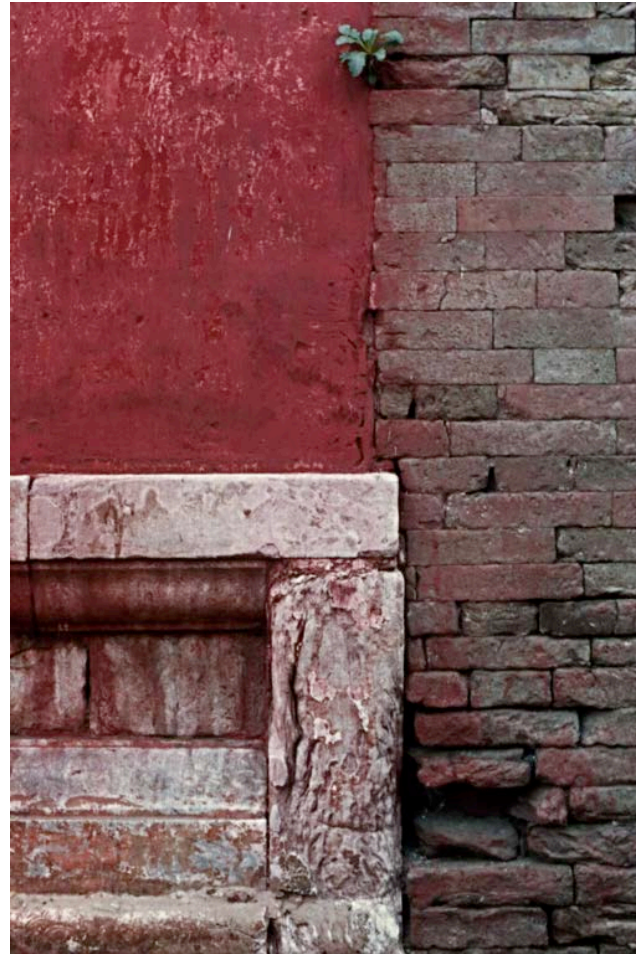


Texture

- What is texture?
- Texture analysis
- Deep Texture



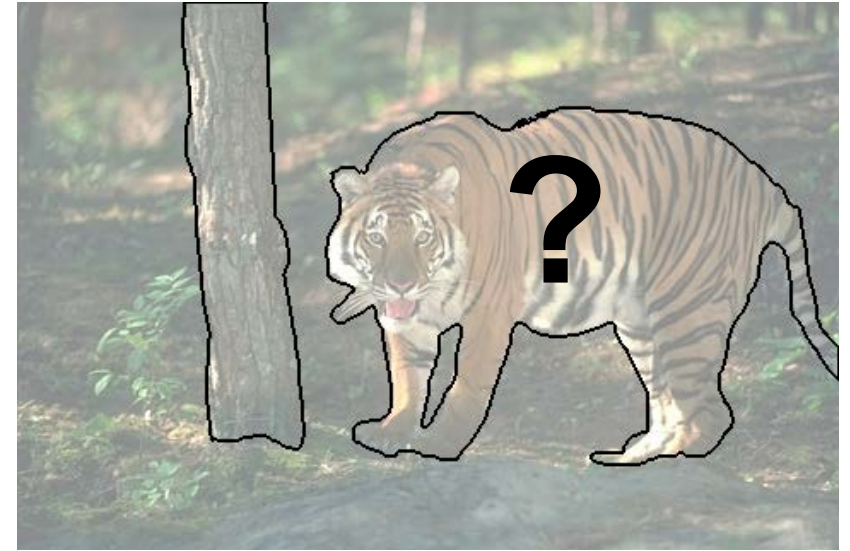
Reminder: Homogeneous or Not?



What is homogeneous in some parts of these images are the statistical properties, not the actual pixel values.



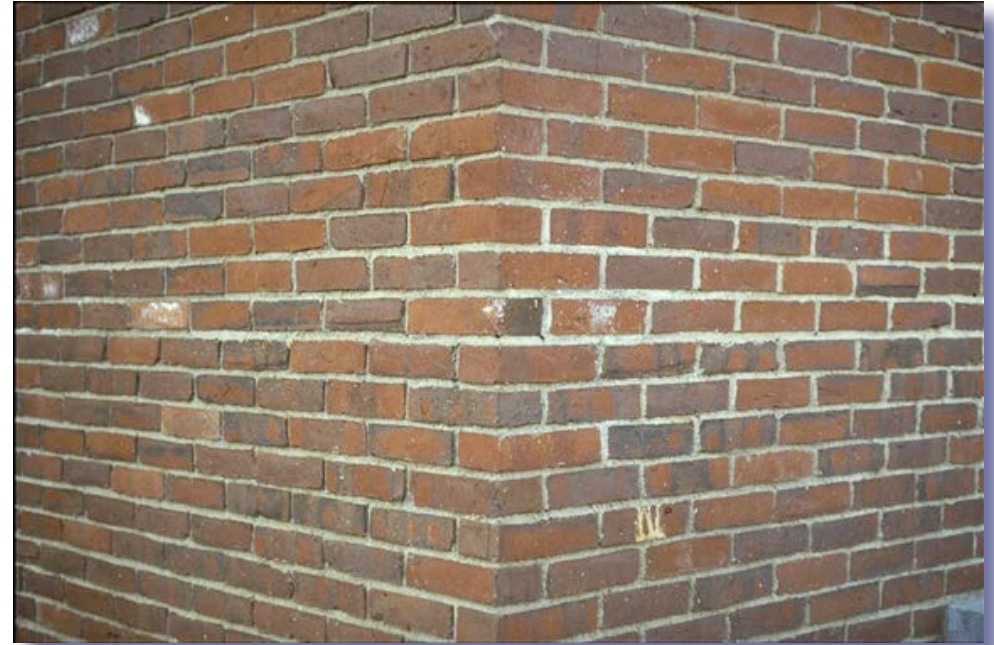
Texture-Based Segmentation



Ideally, we would like to:

- Assign to individual pixels whose texture is similar the same values to form a textural image.
- Evaluate homogeneity both in the original image and in the textural one.

Texture-Based Edges



Similarly, we would like to be able to find boundaries between textures.

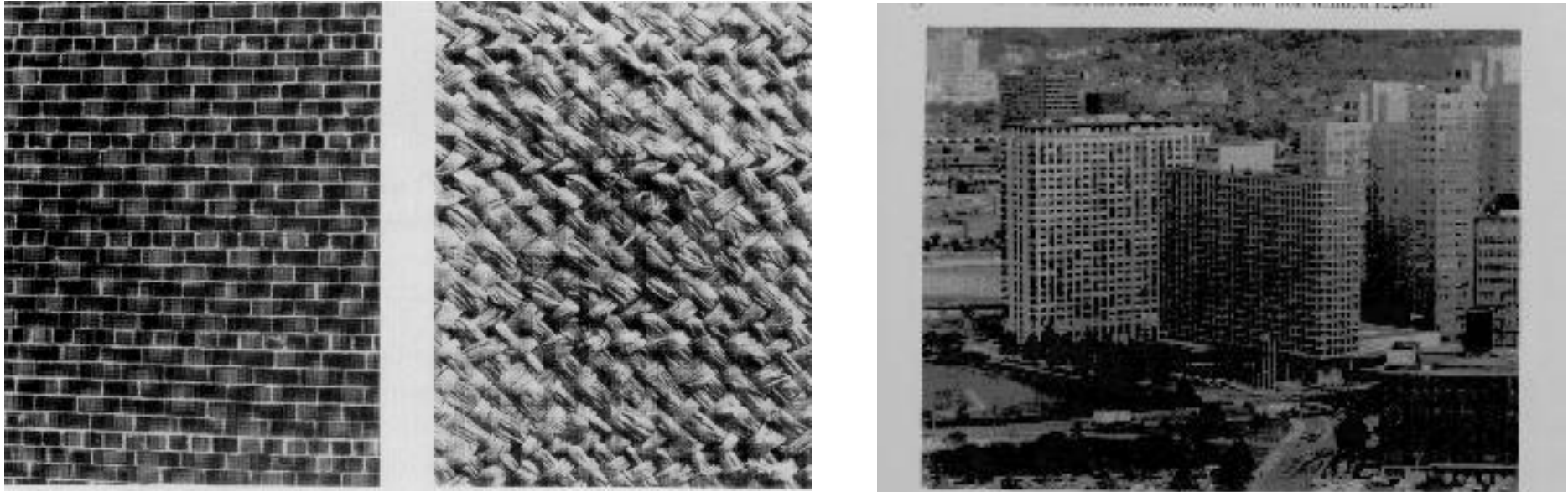
What is Texture?



Repetition of a basic pattern:

- Structural
 - Statistical
- Non local property, subject to distortions.

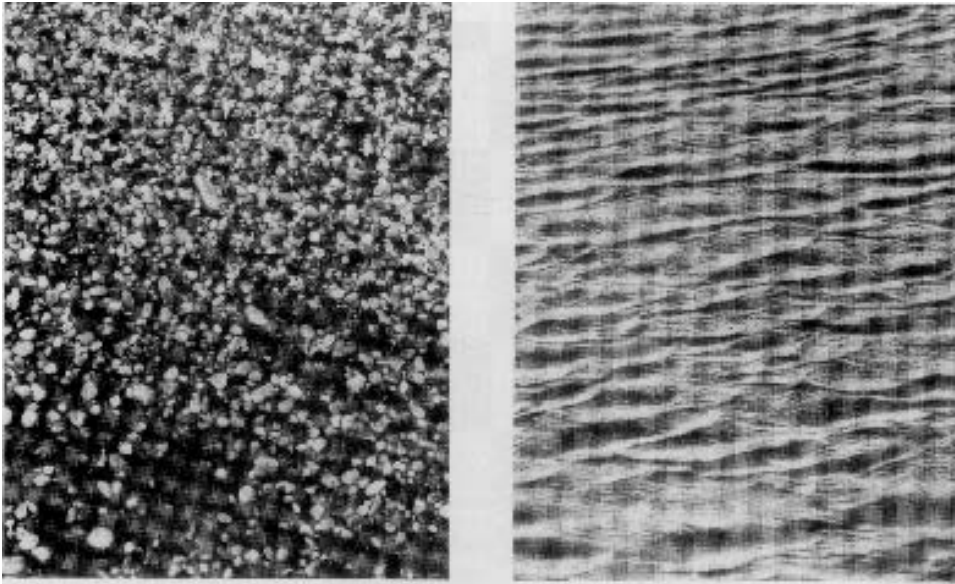
Structural Textures



Repetitive Texture Elements (Texels)

A texel represents the smallest graphical element in a two-dimensional texture that creates the impression of a textured surface.

Statistical Textures



Homogeneous Statistical Properties

Textured vs Smooth

A “featureless” surface can be regarded as the most elementary spatial texture:

- Microstructures define reflectance properties.
- They may be uniform or smoothly varying.

→ Texture is a scale dependent phenomenon

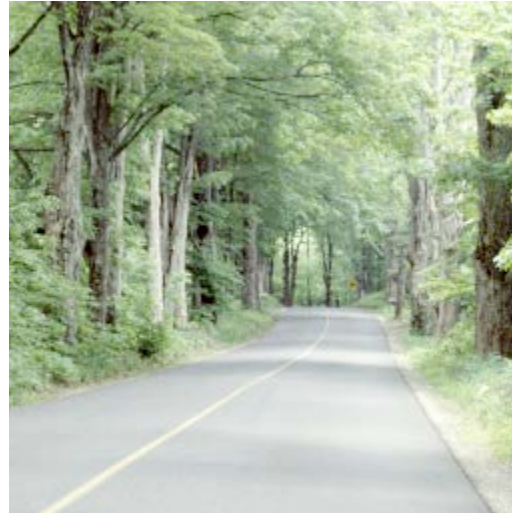
Scale Dependence



At these two different scales, the texture seems very different.

Structural vs Statistical

- Segmenting out texels is difficult or impossible in most real images.

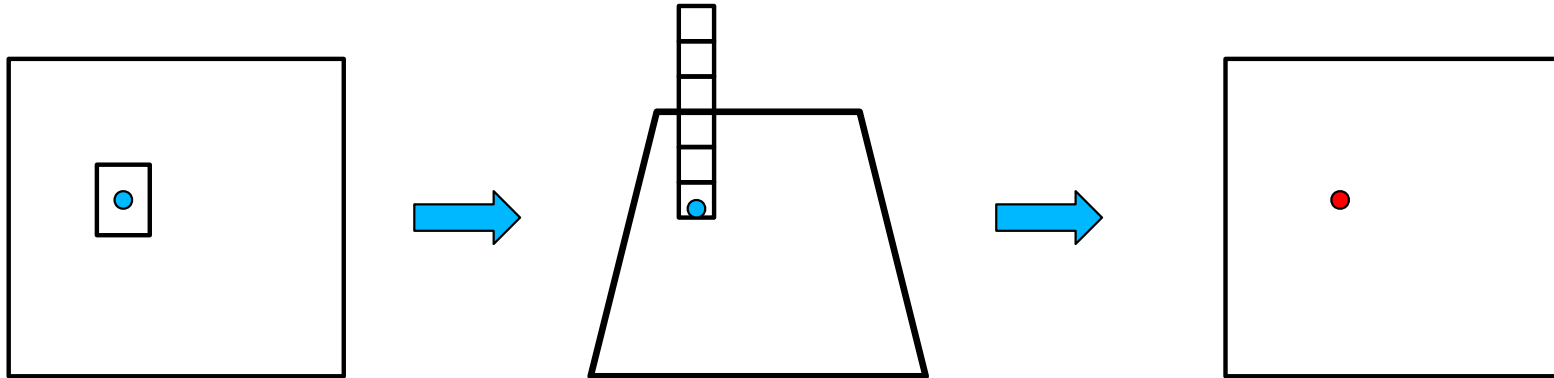


What are the fundamental texture primitives in this image?

- Numeric quantities or statistics that describe a texture can be computed from the gray levels or colors alone.
- The statistical approach is less intuitive, but more effective in practice.

