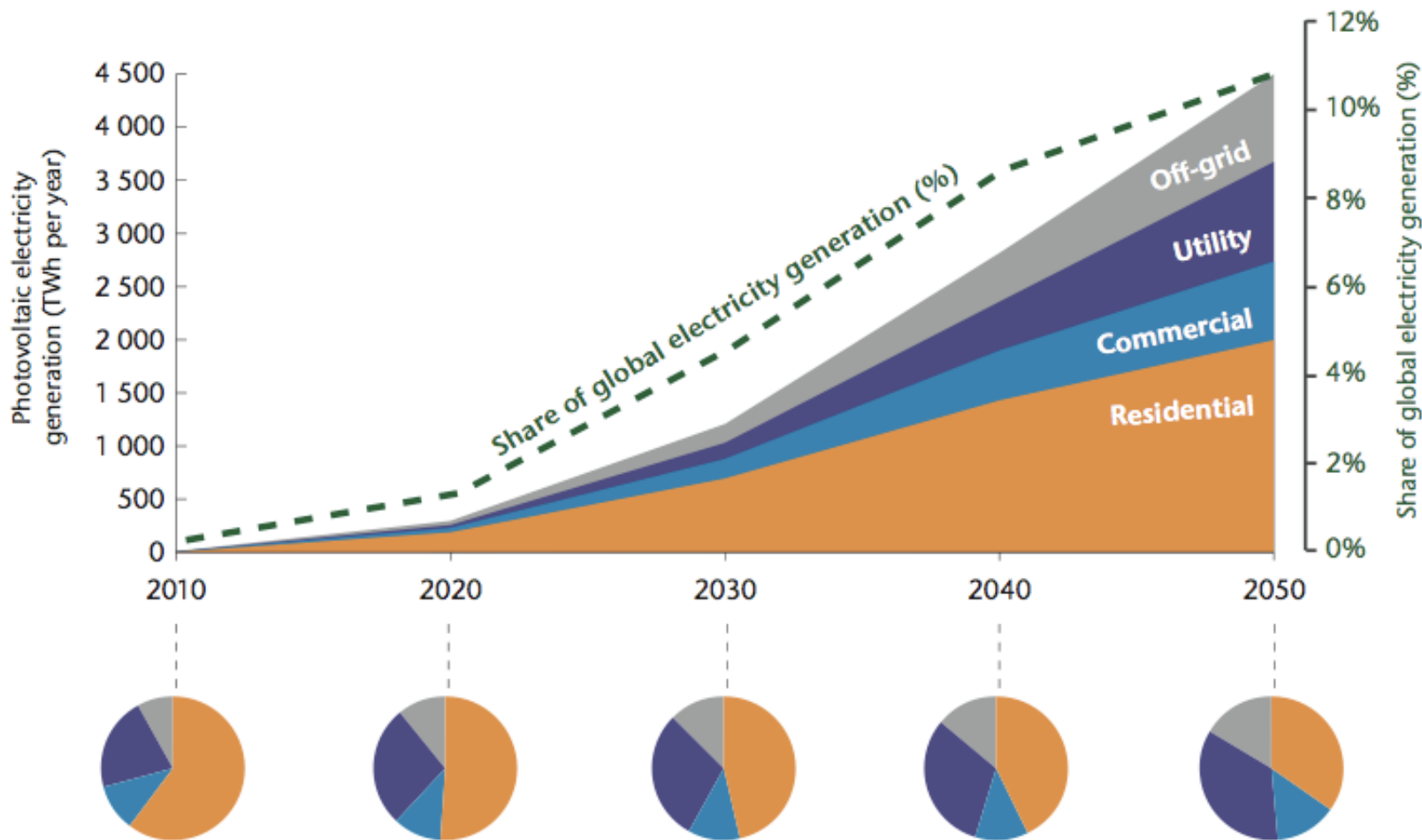
□ Total US energy

Market end-use sectors:

- **Residential** (typically <20 kW on individual homes)
- **Commercial** (typically <1 MW for commercial office buildings, schools, hospitals, and retail)
- **Utility** scale (starting >1 MW, mounted on buildings or directly on the ground)
- **Off-grid** applications (varying sizes)

These different applications have different system costs and compete at different price levels.

Evolution of photovoltaic electricity generation by end-use sector



Summary

- Solar PV power is a commercially available and reliable technology with a **significant potential** for long-term growth in nearly all world regions.
- It is estimated that by **2050**, PV will provide ≈11% of global electricity production (by 2030: 5%) and avoid 2.3 Gt/yr of CO₂ emissions (3 TW installed).
- PV will achieve competitive parity with the power grid by 2020 in many regions.