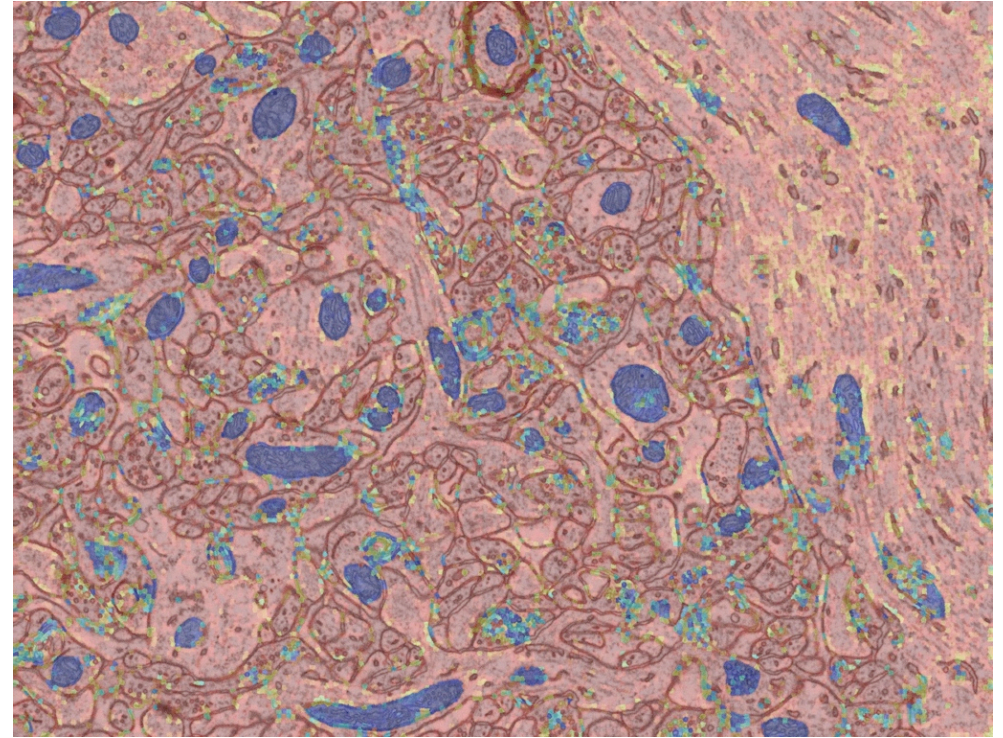
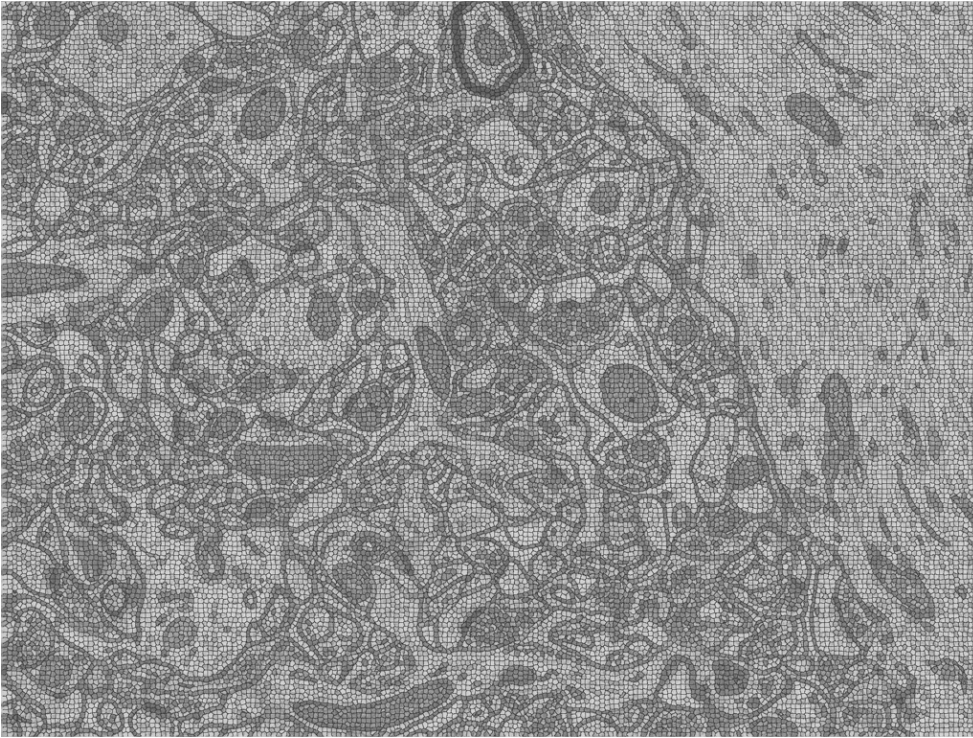
Creating Textural Images

Because texture is non-local, the texture of individual pixels must be estimated using neighborhoods that surround them:



- For each pixel, compute a feature vector using either an image patch or a set of filters.
- Run a classification algorithm to assign a texture value to each pixel.

Reminder: Mitochondria



- Compute image statistics for each superpixel.
 - Train a classifier to assign a probability to be within a mitochondria.
- > We used the super pixels to compute local statistics.

Textural Metrics

Spectral metrics:

- Texture is characterized by the properties of its Fourier transform.

Statistical Metrics:

- Texture is as statistical property of the pixels' intensity and color in a region.

Deep Net Metrics:

- They have now mostly superseded the others.
- They encompass the earlier concepts.

Reminder: Discrete Fourier Transform

$$F(\mu, \nu) = \frac{1}{\sqrt{M * N}} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x, y) e^{-2i\pi(\mu x/M + \nu y/N)}$$

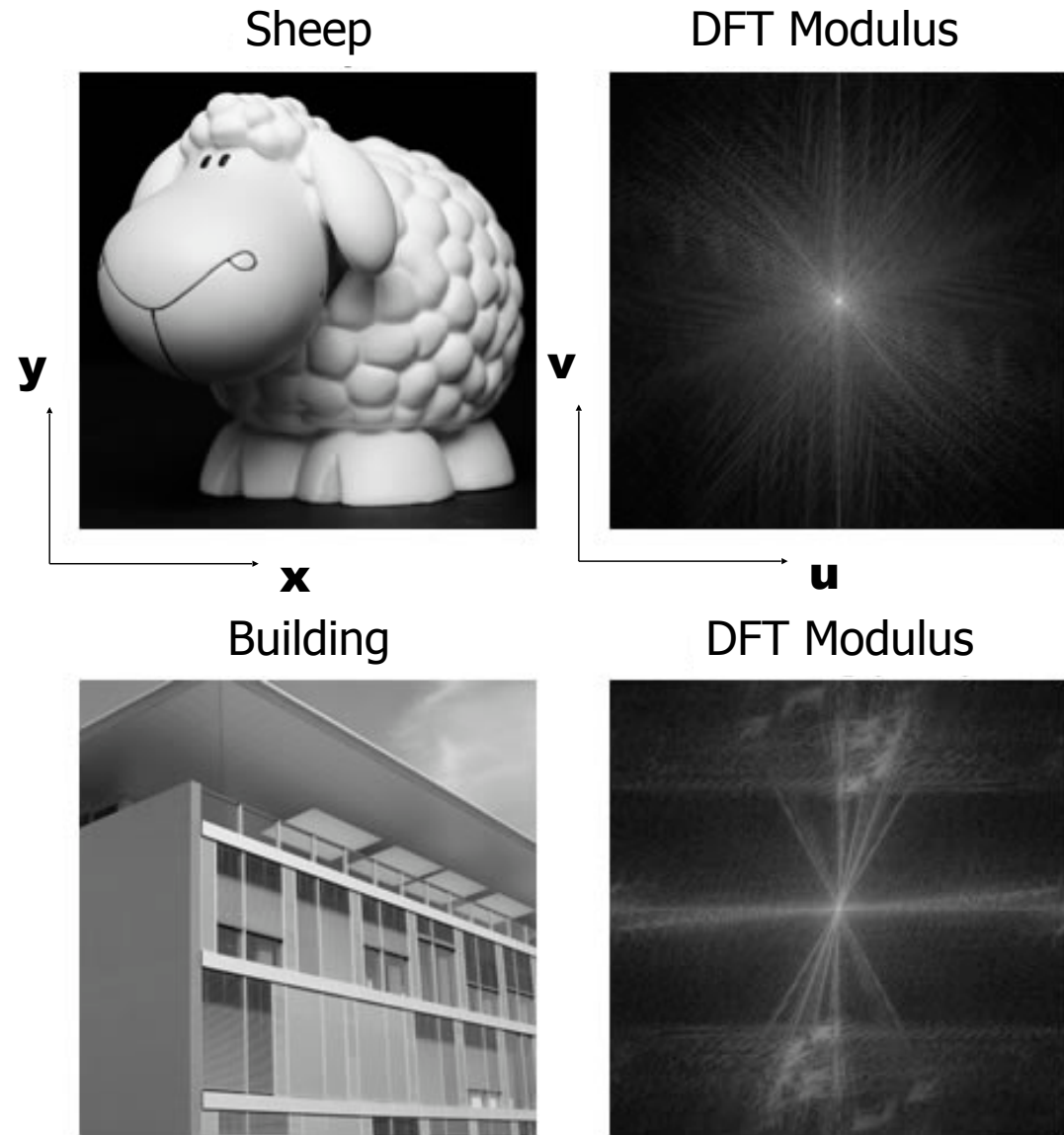
$$f(x, y) = \frac{1}{\sqrt{M * N}} \sum_{\mu=0}^{M-1} \sum_{\nu=0}^{N-1} F(\mu, \nu) e^{+2i\pi(\mu x/M + \nu y/N)}$$

The DFT is the discrete equivalent of the 2D Fourier transform:

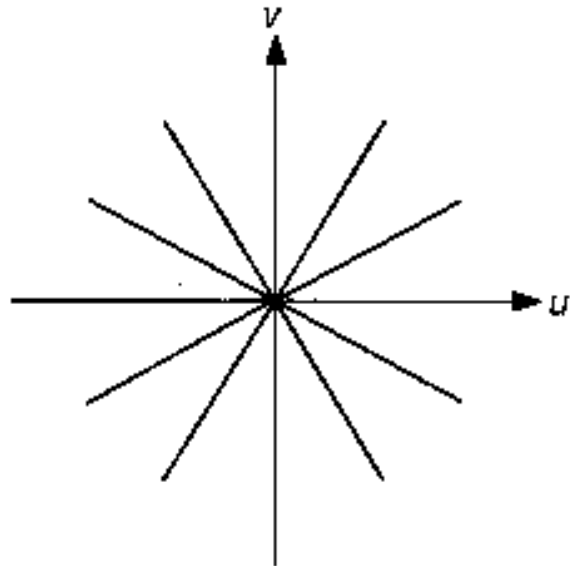
- The 2D function f is written as a sum of sinusoids.
- The DFT of f convolved with g is the product of their DFTs.

Spectral Analysis

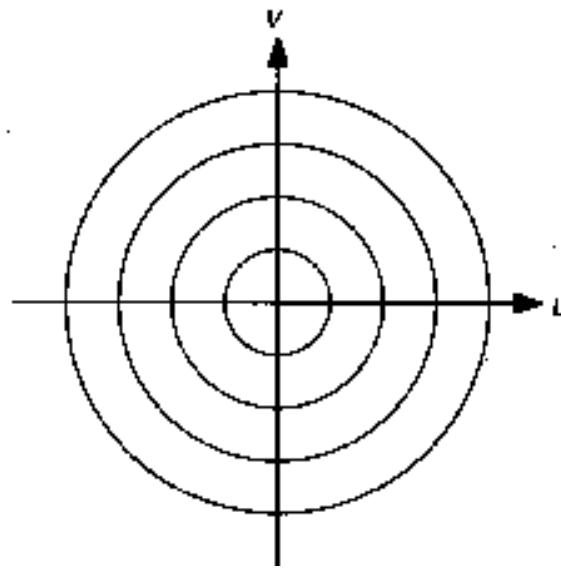
Lines in the DFT modulus images capture the main orientations in the image.



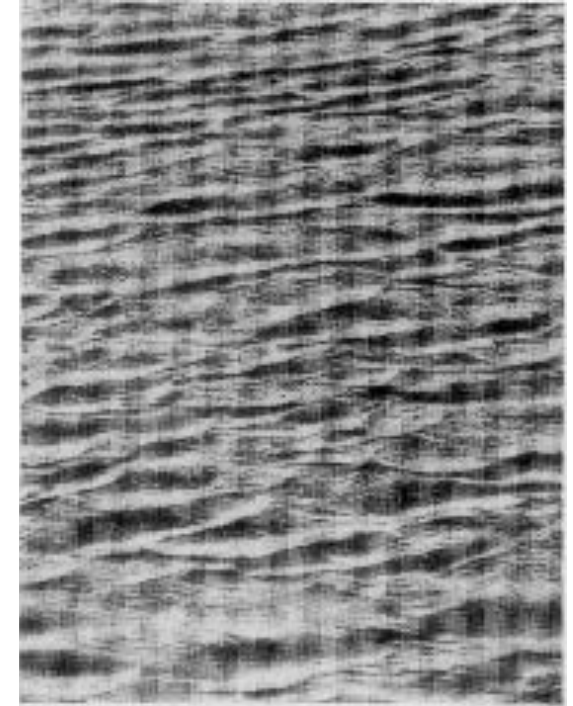
Texture Analysis



Angular bins
in $|DFT|$ image

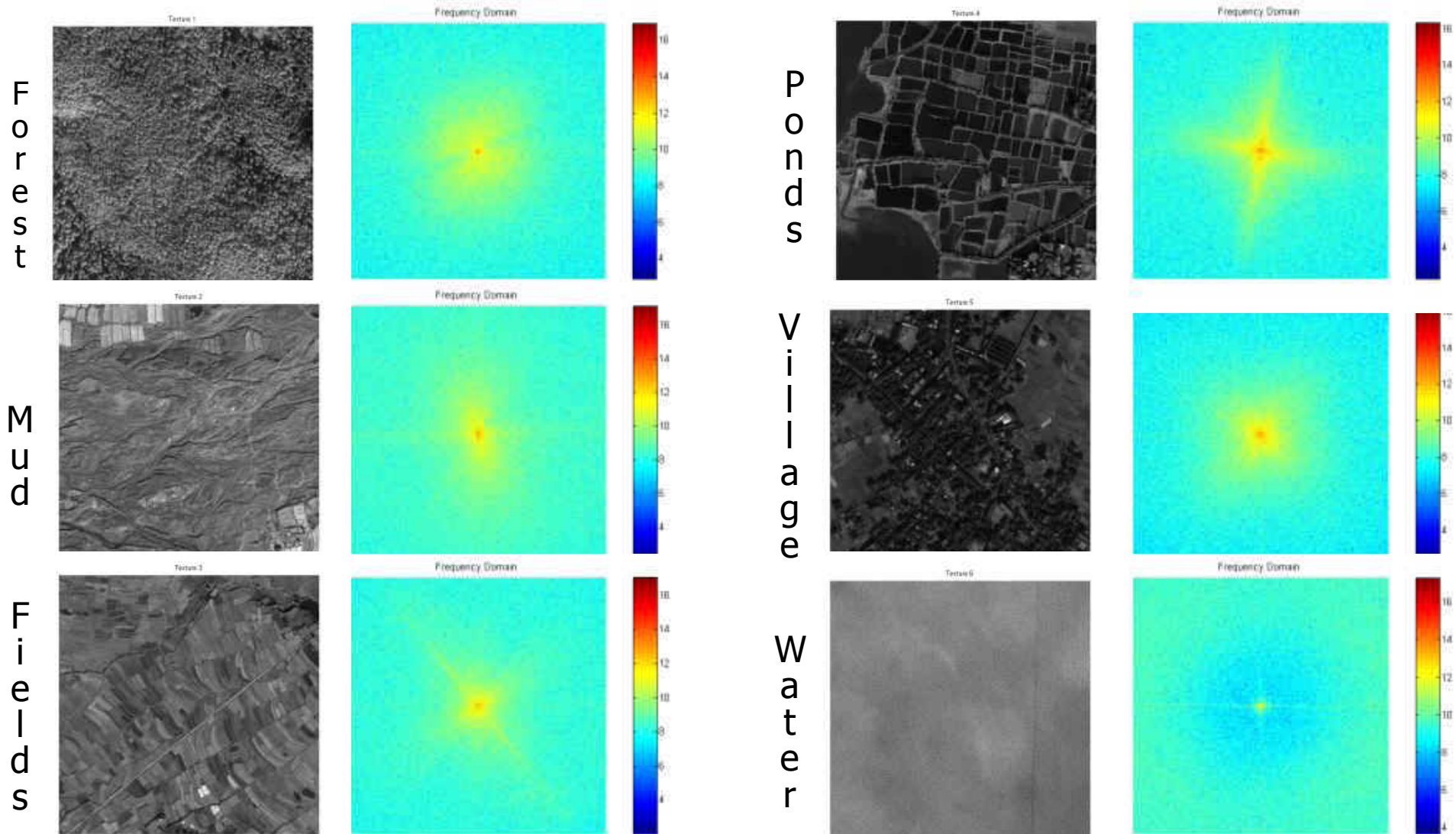


Radial bins
in $|DFT|$ image



Angular and radial bins in the Fourier domain capture the directionality and fluctuation speed of an image texture, respectively.

Fourier Texture Classification



- For some types of textures, the Fourier spectra are easily distinguishable.
- A classifier can be trained to tell them apart.
- However, one must have the same texture in the whole image patch.

Limitations

- DFT on small patches is subject to severe boundary effects.
- Only applicable if texture is uniform over large areas.
- Results can be improved by using wavelets instead, but only up to a point.
 - > More local metrics are required.

Statistical Metrics

First order gray-level statistics:

- Statistics of single pixels in terms of histograms.
- Insensitive to neighborhood relationships.

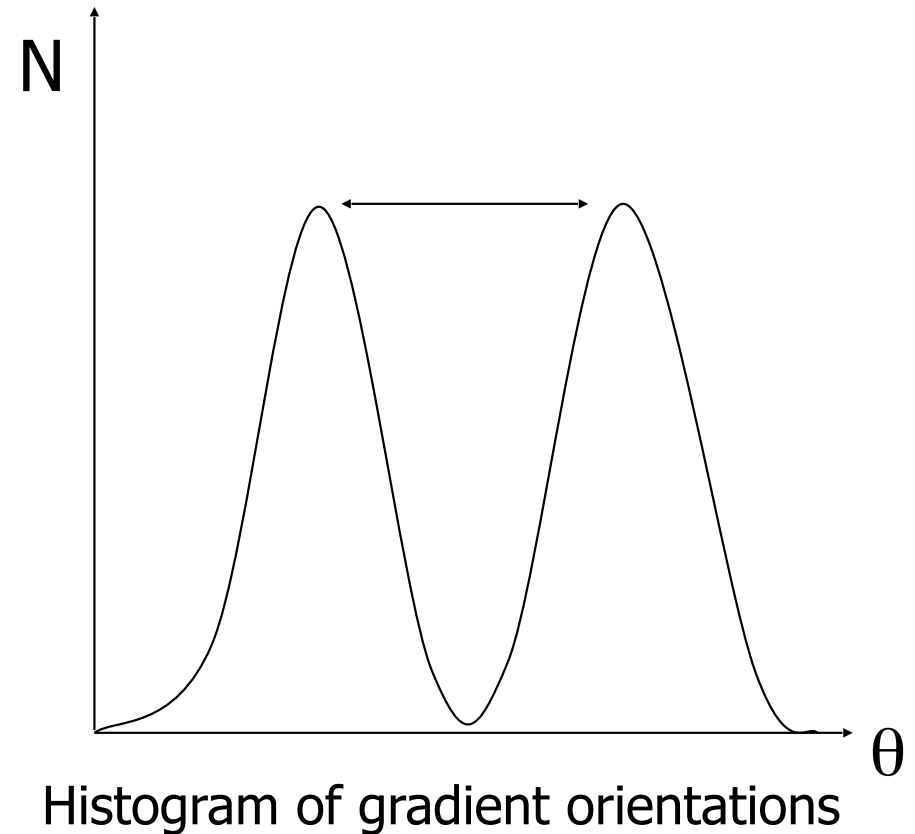
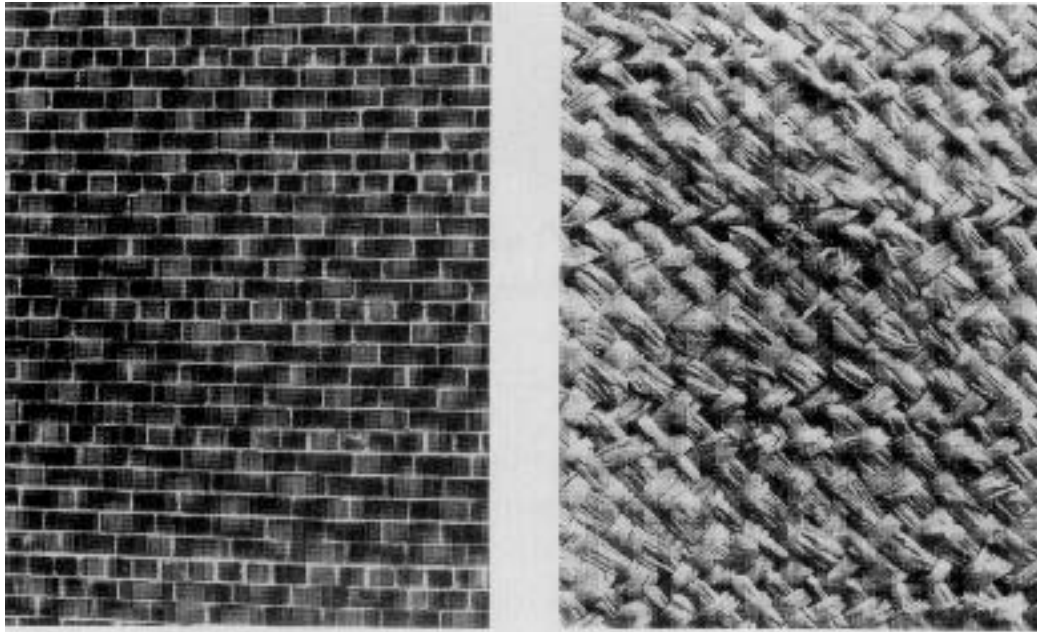
Second order gray-level statistics:

- Statistics of pixel pairs.

Filter-based measures:

- Statistics of whole neighborhoods.

Simple First Order Measure



The orientation histogram gives a clue to the orientation of the underlying plane.

More First Order Measures

Edge Density and Direction:

- Edge detection as a first step in texture analysis.
- The number of edge pixels in a fixed-size region tells us how busy that region is.
- The directions of the edges also help characterize the texture

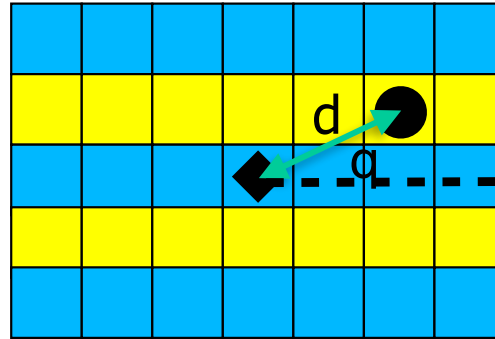
Edgeness per unit area:

- $|\{ p : \text{gradient_magnitude}(p) \geq \text{threshold} \}| / N$ where N is the unit area or region.

Edge magnitude and direction histograms:

- $\{ H_G, H_t \}$

Second Order Measures



Histogram of the co-occurrence of particular intensity values in the image.

- Specified in terms of geometric relationships between pixel pairs:
 - Distance
 - Orientation
- $P(i,j,d,\theta)$ Frequency with which a pixel with value j occurs at distance d and orientation θ from a pixel with value i .

Simple Example

If $I = \begin{bmatrix} 0 & 1 & 2 & 3 & 1 \\ 2 & 1 & 3 & 1 & 1 \\ 0 & 0 & 2 & 2 & 1 \\ 1 & 2 & 0 & 3 & 1 \\ 0 & 0 & 0 & 0 & 3 \end{bmatrix},$

then $H = \begin{bmatrix} 4 & 1 & 1 & 2 \\ 0 & 1 & 2 & 1 \\ 1 & 2 & 1 & 1 \\ 0 & 3 & 0 & 0 \end{bmatrix},$

and $P(l, m, 1, 0) = \frac{H(l, m)}{20}.$

Co-Occurrence Matrix

No need to distinguish between

$$P(m, l, \Delta i, \Delta j)$$

and

$$P(l, m, \Delta i, \Delta j)$$

→ Co-Occurrence matrix C :

$$C = H + H^T$$

Second Order Measures

Contrast:

$$\sum_{i,j=0}^{N-1} P_{i,j}(i-j)^2$$

Dissimilarity:

$$\sum_{i,j=0}^{N-1} P_{i,j}|i-j|$$

Homogeneity:

$$\sum_{i,j=0}^{N-1} \frac{P_{i,j}}{1+(i-j)^2}$$

and many more

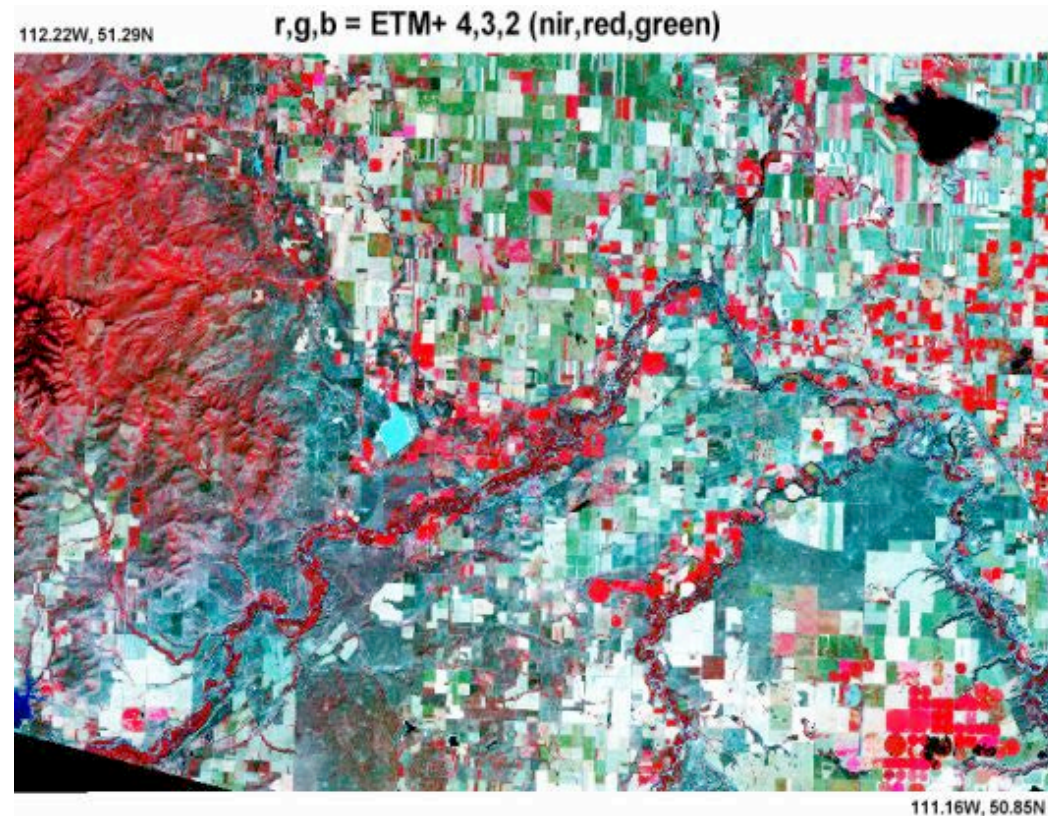
Angular Second Moment (Energy, Uniformity):

$$\sum_{i,j=0}^{N-1} P_{i,j}^2$$

Entropy:

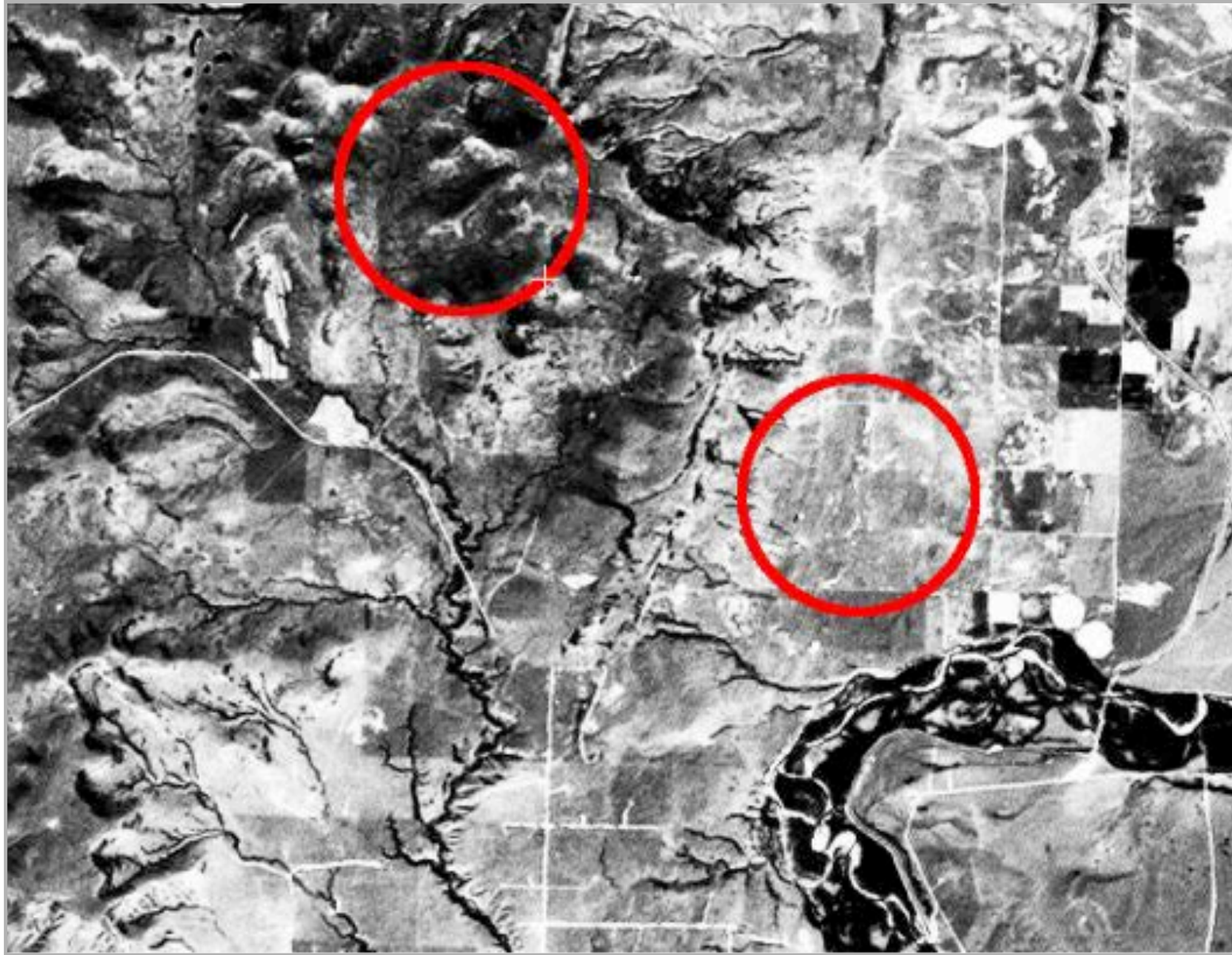
$$\sum_{i,j=0}^{N-1} P_{i,j}(-\ln P_{i,j})$$

Landsat Image



The image is excerpted from Path 41, Row 25 of Landsat 7 ETM+, dated 4 September 1999. This is an area in the Rocky Mountain Foothills near Waterton National Park, Alberta. The western edge of the image contains steep slopes and deep valleys. To the east is both grassland and annual crops, mostly grains. The eastern area is bisected by numerous small streams.

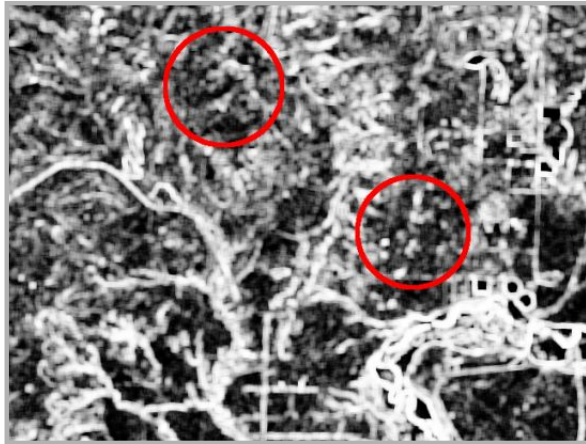
Full Resolution



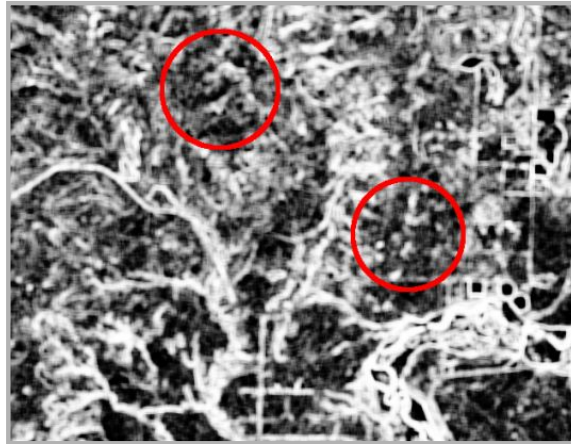
Let us consider two areas, one in the hills, the other in the plain.

Using Second Order Measures

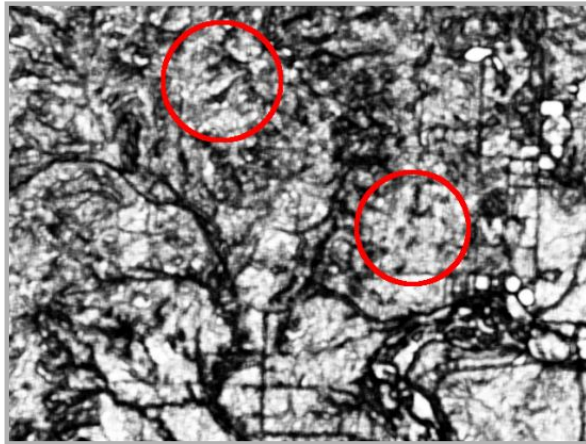
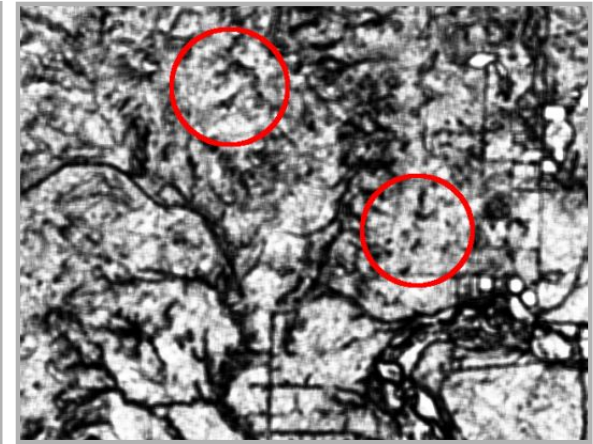
Contrast



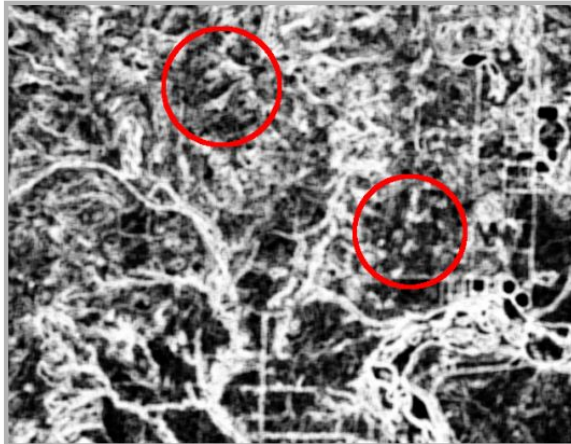
Dissimilarity



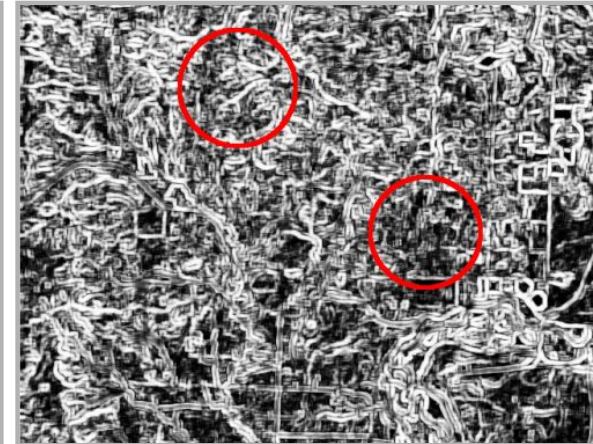
Homogeneity



ASM



Entropy



Correlation

The various measures within the two areas are sufficiently different for a classifier to easily distinguish them.

Classification

Used to identify eight terrain classes:

- Old residential
- New residential
- Urban
- Lake
- Swamp
- Scrub
- Wood



Parameter Choices

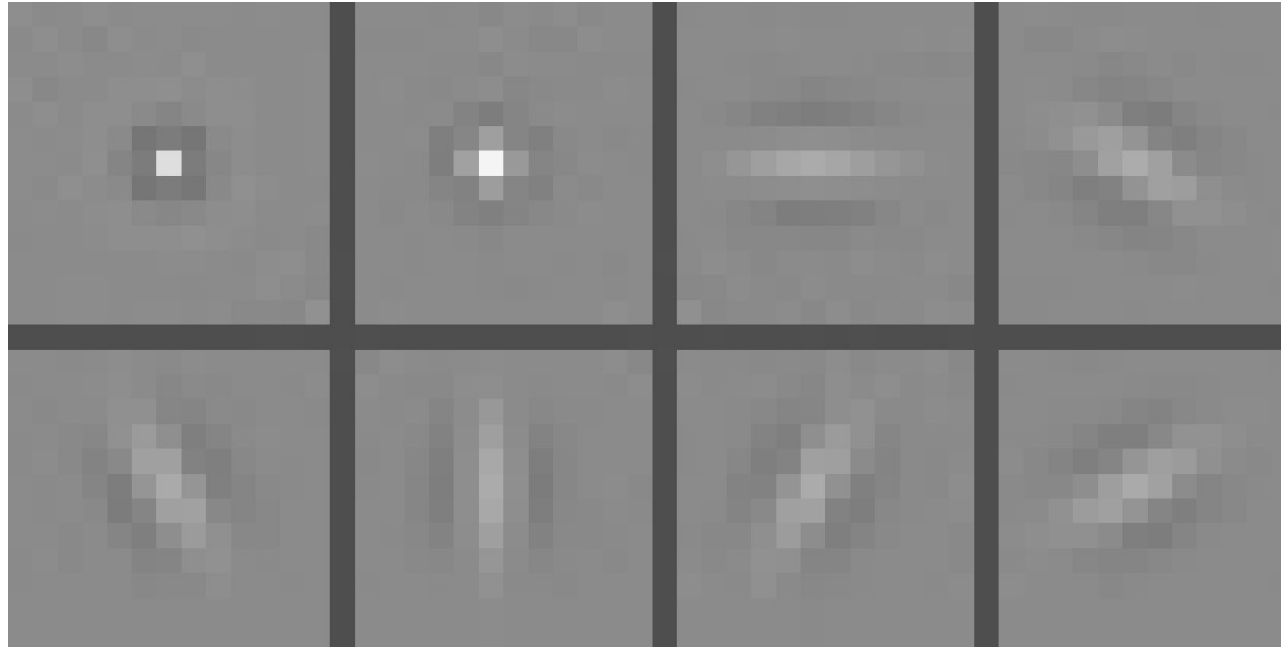
Using co-occurrence matrices requires choosing:

- window size,
- direction of offset,
- offset distance,
- what channels to use,
- what measures to use.

How do we choose these parameters?

- Critical question for **all** statistical texture methods.
- Can be addressed using Machine Learning.

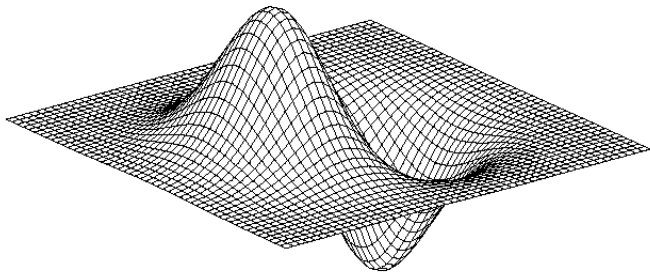
Filter Based Measures



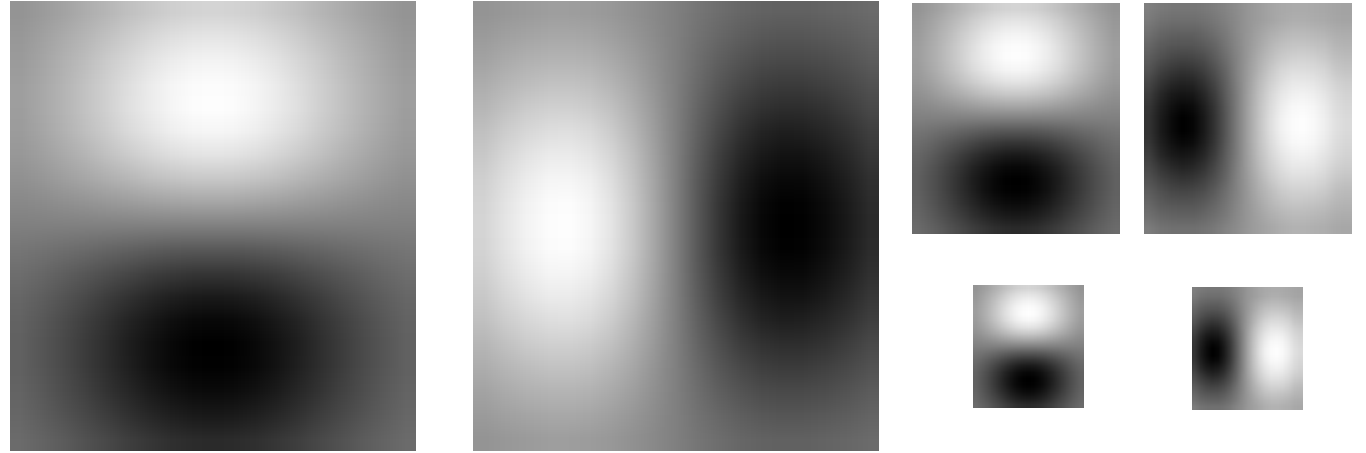
Represent image textures using the responses of a collection of filters.

- An appropriate filter bank will extract useful information such as spots and edges.
- Traditionally one or two spot filters and several oriented bar filters.

Gaussian Filter Derivatives



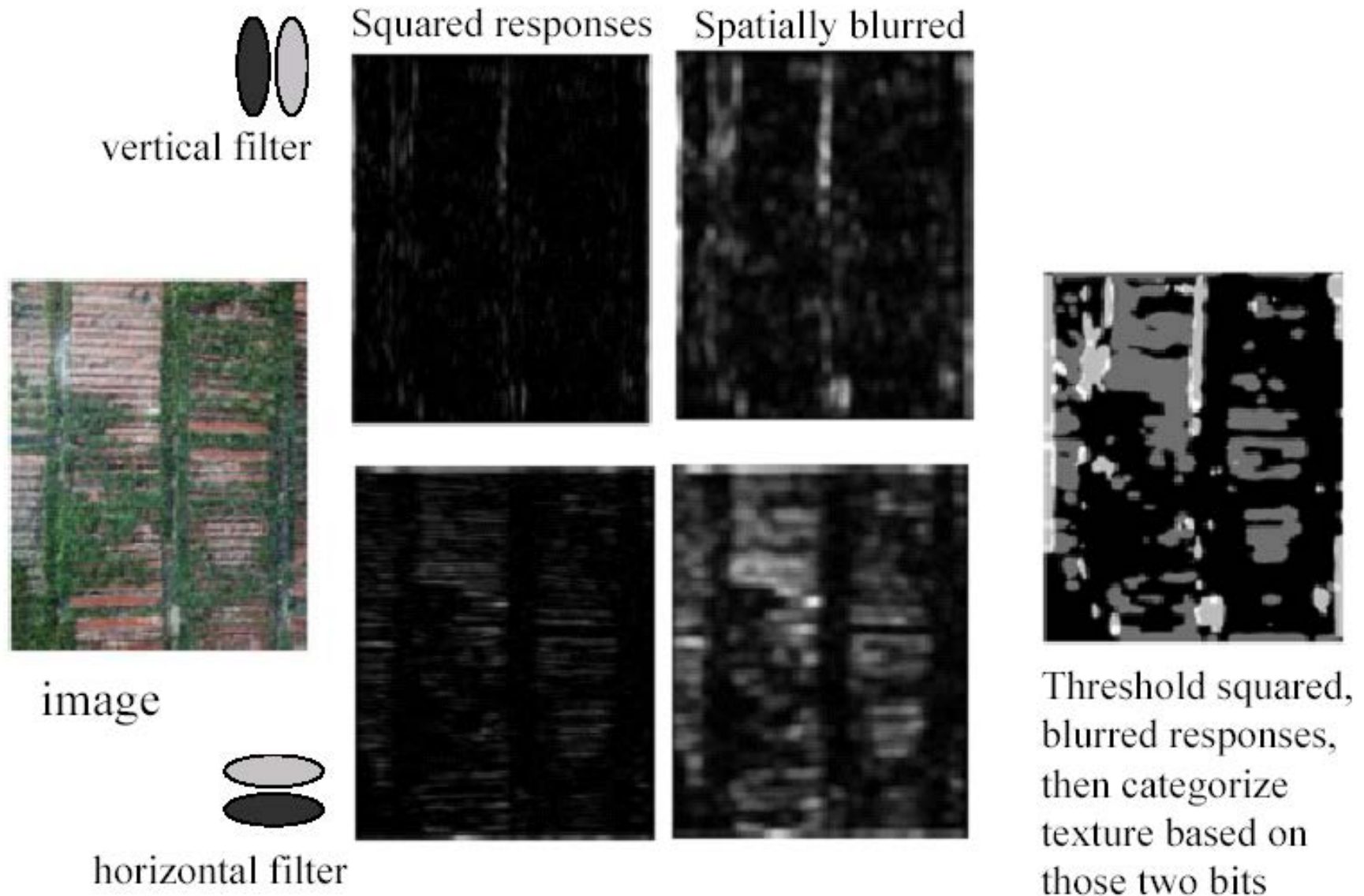
Gaussian Derivative



x and y derivatives at different scales

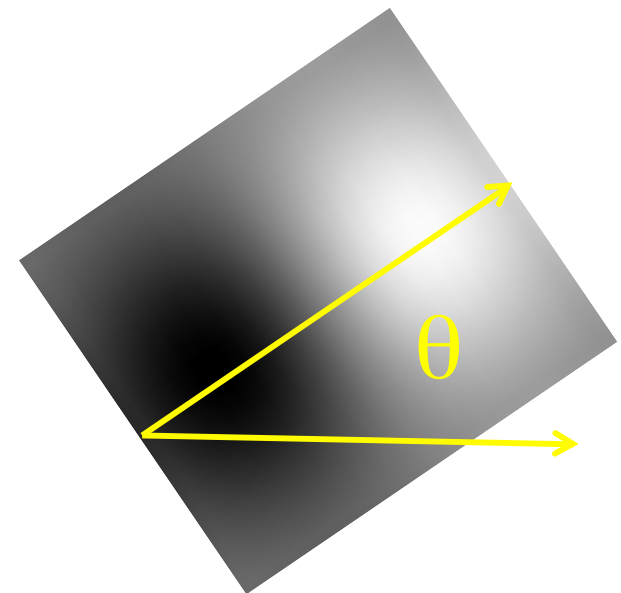
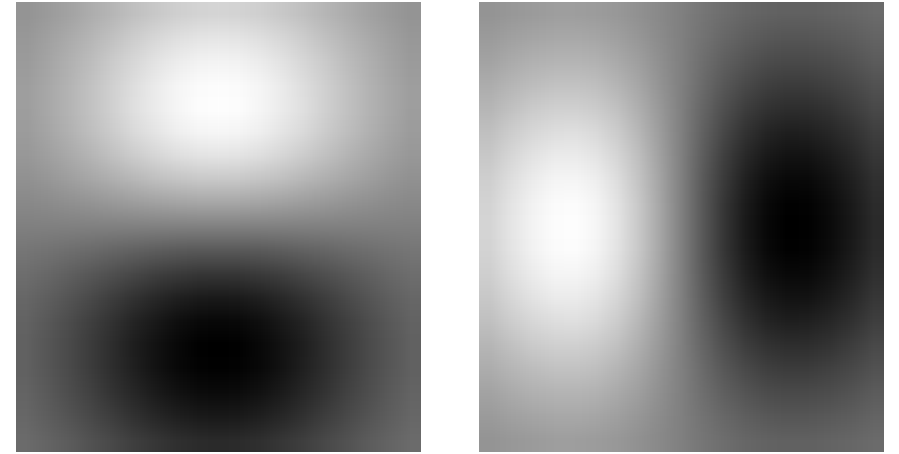
These filters respond to horizontal and vertical edges.

Horizontal and Vertical Structures

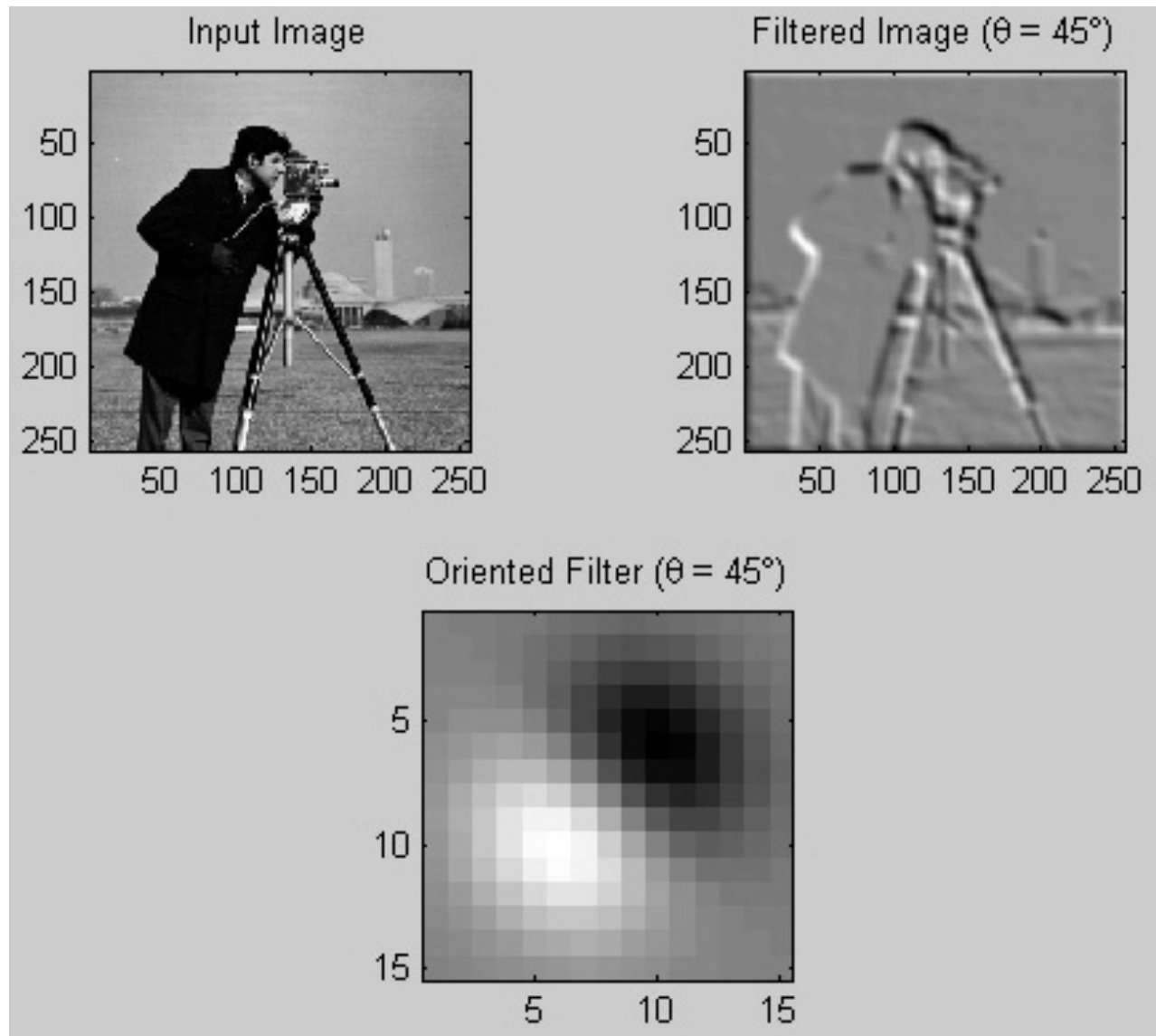


Oriented Filters

$$\frac{\partial I}{\partial \theta} = \cos(\theta) \frac{\partial I}{\partial x} + \sin(\theta) \frac{\partial I}{\partial y}$$

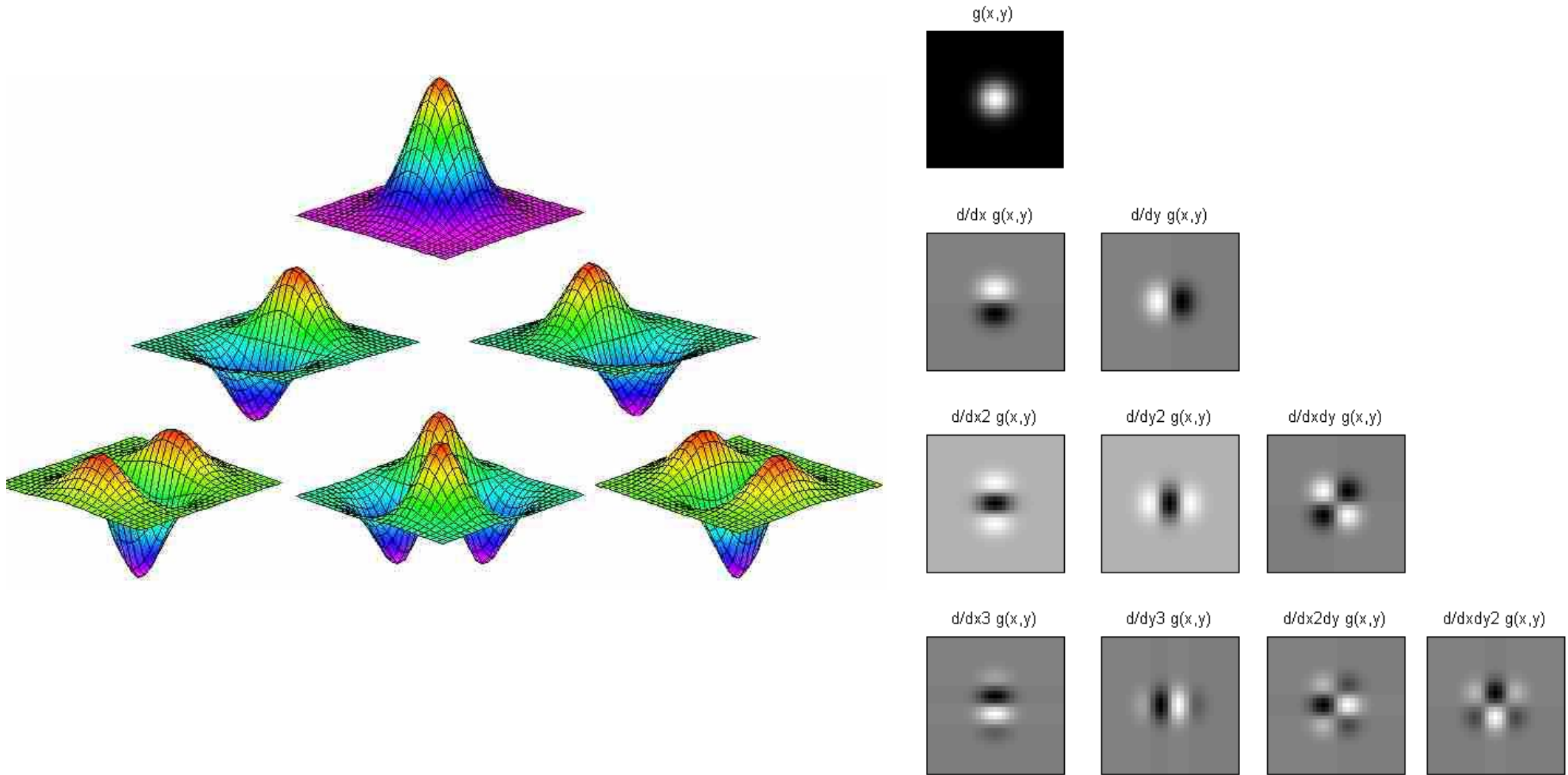


Directional Gradients



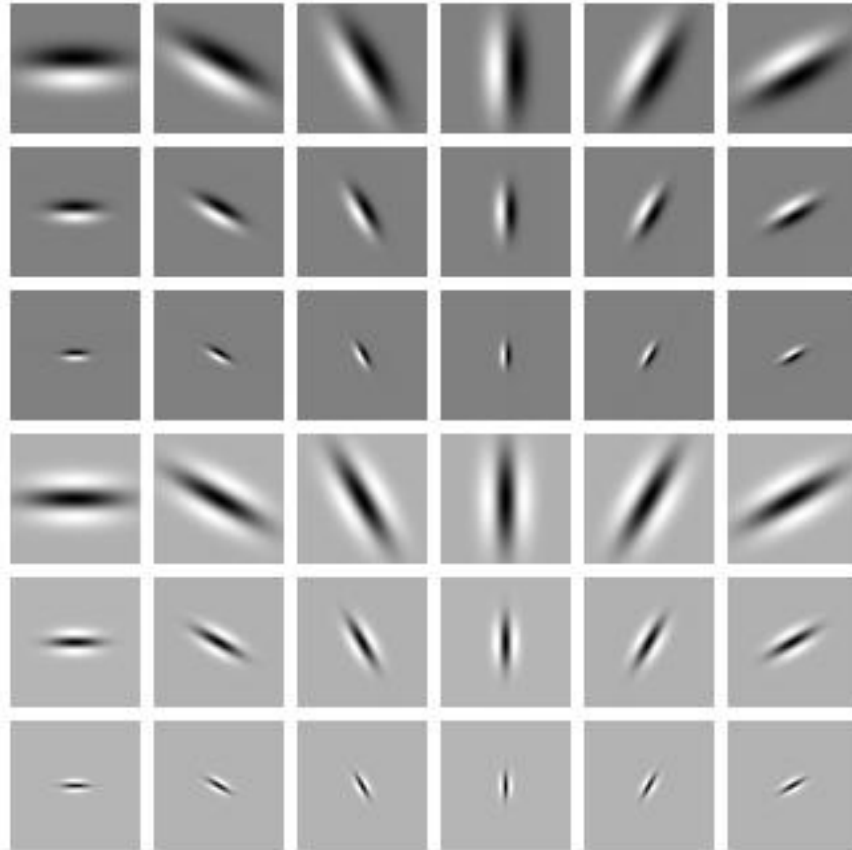
Oriented filters respond to edges in a specific direction.

Higher Order Derivatives

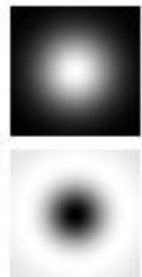


Higher-order derivatives of the Gaussian filters can be used to compute higher-order image derivatives.

Filter Bank

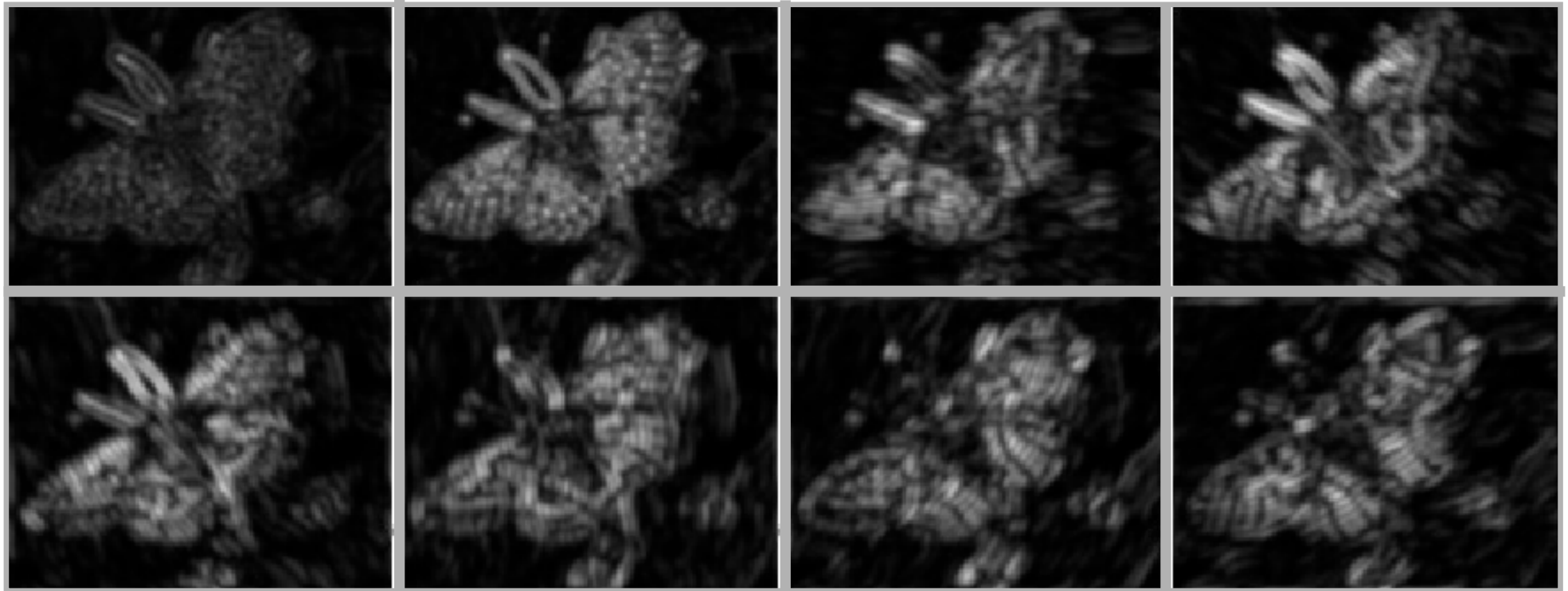


- Different scales.
- Different orientations.
- Derivatives order 0, 1, 2 ..



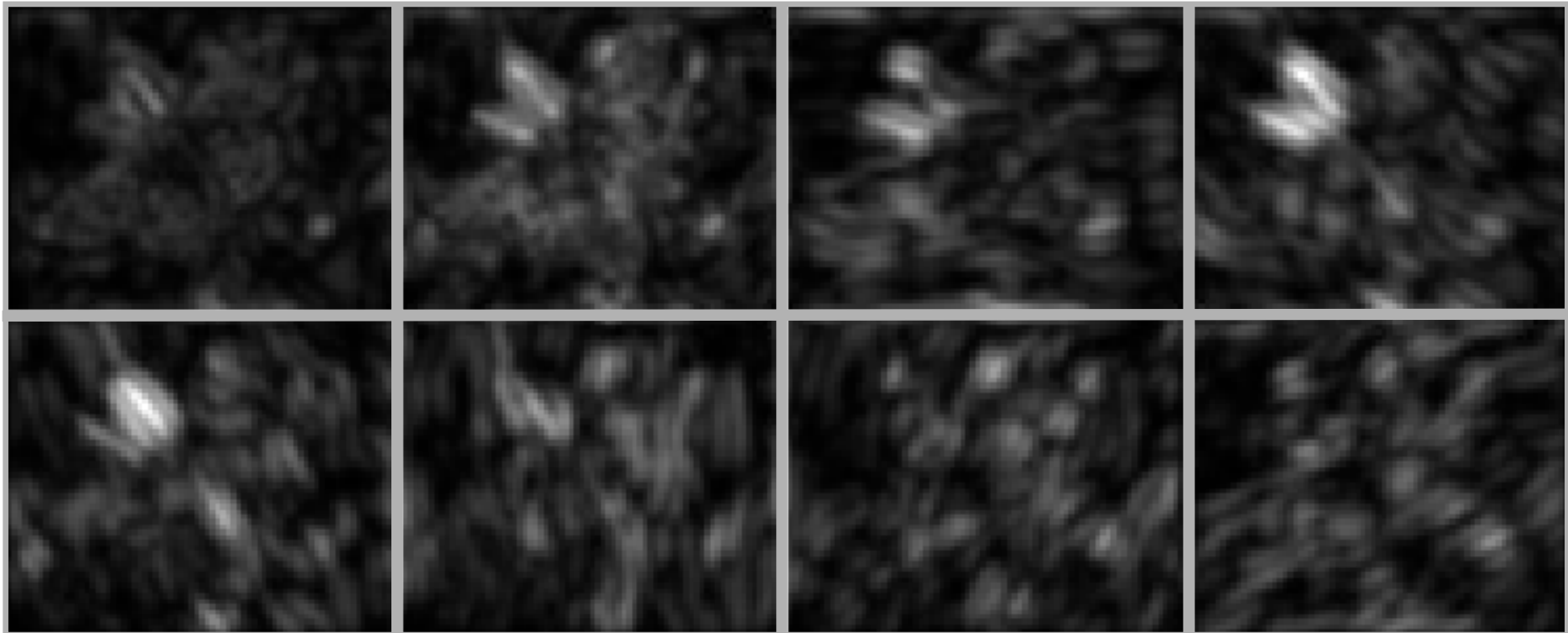
—> For every image pixel, compute a vector of responses to each filter.

Filter Responses: Small Scales



Gaussian filters with a small s . Capture local details.

Filter Responses: Large Scales



Gaussian filters with a large s . Capture larger details.

Gabor Filters

Gabor filters are the products of a Gaussian filter with oriented sinusoids. They come in pairs, each consisting of a symmetric filter and an anti-symmetric filter:

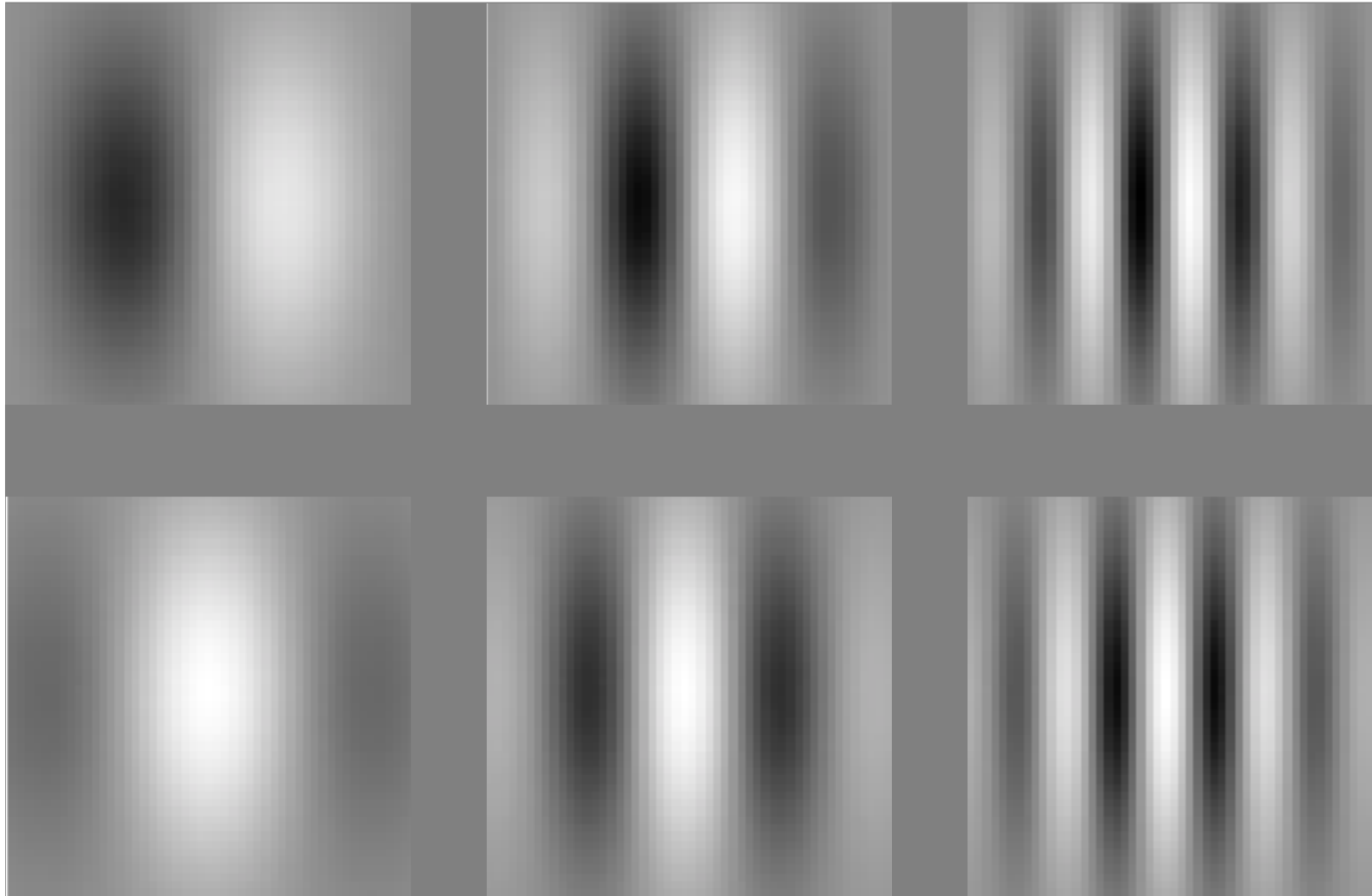
$$G_{\text{sym}}(x, y) = \cos(k_x x + k_y y) \exp\left(-\frac{x^2 + y^2}{2\sigma^2}\right)$$

$$G_{\text{asym}}(x, y) = \sin(k_x x + k_y y) \exp\left(-\frac{x^2 + y^2}{2\sigma^2}\right)$$

where k_x and k_y determine the spatial frequency and the orientation of the filter and σ determines the scale.

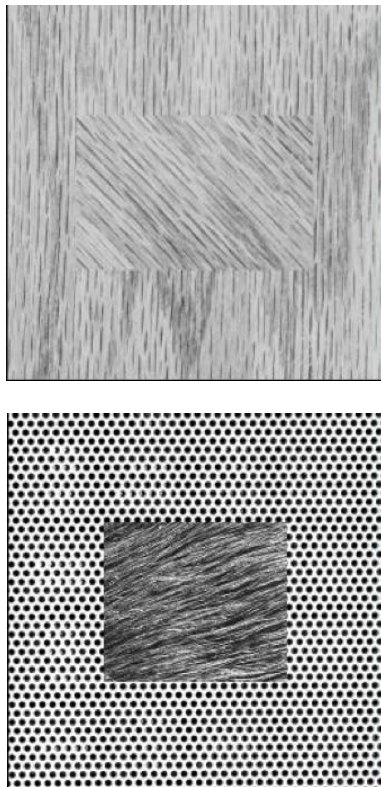
→ A filter bank is formed by varying the frequency, the scale, and the filter orientation

Vertical Derivatives

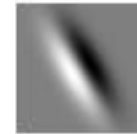
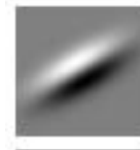


Gabor Responses

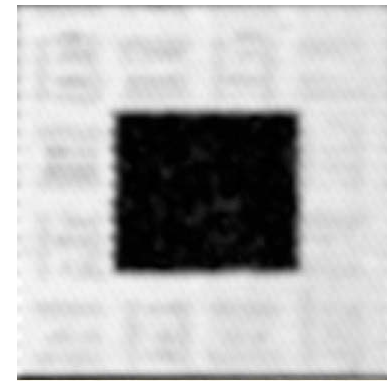
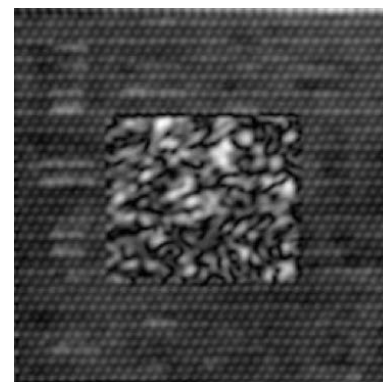
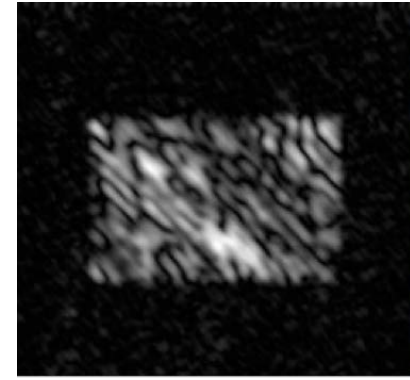
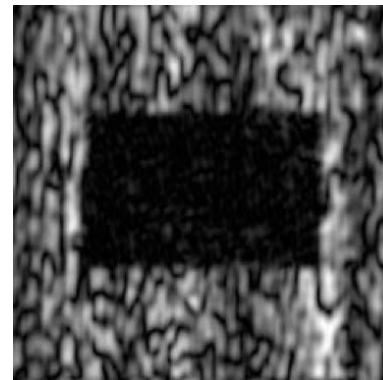
Images:



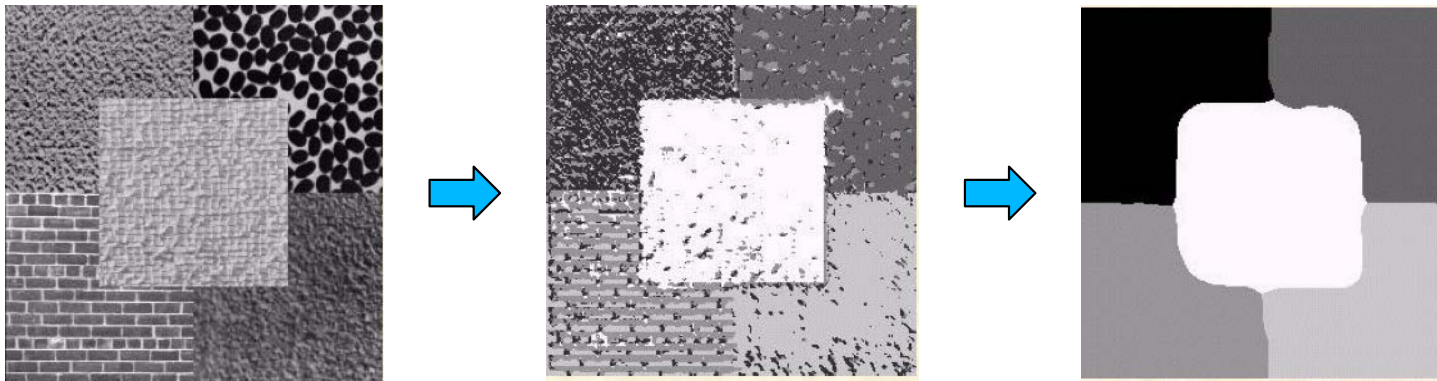
Filters:



Responses:

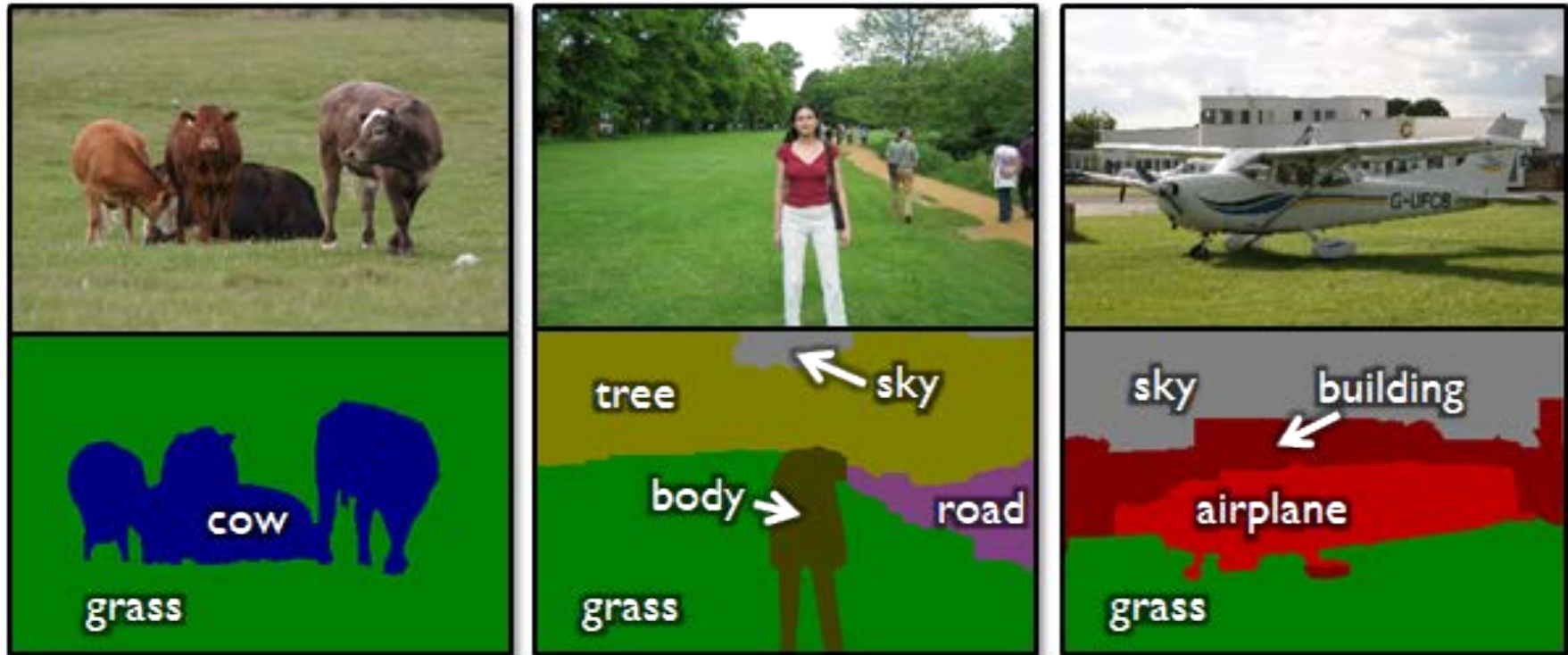


GABOR FILTER CHARACTERISTICS



- Respond strongly at points in an image where there are components that locally have a particular spatial frequency and orientation.
- In theory, by applying a very large number of Gabor filters at different scales, orientations and spatial frequencies, one can analyze an image into a detailed local description.
- In practice, it is not known how many filters, at what scale, frequencies, and orientations, to use. This tends to be application dependent.

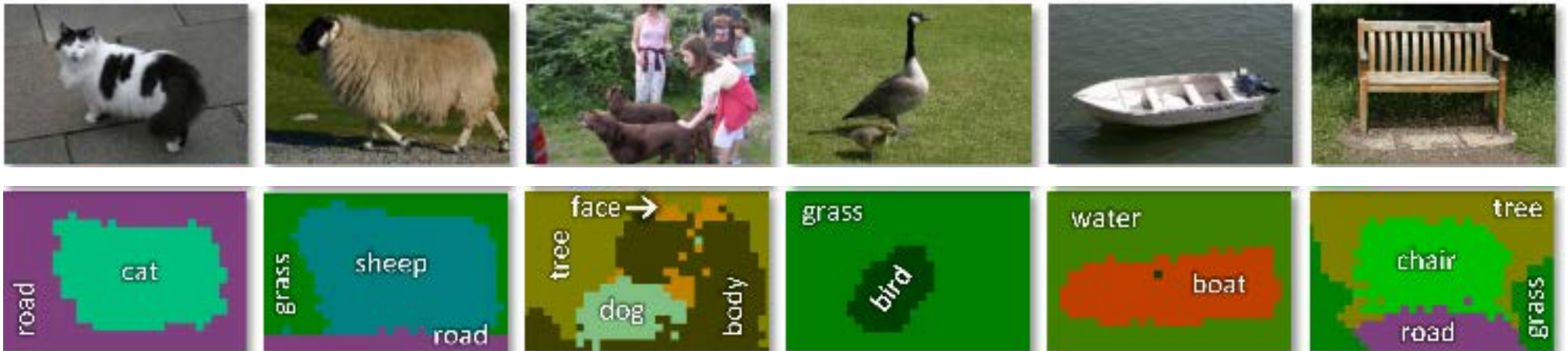
ML to the Rescue: Texton Boost



object classes	building	grass	tree	cow	sheep	sky	airplane	water	face	car
bicycle	flower	sign	bird	book	chair	road	cat	dog	body	boat

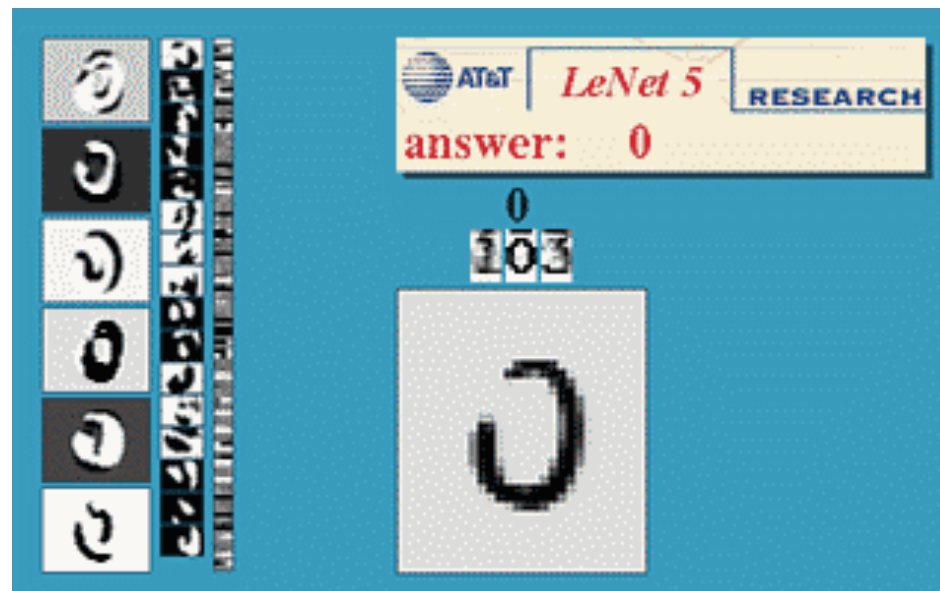
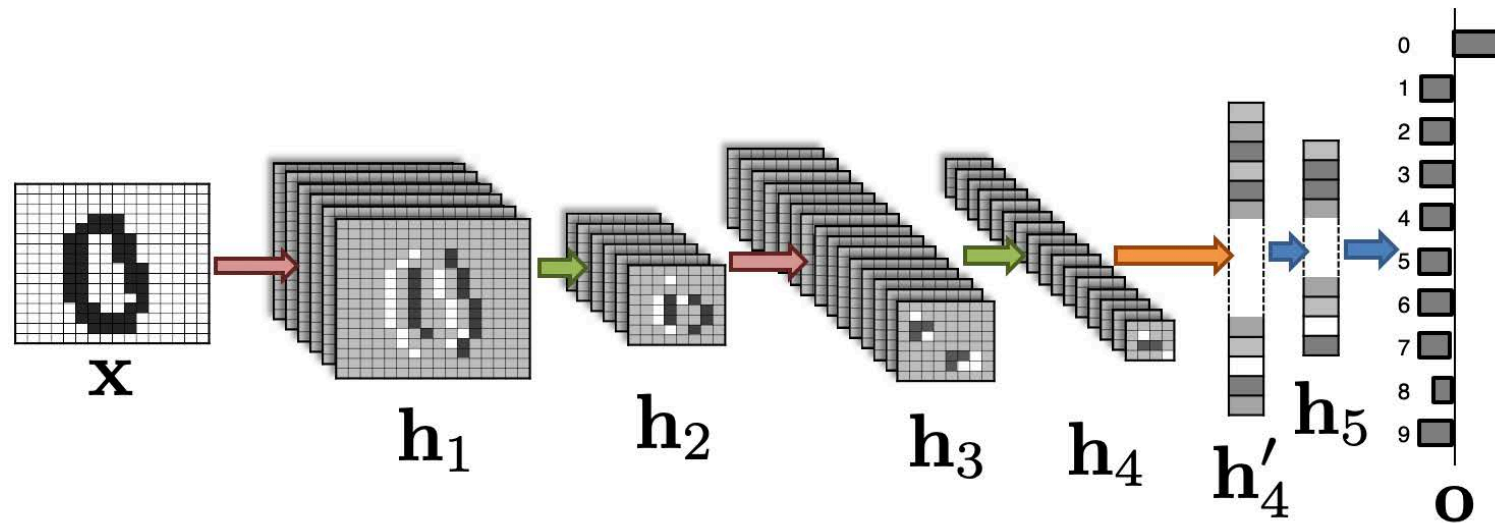
Use AdaBoost to perform classification on the output of Gabor filters.

ML to the Rescue: Texton Forests

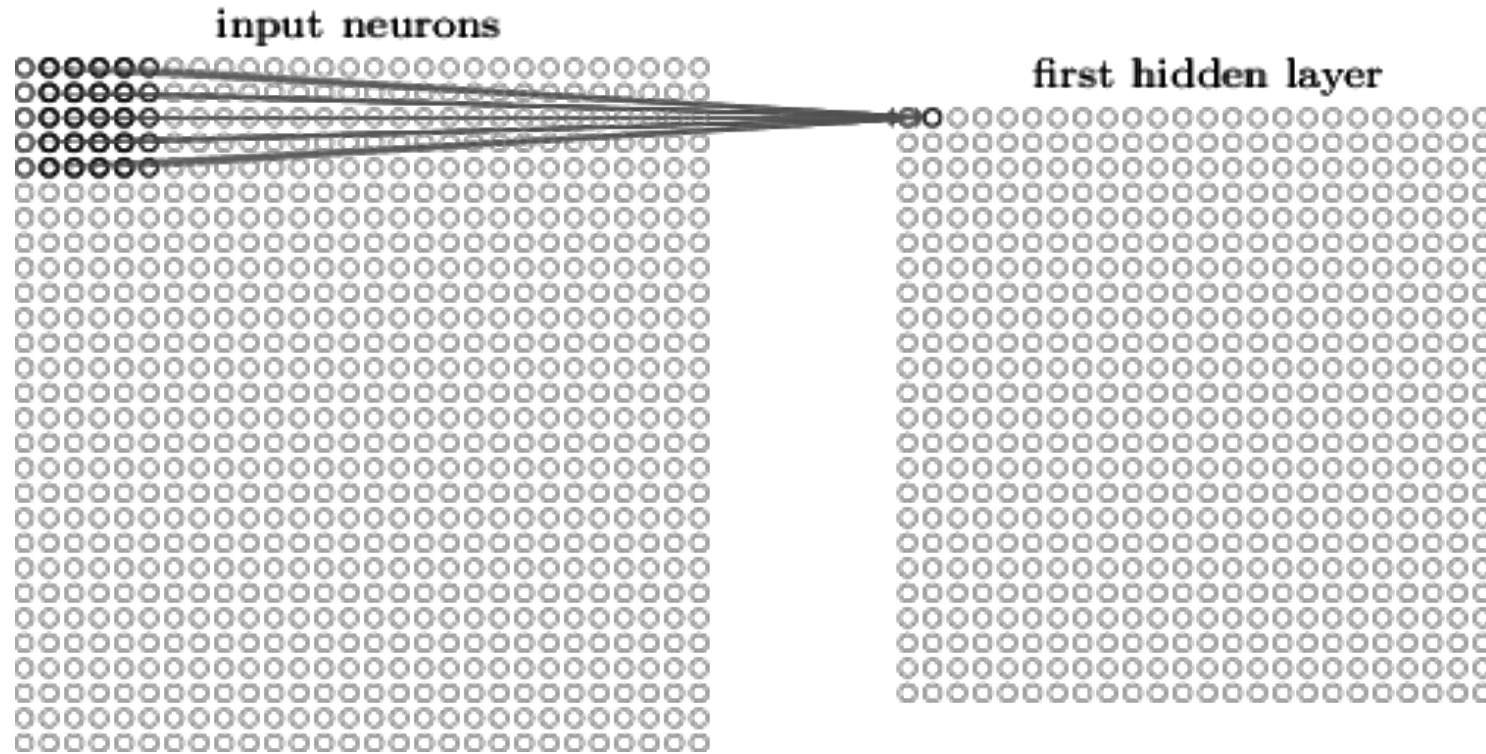


- Using Decision Forests to perform classification on the output of Gabor filters works better in this case.
- But what works even better, is

Reminder: ConvNets

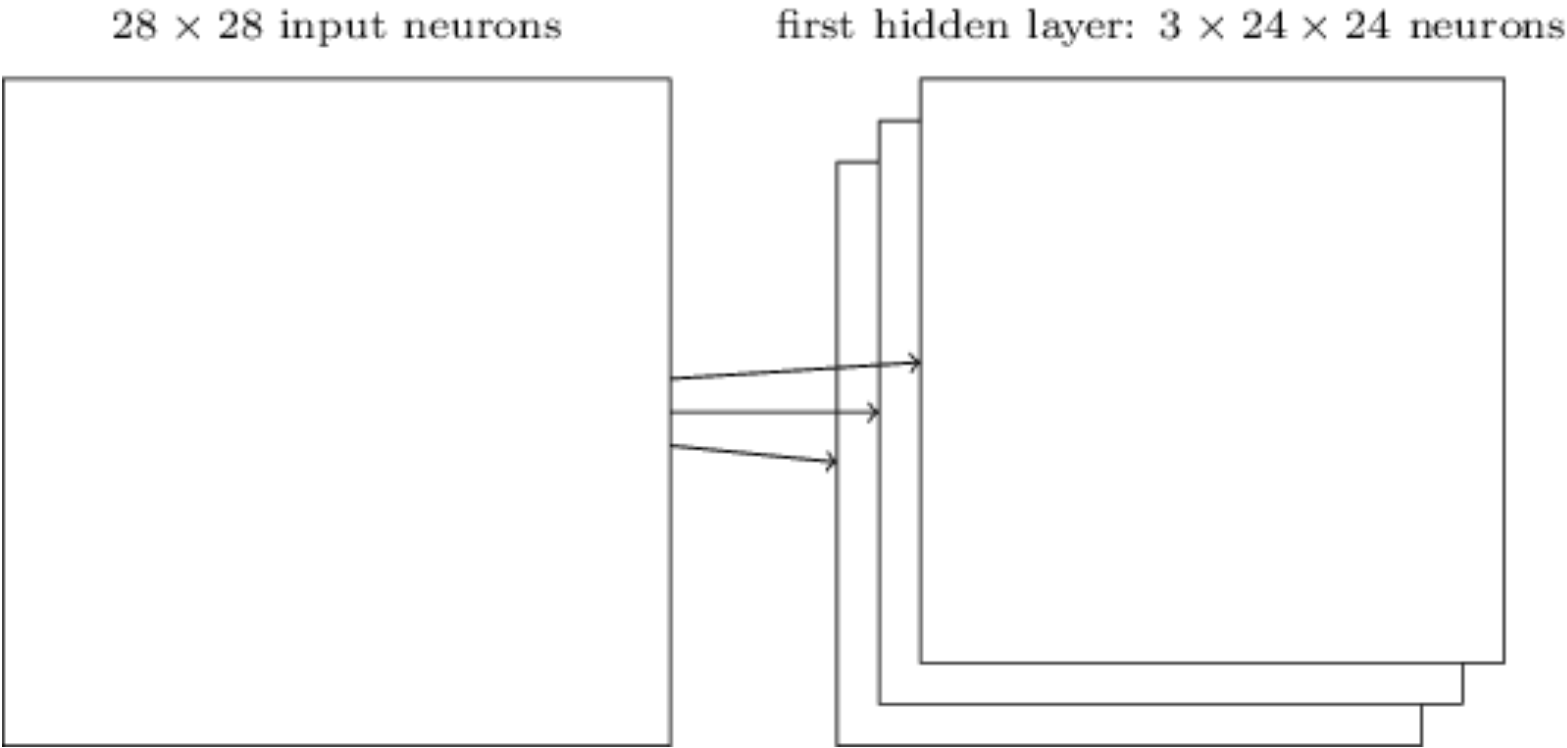


Reminder: Convolutional Layer

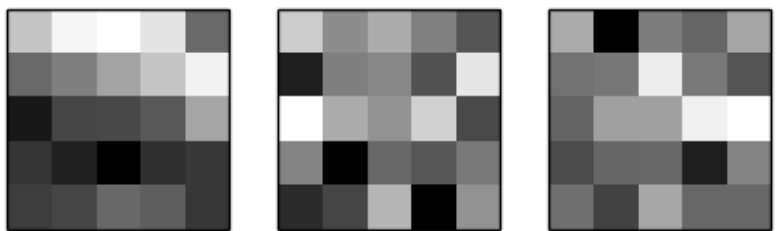


$$\sigma \left(b + \sum_{x=0}^{n_x} \sum_{y=0}^{n_y} w_{x,y} a_{i+x,j+y} \right)$$

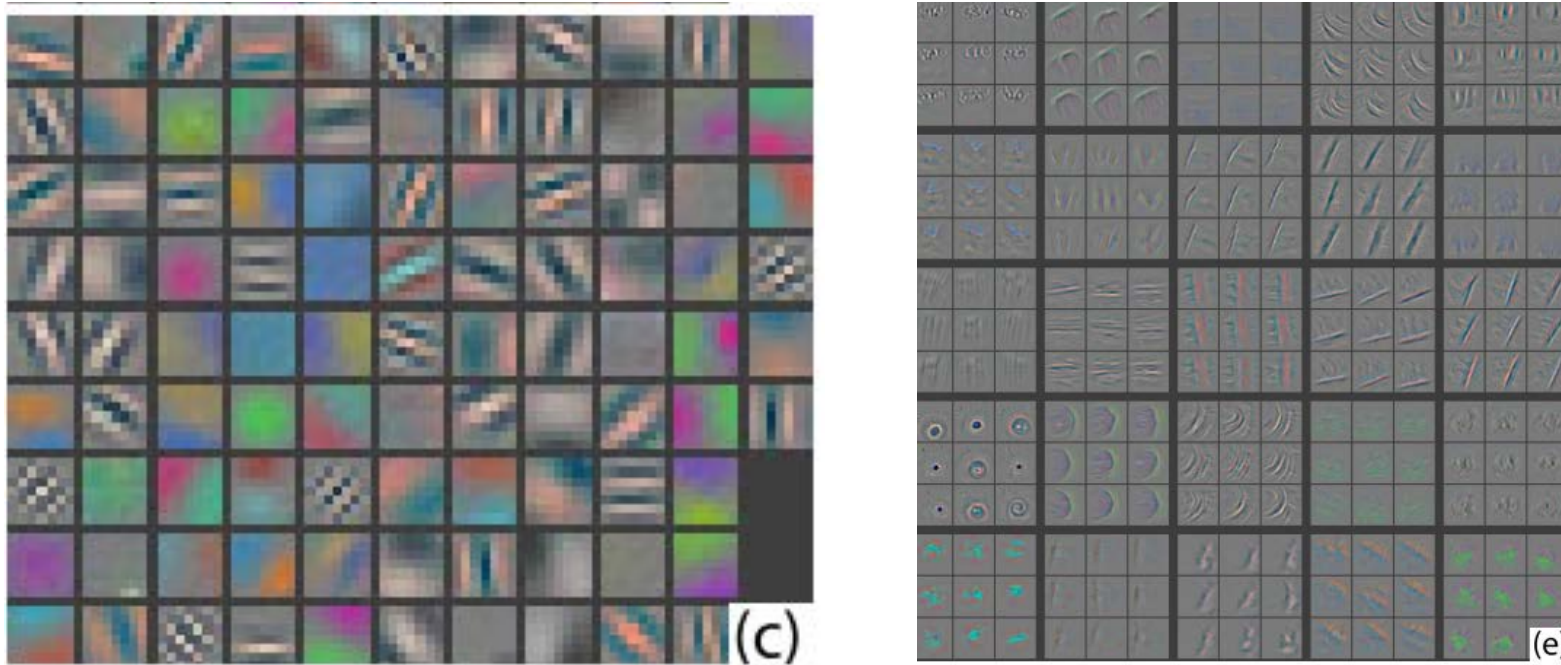
Reminder: Feature Maps



Filters:

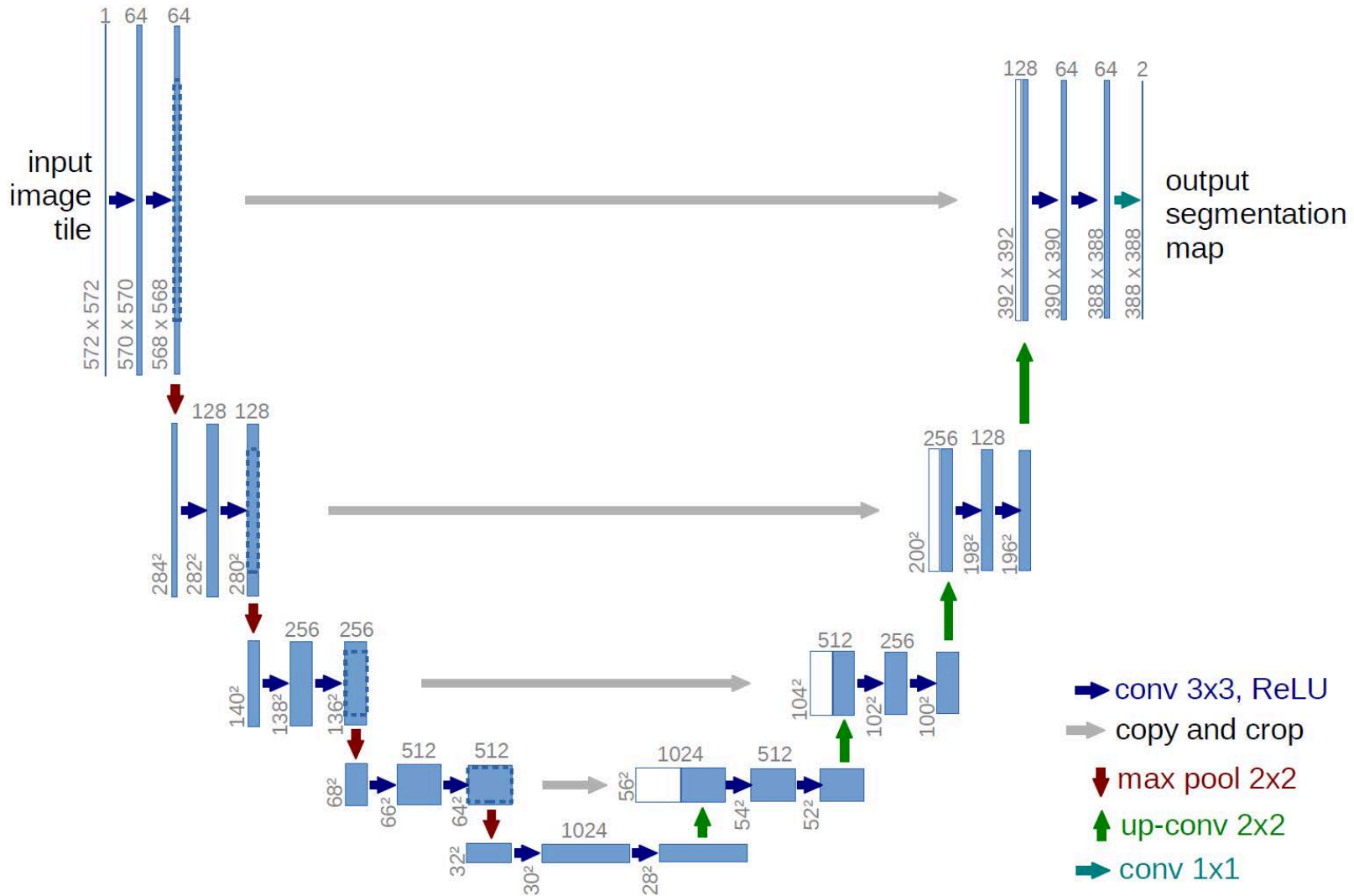
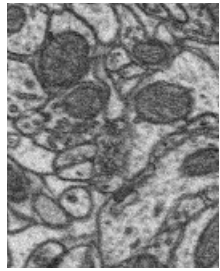


Learned Feature Maps



- Some of these convolutional filters look very Gabor like.
- The network requires a large training set to learn an effective filter bank.
- The older techniques still have their place in the absence of such training sets.

Reminder: U-Net Architecture



In Short

Texture is a key property of objects which is

- Non local
 - Non trivial to measure
 - Subject to deformations
- ➔ Hard to characterize formally and best used in conjunction with effective Machine Learning techniques.
- ➔ This seems to be exactly what Convolutional Neural Nets do.